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NASA TECHNICAL NOTE**NASA TN D-1864****NASA TN D-1864****FLUX PATTERNS RESULTING FROM
FREE-MOLECULE FLOW THROUGH
CONVERGING AND DIVERGING SLOTS**

by Thaine W. Reynolds and Edward A. Richley
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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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SUMMARY

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Equations for the determination of particle flux at a location downstream of the exit of convergent and divergent two-dimensional slots for gas flow through the slot under free-molecule conditions have been derived and solved numerically. Slot configurations range from length to inlet width ratios of 0.25 to 8 and wall half-angles from 75° divergent to 60° convergent.

Flux distribution patterns along surfaces of constant radius from the slot exit centerplane and in planes normal to the slot centerplane are presented for varying distances from the slot exit. Flux along the centerplane close to the slot exit is higher for the smaller length-to-width-ratio slots and becomes less a function of the length to inlet width ratio as the distance from the slot exit increases. As the length to inlet width ratio of the slot increases, the angle giving maximum flux along the centerplane approaches zero (i.e., a parallel-walled slot). A maximum value of flux along the centerplane is obtained in the far field with divergent slots.

Larger length-to-inlet-width-ratio slots give a more collimated beam than do small length to inlet width ratios, and a divergent slot yields a more collimated beam than a convergent slot having the same length to inlet width ratio. The normalized flux patterns for the convergent and divergent slots in the far field follow the cosine distribution law out to angles from the centerplane equal in magnitude to the wall half-angle; beyond this angle the normalized flux falls below the cosine distribution law.

Austin

INTRODUCTION

The gas flow patterns that are obtained from the exit of nozzles or orifices under free-molecule-flow conditions are frequently required in the design of electrostatic thrusters (refs. 1 to 5). Such patterns may also have applicability to a wide range of flow problems in vacuum and space technology. Analytical or experimental determinations of gas profiles under free-molecule-flow conditions have been very limited. Clausing (ref. 6) calculated the far-field flux patterns for flow through short cylindrical tubes (length to radius ratios less than 2). More recently, in reference 7, his analysis has been

extended to include larger length to radius ratios. An experimental determination of far-field gas profiles from cylindrical tubes is given in reference 8.

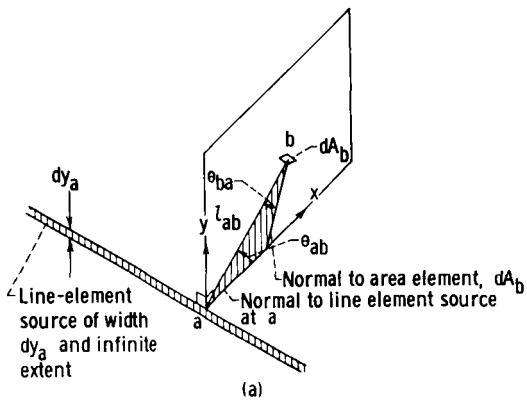
The present report deals with flux distribution patterns resulting from gas flow under free-molecule conditions with diffuse wall reflection through divergent, convergent, and parallel-walled slots, which are two-dimensional (i.e., infinite in extent in a direction normal to the flow direction). The slot configurations, shown schematically in figure 1(a), vary in length to inlet width ratio from 0.25 to 8, and have wall half-angles from 75° divergent to 60° convergent. Two types of flux patterns are presented as shown in figure 1(b). In one, the angular distribution of flux is calculated for various radial distances with the origin taken to be on the centerplane at the exit plane of the slot. In the other, the lateral flux variation normal to the centerplane is determined for planes located at various distances from the slot exit plane. Both distributions are needed because the flux through two differential areas located at the same point, but at some angle to each other, cannot be simply related except at distances far from the slot exit. In each case the flux patterns were evaluated close to the slot exit and for continually increasing distances until the far field is reached. The far field is defined herein to mean that region (or, distance) where the normalized flux patterns become independent of the distance from the slot exit.

The relations for free-molecule flow presented herein are also applicable to certain radiation problems with diffuse reflection, since the flux of emitted radiation then follows the cosine distribution law and the geometric relations become identical to those for molecular flow.

CALCULATION PROCEDURE

The flux distribution downstream from the exit of the slots is calculated under the assumptions that gas flow into the slot is uniform and has a random directional distribution, that free-molecule-flow conditions exist throughout, and that particle reflections from the wall are diffuse. The relation from which the flux distributions are calculated is readily derived from the well-known cosine distribution law of emission from a line-element source (ref. 9). The relation is

$$dn_b = \frac{n_a \cos \theta_{ab} \cos \theta_{ba}}{2l_{ab}} dy_a \quad (1)$$



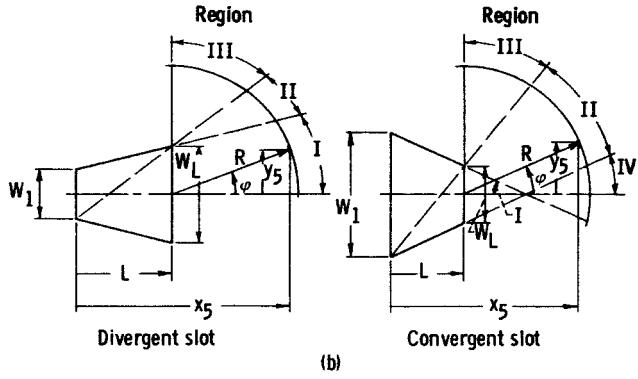
(All symbols are defined in appendix A.)
The geometric parameters given in equation (1) are shown in sketch (a) where

dn_b flux (particles per unit area per unit time) arriving at differential area dA_b from the line-element source dy_a

n_a flux leaving strip, dy_a

Flux Distribution on Surfaces of Constant Radius About Centerline of Exit Plane

Mathematical description of the flux along various radii R beyond the slot exit depends on the regions as noted in sketch (b) and figure 1(c). The regions are symmetrical about the slot centerplane.



convergent slots in planes that are beyond the point of intersection of the extension of the planes of the walls. The flux equations that apply for the various regions are presented next; derivations of these equations are given in appendix B.

Region I. - Region I is bounded by the relation

$$0 \leq \bar{y}_5 \leq \frac{\bar{W}_L}{2} + (\bar{x}_5 - \bar{L}) \tan \beta \quad (2)$$

The flux at point 5 in the radial direction ϕ is given by

$$\begin{aligned} \frac{n_5(\phi)}{n_1} &= \frac{1}{2R} \left\{ \frac{[(\bar{x}_5 - \bar{L})(1 - 2\bar{y}_5) + 2\bar{x}_5\bar{y}_5]}{\sqrt{4\bar{x}_5^2 + (1 - 2\bar{y}_5)^2}} + \frac{[(\bar{x}_5 - \bar{L})(1 + 2\bar{y}_5) - 2\bar{x}_5\bar{y}_5]}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right\} \\ &+ \int_0^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} \left\{ \frac{(1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta)[(1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta) \sin \phi + 2(\bar{x}_5 - \bar{x}_3) \cos \phi]}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right. \\ &\left. + \frac{(1 - 2\bar{y}_5 + 2\bar{x}_5 \tan \beta)[(1 - 2\bar{y}_5 + 2\bar{x}_3 \tan \beta) \sin \phi + 2(\bar{x}_5 - \bar{x}_3) \cos \phi]}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 - 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \end{aligned} \quad (3)$$

The first term in equation (3) is the direct flux from the inlet; the integral is the flux from the two walls.

Region II. - Region II is bounded by the relation

$$\frac{\bar{W}_L}{2} + (\bar{x}_5 - \bar{L}) \tan \beta \leq \bar{y}_5 \leq \frac{\bar{W}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{2} \left(\frac{\bar{W}_L + 1}{\bar{L}} \right) \quad (4)$$

The flux relation is

$$\frac{n_5(\phi)}{n_1} = \frac{1}{2R} \left[\frac{(\bar{x}_5 - \bar{L})(\bar{y}_1' - \bar{y}_5) + \bar{x}_5 \bar{y}_5}{\sqrt{\bar{x}_5^2 + (\bar{y}_1' - \bar{y}_5)^2}} + \frac{(\bar{x}_5 - \bar{L})(1 + 2\bar{y}_5) - 2\bar{x}_5 \bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right] + \int_0^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} d\bar{x}_3 \times \left\{ \frac{(1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta) [(1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta) \sin \phi + 2(\bar{x}_5 - \bar{x}_3) \cos \phi]}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \quad (5)$$

where

$$\bar{y}_1' = \frac{\bar{w}_L}{2} - \left[\frac{\bar{y}_5 - (\bar{w}_L/2)}{\bar{x}_5 - \bar{L}} \right] \bar{L}$$

Region III. - Region III is bounded by the relation

$$\bar{R} \geq \bar{y}_5 \geq \frac{\bar{w}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{2} \left(\frac{\bar{w}_L + 1}{\bar{L}} \right) \quad (6)$$

In region III there is no contribution from the inlet. The flux at point 5 is entirely from one wall and is given by the relation

$$\frac{n_5(\phi)}{n_1} = \int_{\bar{x}_3'}^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} d\bar{x}_3 \times \left\{ \frac{(1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta) [(1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta) \sin \phi + 2(\bar{x}_5 - \bar{x}_3) \cos \phi]}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \quad (7)$$

where the limit \bar{x}_3' is given by the relation

$$\bar{x}_3' = \frac{1}{1 + \left[\frac{\bar{x}_5 - \bar{L}}{\bar{y}_5 - (\bar{w}_L/2)} \right] \tan \beta} \left\{ \bar{L} - \left[\frac{\bar{x}_5 - \bar{L}}{\bar{y}_5 - (\bar{w}_L/2)} \right] \left[\frac{\bar{w}_L + 1}{2} \right] \right\} \quad (8)$$

Region IV. - Region IV occurs only for the convergent slots when

$$\bar{x}_5 > \frac{1}{2|\tan \beta|} \quad (9)$$

For this condition, the bounds of region IV are given by the relation

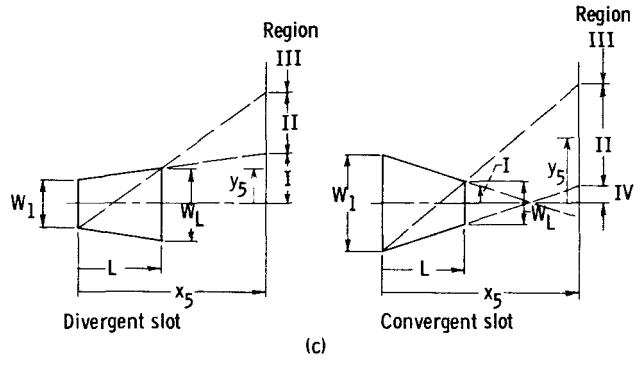
$$0 \leq \tan \phi \leq |\tan \beta| - \frac{\bar{W}_L \sec \phi}{2\bar{R}} \quad (10)$$

The flux at point 5 is then given by

$$\frac{n_5(\phi)}{n_1} = \frac{\bar{W}_L}{4\bar{R}} \left\{ \frac{1}{\sqrt{1 + [(\bar{W}_L/2\bar{R}) \sec \phi - \tan \phi]^2}} + \frac{1}{\sqrt{1 + [(\bar{W}_L/2\bar{R}) \sec \phi + \tan \phi]^2}} \right\} \quad (11)$$

Flux Distributions in Planes Beyond Exit

Flux variations in planes beyond the exit are also divided into four regions as noted in sketch (c) and figure 1(d).



In region I, flux is due to contributions from all of the inlet and from both walls. In region II, flux is from all of one wall and from part of the inlet. In region III, there is no direct flux from the inlet, and only flux from all or part of the one wall is "seen" by the point 5. In region IV, there is direct flux from part of the inlet only; there is no direct flux from either wall. Region IV occurs only for the convergent cases in planes

that are beyond the point of intersection of the extension of the planes of the walls. The flux equations that apply for the various regions are given next; derivations are given in appendix B.

Region I. - The boundary of region I is determined by the relation

$$0 \leq \bar{y}_5 \leq \frac{\bar{W}_L}{2} + (\bar{x}_5 - \bar{L}) \tan \beta \quad (12)$$

The flux at point 5 is given by the following expression:

$$\frac{n_5(\bar{y}_5)}{n_1} = \frac{1}{2} \left[\frac{1 - 2\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 - 2\bar{y}_5)^2}} + \frac{1 + 2\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right]$$

$$+ 2 \int_0^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} (\bar{x}_5 - \bar{x}_3) \left\{ \frac{1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right. \\ \left. + \frac{1 - 2\bar{y}_5 + 2\bar{x}_5 \tan \beta}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 - 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \quad (13)$$

The first term of equation (13) represents flux direct from the opening; the integral represents flux from the walls.

Region II. - Region II is bounded by the relation

$$\frac{\bar{W}_L}{2} + (\bar{x}_5 - \bar{L}) \tan \beta \leq \bar{y}_5 \leq \frac{\bar{W}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{2} \left(\frac{\bar{W}_L + 1}{\bar{L}} \right) \quad (14)$$

The flux at point 5 is given by the relation

$$\left(\frac{n_5}{n_1} \right)_{in} = \frac{1}{2} \left[\frac{\bar{y}_1 - \bar{y}_5}{\sqrt{\bar{x}_5^2 + (\bar{y}_1 - \bar{y}_5)^2}} + \frac{1 + 2\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right] \\ + 2 \int_0^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} (\bar{x}_5 - \bar{x}_3) \left\{ \frac{1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \quad (15)$$

Region III. - Region III is determined by the relation

$$\bar{y}_5 \geq \frac{\bar{W}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{2} \left(\frac{\bar{W}_L + 1}{\bar{L}} \right) \quad (16)$$

The flux at point 5 is given by

$$\frac{n_5(\bar{y}_5)}{n_1} = 2 \int_{\bar{x}'_3}^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} (\bar{x}_5 - \bar{x}_3) \left\{ \frac{1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \quad (17)$$

where the limit \bar{x}'_3 is given by

$$\bar{x}'_3 = \frac{1}{1 + \left[\frac{\bar{x}_5 - \bar{L}}{\bar{y}_5 - (\bar{W}_L/2)} \right] \tan \beta} \left\{ \bar{L} - \left[\frac{\bar{x}_5 - \bar{L}}{\bar{y}_5 - (\bar{W}_L/2)} \right] \left[\frac{\bar{W}_L + 1}{2} \right] \right\} \quad (18)$$

Since there is no direct flux contribution from the inlet, equation (17) represents only flux from the one wall.

Region IV. - Region IV occurs for the convergent case when the location of the plane \bar{x}_5 is beyond the point of intersection of the extension of the side walls; that is, for

$$\bar{x}_5 > \frac{1}{2|\tan \beta|} \quad (19)$$

where $|\tan \beta|$ is the absolute value of the tangent of β , the half-angle of convergence. In plane \bar{x}_5 then, the limit for region IV is

$$0 \leq \bar{y}_5 \leq \bar{x}_5 |\tan \beta| - \frac{1}{2} \quad (20)$$

The flux at point 5 in region IV is given by

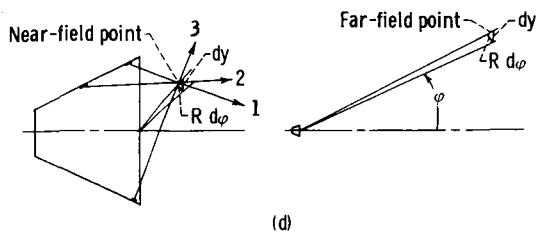
$$\frac{n_5(\bar{y}_5)}{n_1} = \frac{1}{2} \left[\frac{\bar{W}_L - 2\bar{y}_5}{\sqrt{4(\bar{x}_5 - \bar{L})^2 + (\bar{W}_L - 2\bar{y}_5)^2}} + \frac{\bar{W}_L + 2\bar{y}_5}{\sqrt{4(\bar{x}_5 - \bar{L})^2 + (\bar{W}_L + 2\bar{y}_5)^2}} \right] \quad (21)$$

The foregoing series of equations for the radial and plane flux values were programmed for solution on an IBM 7094 computer. Values of the wall flux $n(\bar{x}_3)/n_1$ required for the numerical integrations were obtained from reference 10.

Relation Between Radial and Plane Flux

Since the total particle flux through a small area is the summation of contributions from the various inlet and wall areas, it can be seen from

sketch (d) that, near the slot exit (i.e., in the near field), there is no simple relation between the total flux through two differential areas located at the same point (x_5, y_5) but at some angle to each other. For instance, particle trajectories labeled 1 and 2 in sketch (d) pass through the differential area dy but not through the differential area $R d\phi$. On the other hand, particle trajectory 3 passes through area $R d\phi$ but not through dy . Thus, the near-field flux through $R d\phi$ and dy are not simply related. Far from the slot exit (i.e., in the far field), however, particle trajectories that pass through area $R d\phi$ also pass through dy . Since the area dy is related to the area $R d\phi$ by



(d)

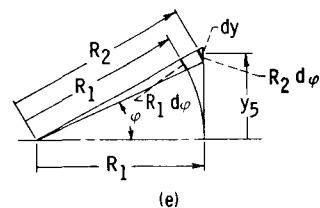
$R d\phi$ and dy are not simply related. Far from the slot exit (i.e., in the far field), however, particle trajectories that pass through area $R d\phi$ also pass through dy . Since the area dy is related to the area $R d\phi$ by

$$R d\phi = dy \cos \varphi \quad (22)$$

the radial flux in the far field is simply related to the plane flux at the same point. The relation is

$$n(y) = n(\varphi) \cos \varphi \quad (23)$$

Another far-field relation may be developed from the geometric quantities shown in sketch (e). From the sketch it can be seen that $R_1/R_2 = \cos \varphi$ and $dy \cos \varphi = R_2 d\phi$, so that $R_1 d\phi = \cos^2 \varphi dy$. Thus, the flux through a point on the plane $x - L$ is related to the radial flux at the same angle, for $R_1 = x - L$, by the equation



(e)

$$[n(y_5)]_{x-L} = [n(\varphi)]_{R_1=x-L} \cos^2 \varphi \quad (24)$$

Centerplane Flux Parameter

A parameter that is useful in indicating the approach of the centerplane flux (i.e., at $\varphi = y_5 = 0$) to its far-field value is the product $\bar{R}[n_5(0)/n_1]$. The asymptotic value of $n_5(0)/n_1$, obtained from equation (3), or (13), as x_5 becomes large is (for region I)

$$\left[\frac{n_5(0)}{n_1} \right]_{\bar{x}_5 \gg \bar{L}} = \frac{1}{2\bar{R}} \left[1 + 2\bar{L} \tan \beta \frac{\hat{n}(\bar{x}_3)}{n_1} \right] \quad (25)$$

where $\hat{n}(\bar{x}_3)/n_1$ is the average wall flux; that is,

$$\frac{\hat{n}(\bar{x}_3)}{n_1} = \frac{1}{\bar{L}} \int_0^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} d\bar{x}_3 \quad (26)$$

For divergent or parallel-walled slots, equation (25) becomes

$$\bar{R} \left[\frac{n_5(0)}{n_1} \right]_{x_5 \gg \bar{L}} = \frac{1}{2} \left[1 + 2\bar{L} \tan \beta \frac{\hat{n}(\bar{x}_3)}{n_1} \right] \quad (27)$$

For the convergent slot, where the centerplane in the far field is located in region IV, the asymptotic value of $n_5(0)/n_1$ becomes (refer to eq. (11) or (21))

$$\left[\frac{n_5(0)}{n_1} \right]_{x_5 \gg \bar{L}} = \frac{1}{2} \frac{\bar{W}_L}{\bar{R}} \quad (28)$$

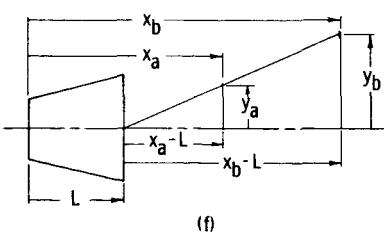
or

$$\bar{R} \left[\frac{n_5(0)}{n_1} \right]_{x_5 \gg \bar{L}} = \frac{\bar{W}_L}{2} \quad (29)$$

RESULTS AND DISCUSSION

The calculated angular distributions of particle flux at various radial distances from the slot exit are presented in table I. Values of flux on the centerplane ($\phi = 0$) are given in terms of the ratio to the inlet flux $[n(0)/n_1]$, while values at angles ϕ other than zero are normalized to the value on the centerplane at the same radius $n(\phi)/n(0)$.

The calculated distributions of particle flux at various distances from the centerplane, in planes located at several distances downstream from the slot exit, are presented in table II. As in table I, values of flux on the centerplane ($y = 0$) are given in terms of inlet flux $n(0)/n_1$, while values at distances y other than zero, are normalized to the value on the centerplane in the same plane $n(y)/n(0)$. It will be noted that the y -coordinate listing in the table is given as the ratio $y/(x - L)$. This parameter was chosen because a particular value of $y/(x - L)$ corresponds to the same angle from the centerplane regardless of the location of the plane downstream from the slot exit (see sketch (f)). In the far field, the normalized flux $n(y)/n(0)$ at a particular value of $y/(x - L)$ is independent of downstream distance.



Flux Distribution Along Centerplane

Values of the flux along the centerplane $n(0)/n_1$ obtained from either table I or II are shown for the various configurations in figures 2 to 4. In figure 2, values are shown for parallel-walled slots ($\beta = 0$) of various length to inlet width ratios, L/W_1 . Near the exit, the flux is highest for the lower values of L/W_1 . As the distance from the slot exit increases, the flux becomes less dependent on L/W_1 and approaches the theoretical value $\left[\frac{n(0)}{n_1} = \frac{1}{2R} \right]$ obtained for a slit source at large distances from the source.

The variation of flux with distance from the slot exit for $L/W_1 = 4$ is shown for various wall half-angles in figure 3. Close to the slot exit the flux is higher for the less divergent wall half-angles, β . Also, it is apparent that the flux from various slots does not approach the same limit in the far field. The lower line of figure 3 shows the direct flux contribution from the slot inlet, that is, the flux that has arrived at the centerplane without having had a collision with the slot wall. The 75° divergent slot has centerplane flux values nearly equal to those obtainable from the inlet directly, indicating that the contribution from the walls is very small for wall half-angles of this magnitude or greater. It is also apparent from figure 3 that at any particular distance from the exit of a slot there is a particular wall half-angle that will give a maximum value of the flux $n(0)/n_1$. This feature is shown more clearly in figure 4, wherein centerplane flux is plotted as a function of wall half-angle for various distances from the slot exit for all the length to width ratios examined. The wall half-angle that yields the maximum flux increases (i.e., is more divergent) as the distance from the slot exit increases; however, the maximum is not very pronounced at large wall half-angles.

Shown in figure 5 are some typical variations of the product $\bar{R}[n(0)/n_1]$ with distance downstream. The value of $\bar{R}[n(0)/n_1]$ approaches its far-field limit more rapidly for smaller values of L/W_1 (fig. 5(a)) and for the less divergent slots (fig. 5(b)).

The far-field limiting values of the flux parameter $\bar{R}[n(0)/n_1]$ may be calculated from equations (27) and (29). Values of the average wall flux $\hat{n}(x_3)/n_1$, required in equation (27), were calculated from the wall flux distributions in reference 10 and are shown in figure 6.

The resulting far-field limiting values of $\bar{R}[n(0)/n_1]$ are shown in figure 7 as functions of L/W_1 and β . The maximum value at any particular radius \bar{R} is obtained with divergent slots.

Far-Field Flux Distributions

Some typical variations in the far-field flux patterns of the different slot configurations are shown in figures 8 to 10. In figure 8, results are shown for parallel-walled slots of various length to width ratios. A beam-

collimation effect resulting from increasing L/W_1 is apparent.

The far-field radial flux patterns for 20° divergent and 20° convergent slots are shown in figures 9(a) and (b), respectively, for various length to width ratios. The discontinuities in slope of these curves occur at the boundaries at the three different flux regions. The normalized flux follows the cosine distribution law out to the angle $\phi = |\beta|$. Beyond this angle, the flux drops below the cosine pattern. Again, the longer the slot, the more collimated is the resulting beam. The divergent slot results in a more collimated beam than the convergent slot.

The far-field flux patterns for a particular length to width ratio ($L/W_1 = 1$), and various angles of divergence and convergence are shown in figures 10(a) and (b). Again, the flux pattern follows the cosine distribution law out to the angle $\phi = |\beta|$ and drops below the cosine pattern more rapidly for the divergent than for the convergent configurations.

The representative plots thus far presented have been radial flux patterns. As shown in equation (23), the radial and plane flux values at a point are simply related to each other in the far field. Similarly, values of $n(\bar{y})$ and $n(\phi)$ for $\bar{x} - \bar{L} = \bar{R}$ are simply related as shown by equation (24). Compared in figure 11 are far-field values of the flux $n(\phi)/n(0)$ obtained by direct calculation (table I) and as determined from equation (24). The excellent agreement shows that the tabulated values were made out to large enough distances to be in the far field at all angles from the slot centerplane.

Near-Field Flux Distributions

Some illustrative flux distribution patterns in the near field are shown in figures 12 to 14. Radial flux patterns for the parallel-walled slot of length to inlet width ratio of 8 are shown in figure 12. An abrupt change in the slope of the flux curve is apparent at the boundary between regions I and II. The small maximum in radial flux curve at $\phi > 0$ for a small \bar{R} was unexpected, but its existence is verified by differentiation of equation (3) for the case of $\beta = 0$. This yields the relation

$$\left[\frac{d\left(\frac{n_5(\phi)}{n_1}\right)}{d\phi} \right]_{\phi=0} = \int_0^{\bar{L}} \frac{n(\bar{x}_3)}{n_1} \frac{2}{\left[4(\bar{L} + \bar{R} - \bar{x}_3)^2 + 1 \right]^{3/2}} d\bar{x}_3$$

which shows that the slope is small but positive at $\phi = 0$ and approaches zero as the radius increases. The flux in planes at varying distance from the slot exit for this same configuration are shown in figure 12(b). This figure shows clearly the large variation in flux distribution as distance downstream from the exit is varied.

Near-field flux patterns for a convergent slot of $L/W_1 = 1$ and $\beta = -20^\circ$

are shown in figures 14(a) and (b). The behavior of the patterns for this convergent case differs from that for the divergent slot shown in figure 13. Within the angle $\phi \leq |\beta|$, the normalized flux (fig. 14(a)) drops below its final far-field value and then rises, while for the divergent slot (fig. 13(a)) the relative flux continuously approaches the far-field value. Comparison of figures 13(b) and 14(b) also shows that, for a range of $y/(x - L)$ values, the flux distributions are much more widely spread for the divergent slot than for the convergent slot.

Other Considerations

The directivity of the molecular beams emerging from slots of different L/W_1 ratios is illustrated in figure 15, which shows the far-field flux patterns for divergent slots with $\beta = 20^\circ$ and varying L/W_1 values. The curves are different from those of figure 9(a) in that the flux from the zero-length slot is used as the reference for all the relative flux values, so that a true comparison of the relative flux is obtained when the inlet flux density is the same.

A similar comparison for slots of $L/W_1 = 4$ and varying wall half-angles is shown in figure 16. The highest flux in the central portion of the beam is obtained with a wall half-angle of about 20° . However, the 10° and 30° wall half-angles are only slightly below this maximum flux level. The trend for other L/W_1 slots would be similar, with the maximum flux occurring at slightly different wall half-angles as illustrated in figure 7.

CONCLUDING REMARKS

Equations for the determination of particle flux at a location downstream from the exit of convergent and divergent two-dimensional slots under free-molecule conditions have been derived and solved numerically. Slot configurations include length to inlet width ratios from 0.25 to 8 and wall half-angles from 75° divergent to 60° convergent. Flux distribution patterns at various distances from the slot exit are presented. Patterns are calculated in two ways: (1) variation with angle at constant radius, and (2) variation with distance from the centerplane in a plane normal to the flow direction.

From typical illustrative plots of the calculations, the following features of the particle flux were evident:

(1) Values of flux along the centerplane for the parallel-walled slots are highest for small length-to-width-ratio slots initially and become less a function of the length to inlet width ratio as the distance from the slot increases.

(2) There is a particular wall half-angle that yields a maximum in the centerplane flux at a given distance from the slot exit. This angle becomes more divergent as the distance from the slot increases; however, the flux is not sensitive to wall half-angle variations at the larger distances.

(3) Far-field limiting values of the function $\bar{R}[n(0)/n_1]$ are approached in shorter distances the smaller the length to inlet width ratio of the slot and the more convergent the slot.

(4) The beam is more collimated the larger the length to inlet width ratio of the slot.

(5) A divergent slot yields a more collimated beam than a convergent slot of the same length to inlet width ratio and the same wall half-angle.

(6) Far-field distribution patterns of both convergent and divergent slots follow the cosine distribution law out to angles equal to the wall half-angle and then drop below the cosine law pattern.

Lewis Research Center
National Aeronautics and Space Administration
Cleveland, Ohio, June 12, 1964

APPENDIX A

SYMBOLS

A	area
L	length of configuration
l	length of line
n	flux or arrival rate, number/(area)(time)
$\hat{n}(\bar{x}_3)/n_l$	average wall flux
R	radial distance
w_l	inlet width of slot
w_L	exit width of slot
x	axial distance from slot inlet
y	lateral distance from slot centerplane
y'_l	upper limit lateral distance from slot centerplane in plane of opening (see sketch (i))
y''_l	lower limit lateral distance from slot centerplane in plane of opening (see sketch (i))
β	half-angle of slot; positive for diverging and negative for converging slot
θ	angle between surface normal and line
ϕ	angle between R and slot centerplane

Subscripts:

a,b	general points
in	inlet
w	wall
l	inlet plane
2,3	wall
4	exit plane

5 beyond exit plane

Superscript:

($\bar{}$) nondimensionalized quantity, divided by W_1 , the inlet slot width

APPENDIX B

DERIVATION OF FLUX RELATIONS

The equation from which all flux relations herein are derived is the differential line-element source relation:

$$dn_b = \frac{n_a \cos \theta_{ab} \cos \theta_{ba}}{2l_{ab}} dy_a \quad (B1)$$

As illustrated in sketches (c) and (d) there are four possible regions in which a point, at which the flux is to be determined, may lie. The flux equation is different for each region and for different orientations of the flux area.

Radial Flux Relations

I. Refer to figure 1(c). Point 5 is in region I, which is bounded by

$$0 \leq \bar{y}_5 \leq \frac{\bar{w}_L}{2} + (\bar{x}_5 - \bar{L}) \tan \beta \quad (B2)$$

A. Inlet.

$$\frac{n_5}{n_1} = \int_{-W/2}^{W/2} \frac{\cos \theta_{15} \cos \theta_{51}}{2l_{15}} dy_1 \quad (B3)$$

Substituting the following geometric relations

$$l_{15}^2 = x_5^2 + (y_5 - y_1)^2$$

$$\cos \theta_{15} = \frac{x_5}{l_{15}}$$

$$\cos \theta_{51} = \cos (\phi - \theta_{15}) = \frac{x_5}{l_{15}} \left(\frac{x_5 - L}{R} \right) + \frac{y_5}{R} \left(\frac{y_5 - y_1}{l_{15}} \right)$$

into equation (B3) yields

$$\left(\frac{n_5}{n_1}\right)_{in} = \int_{-W_1/2}^{W_1/2} \frac{x_5[x_5(x_5 - L) + y_5(y_5 - y_1)]}{2R[x_5^2 + (y_5 - y_1)^2]^{3/2}} \quad (B4)$$

Integrating equation (B4) and nondimensionalizing yields

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2R} \left[\frac{(\bar{x}_5 - \bar{L})(1 - 2\bar{y}_5) + 2\bar{x}_5\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 - 2\bar{y}_5)^2}} + \frac{(\bar{x}_5 - \bar{L})(1 + 2\bar{y}_5) - 2\bar{x}_5\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right] \quad (B5)$$

All barred quantities are nondimensional variables made dimensionless by referring them to the inlet width W_1 .

B. Wall. The flux at point 5 from one wall is

$$\left(\frac{n_5}{n_1}\right)_w = \int_0^L \frac{n_3(x_3)}{n_1} \frac{\cos \theta_{35} \cos \theta_{53}}{2l_{35}} \sec \beta \, dx_3 \quad (B6)$$

Substituting the following geometric relations

$$\cos \theta_{35} = \frac{y_5 - y_3}{l_{35}} \cos \beta + \frac{x_5 - x_3}{l_{35}} \sin \beta$$

$$\cos \theta_{53} = \frac{y_5 - y_3}{l_{35}} \sin \varphi + \frac{x_5 - x_3}{l_{35}} \cos \varphi$$

$$l_{35}^2 = (x_5 - x_3)^2 + (y_5 - y_3)^2$$

into equation (B6) yields

$$\left(\frac{n_5}{n_1}\right)_w = \int_0^L \frac{n_3(x_3)}{n_1} \frac{[y_5 - y_3 + (x_5 - x_3) \tan \beta][(y_5 - y_3) \sin \varphi + (x_5 - x_3) \cos \varphi]}{2[(x_5 - x_3)^2 + (y_5 - y_3)^2]^{3/2}} \, dx_3 \quad (B7)$$

Noting that $y_3 = -(W_1/2) - x_3 \tan \beta$ and nondimensionalizing the resulting equation yields the wall contribution to the flux:

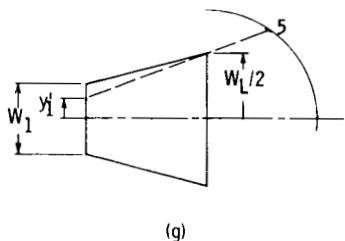
$$\left(\frac{n_5}{n_1}\right)_w = \int_0^{\bar{L}} \frac{n_3(\bar{x}_3)}{n_1} \times \left\{ \frac{(1+2\bar{y}_5 + 2\bar{x}_5 \tan \beta) [(1+2\bar{y}_5 + 2\bar{x}_3 \tan \beta) \sin \varphi + 2(\bar{x}_5 - \bar{x}_3) \cos \varphi]}{\left[4(\bar{x}_5 - \bar{x}_3)^2 + (1+2\bar{y}_5 + 2\bar{x}_3 \tan \beta)^2\right]^{3/2}} \right\} d\bar{x}_3 \quad (B8)$$

This is the contribution from one wall only. The contribution from the other wall to the flux at point 5 is obtained by making the substitution $y_5 = -y_5$ into equation (B8).

II. Point 5 is in region II, which is bounded by

$$\frac{\bar{W}_L}{2} + (\bar{x}_5 - \bar{L}) \tan \beta \leq \bar{y}_5 \leq \frac{\bar{W}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{\bar{L}} \left(\frac{\bar{W}_L + 1}{\bar{L}} \right) \quad (B9)$$

A. Inlet. The flux at point 5 from the inlet is similar to equation (B4) with a different upper limit y'_1 , as may be noted in sketch (g).



Integration of equation (B4) with the upper limit of y'_1 yields

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2R} \left\{ \frac{(\bar{x}_5 - \bar{L})(y'_1 - \bar{y}_5) + \bar{x}_5 \bar{y}_5}{\sqrt{\bar{x}_5^2 + (y'_1 - \bar{y}_5)^2}} + \frac{(\bar{x}_5 - \bar{L})[(W_L/2) + \bar{y}_5] - \bar{x}_5 \bar{y}_5}{\sqrt{\bar{x}_5^2 + [(W_L/2) + \bar{y}_5]^2}} \right\} \quad (B10)$$

Expressed in nondimensional form, the contribution from the inlet is

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2R} \left[\frac{(\bar{x}_5 - \bar{L})(\bar{y}'_1 - \bar{y}_5) + \bar{x}_5 \bar{y}_5}{\sqrt{\bar{x}_5^2 + (\bar{y}'_1 - \bar{y}_5)^2}} + \frac{(\bar{x}_5 - \bar{L})(1+2\bar{y}_5) - 2\bar{x}_5 \bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1+2\bar{y}_5)^2}} \right] \quad (B11)$$

where

$$\bar{y}'_1 = \frac{\bar{W}_L}{2} - \bar{L} \left[\frac{\bar{y}_5 - (\bar{W}_L/2)}{\bar{x}_5 - \bar{L}} \right] \quad (B12)$$

B. Wall. The flux at point 5 comes from one wall only and is given by equation (B8).

III. Point 5 is in region III, which is bounded by the relation

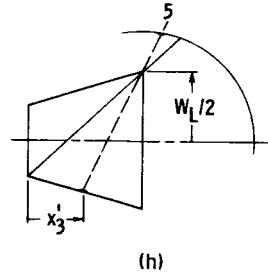
$$\bar{R} \geq \bar{y}_5 \geq \frac{\bar{w}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{2} \left(\frac{\bar{w}_L + 1}{\bar{L}} \right) \quad (\text{B13})$$

A. Inlet. There is no contribution from the inlet.

B. Wall. The flux from the wall is similar to equation (B8) with a different lower limit \bar{x}_3' , as may be noted in sketch (h). Thus, the contribution to the flux at point 5 from the wall is

$$\begin{aligned} \left(\frac{n_5}{n_1} \right)_w &= \int_{\bar{x}_3'}^{\bar{L}} \frac{n_3(\bar{x}_3)}{n_1} \\ &\times \left\{ \frac{(1+2\bar{y}_5+2\bar{x}_5 \tan \beta)[(1+2\bar{y}_5+2\bar{x}_3 \tan \beta) \sin \varphi + 2(\bar{x}_5 - \bar{x}_3) \cos \varphi]}{[4(\bar{x}_5 - \bar{x}_3)^2 + (1+2\bar{y}_5+2\bar{x}_3 \tan \beta)^2]^{3/2}} \right\} d\bar{x}_3 \end{aligned} \quad (\text{B14})$$

where



$$\begin{aligned} \bar{x}_3' &= \frac{1}{1 + \left[\frac{\bar{x}_5 - \bar{L}}{\bar{y}_5 - (\bar{w}_L/2)} \right] \tan \beta} \\ &\times \left\{ \bar{L} - \left[\frac{\bar{x}_5 - \bar{L}}{\bar{y}_5 - (\bar{w}_L/2)} \right] \left[\frac{\bar{w}_L + 1}{2} \right] \right\} \end{aligned} \quad (\text{B15})$$

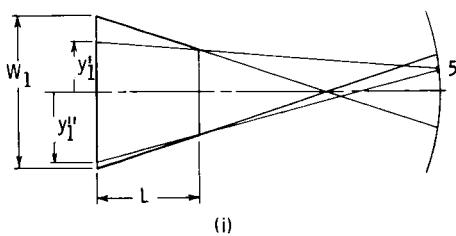
IV. Point 5 is in region IV, which is defined by the conditions

$$\bar{x}_5 \geq \frac{1}{2|\tan \beta|} \quad (\text{B16})$$

and

$$0 \leq \tan \Phi \leq |\tan \beta| - \frac{\bar{w}_L \sec \Phi}{2\bar{R}} \quad (\text{B17})$$

A. Inlet. The flux at point 5 from the inlet will be similar to equation (B4) with different upper and lower limits, as may be noted in sketch (i), where



$$y_1' = \frac{w_L}{2} - \left[\frac{y_5 - (w_L/2)}{x_5 - L} \right] L$$

$$y_1'' = \left[\frac{y_5 + (w_L/2)}{x_5 - L} \right] L - \frac{w_L}{2}$$

Integration of equation (B4) with lower limit y_1'' and upper limit y_1' yields

$$\left(\frac{n_5}{n_1} \right)_{in} = \frac{\bar{w}_L}{4\bar{R}} \left\{ \frac{1}{\sqrt{1 + [(\bar{w}_L/2\bar{R}) \sec \varphi - \tan \varphi]^2}} + \frac{1}{\sqrt{1 + [(\bar{w}_L/2\bar{R}) \sec \varphi + \tan \varphi]^2}} \right\} \quad (B18)$$

B. Wall. There is no flux from the walls to region IV.

Flux Relations for Planes

I. Refer to figure 1(d). Point 5 is in region I. The bound for region I is given by equation (B2).

A. Inlet. The flux is given directly (ref. 9):

$$\left(\frac{n_5}{n_1} \right)_{in} = \frac{1}{2} \left[\frac{1 - 2\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 - 2\bar{y}_5)^2}} + \frac{1 + 2\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right] \quad (B19)$$

B. Wall. The contribution to the flux at point 5 from one wall is

$$\left(\frac{n_5}{n_1} \right)_w = \int_0^L \frac{n_3(\bar{x}_3)}{n_1} \frac{\cos \theta_{35} \cos \theta_{53}}{2l_{35}} \sec \beta \, dx_3 \quad (B20)$$

Substituting the following geometric relations

$$\cos \theta_{35} = \frac{y_5 - y_3}{l_{35}} \cos \beta + \frac{x_5 - x_3}{l_{35}} \sin \beta$$

$$\cos \theta_{53} = \frac{x_5 - x_3}{l_{35}}$$

$$l_{35}^2 = (x_5 - x_3)^2 + (y_5 - y_3)^2$$

into equation (B20) yields

$$\left(\frac{n_5}{n_1}\right)_w = \frac{1}{2} \int_0^L \frac{n_3(x_3)}{n_1} \frac{(x_5 - x_3)[y_5 - y_3 + (x_5 - x_3) \tan \beta]}{\left[(x_5 - x_3)^2 + (y_5 - y_3)^2\right]^{3/2}} dx_3 \quad (B21)$$

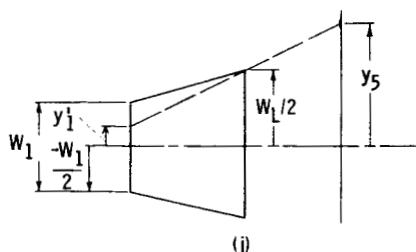
Noting that $y_3 = -[(W_1/2) + x_3 \tan \beta]$ and nondimensionalizing the resulting equation yields the wall contribution to the flux:

$$\left(\frac{n_5}{n_1}\right)_w = 2 \int_0^{\bar{L}} \frac{n_3(\bar{x}_3)}{n_1} \frac{(\bar{x}_5 - \bar{x}_3)(1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta)}{\left[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta)^2\right]^{3/2}} d\bar{x}_3 \quad (B22)$$

The flux contribution from the other wall is obtained by substituting the relation $\bar{y}_5 = -\bar{y}_3$ into equation (B22).

II. Point 5 is in region II. The bounds for region II are given by the relation (B9).

A. Inlet. The flux at point 5 from the opening is (see sketch (j))



$$\left(\frac{n_5}{n_1}\right)_{in} = \int_{-W_1/2}^{y'_1} \frac{\cos \theta_{15} \cos \theta_{51}}{2l_{15}} dy_1 \quad (B23)$$

The integration is identical to that employed in obtaining equation (B19) except for the different upper limit. Integration of equation (B23) yields

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2} \left\{ \frac{y'_1 - y_5}{\sqrt{x_5^2 + (y'_1 - y_5)^2}} + \frac{(W_1/2) + y_5}{\sqrt{x^2 + [(W_1/2) + y_5]^2}} \right\} \quad (B24)$$

Putting equation (B24) into nondimensional form, related to W_L , yields

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2} \left[\frac{\bar{y}_1' - \bar{y}_5}{\sqrt{\bar{x}_5^2 + (\bar{y}_1' - \bar{y}_5)^2}} + \frac{1 + 2\bar{y}_5}{\sqrt{4\bar{x}_5^2 + (1 + 2\bar{y}_5)^2}} \right] \quad (B25)$$

where

$$\bar{y}_1' = \frac{\bar{W}_L}{2} - \frac{\bar{L}}{2} \left[\frac{\bar{y}_5 - (\bar{W}_L/2)}{\bar{x}_5 - \bar{L}} \right] \quad (B26)$$

B. Wall. Only one wall contributes flux to point 5 in region II. The flux is given by equation (B22).

III. Point 5 is in region III. The bound for region III is

$$\bar{y}_5 \geq \frac{\bar{W}_L}{2} + \frac{\bar{x}_5 - \bar{L}}{2} \left(\frac{\bar{W}_L + 1}{\bar{L}} \right) \quad (B27)$$

A. Inlet. There is no contribution to flux from the inlet.

B. Wall. The wall contribution to the flux is similar to equation (B22) with a different lower limit \bar{x}_3' , similar to the situation illustrated in sketch (f). The relation is

$$\begin{aligned} \left(\frac{n_5}{n_1}\right)_w &= 2 \int_{\bar{x}_3'}^{\bar{L}} \frac{n_3(\bar{x}_3)}{n_1} (\bar{x}_5 - \bar{x}_3) \\ &\times \left\{ \frac{1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta}{\left[4(\bar{x}_5 - \bar{x}_3)^2 + (1 + 2\bar{y}_5 + 2\bar{x}_5 \tan \beta)^2 \right]^{3/2}} \right\} d\bar{x}_3 \end{aligned} \quad (B28)$$

where \bar{x}_3' is given by equation (B15).

IV. Point 5 is in region IV. The bounds for region IV are given by the relation (B16) and

$$0 \leq \bar{y}_5 \leq \bar{x}_5 |\tan \beta| - \frac{1}{2} \quad (B29)$$

A. Inlet. The flux at point 5 from the inlet (see sketch (i)) is

$$\left(\frac{n_5}{n_1}\right)_{in} = \int_{-y_1''}^{y_1'} \frac{\cos \theta_{15} \cos \theta_{51}}{2l_{15}} dy_1 \quad (B30)$$

Integration of equation (B30) is identical to that for obtaining equation (B24) except for the different limits. Integration of equation (B30) yields

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2} \left[\frac{y_1' - y_5}{\sqrt{x_5^2 + (y_1' - y_5)^2}} + \frac{y_1'' + y_5}{\sqrt{x_5^2 + (y_1'' + y_5)^2}} \right] \quad (B31)$$

The geometric relations

$$\frac{y_5 - L}{(W_L/2) - y_5} = \frac{x_5}{y_1 - y_5} \quad (B32)$$

$$\frac{x_5 - L}{(W_L/2) + y_5} = \frac{x_5}{y_1'' + y_5} \quad (B33)$$

can be used to rewrite equation (B31) in nondimensional form:

$$\left(\frac{n_5}{n_1}\right)_{in} = \frac{1}{2} \left[\frac{\bar{W}_L - 2\bar{y}_5}{\sqrt{4(\bar{x}_5 - \bar{L})^2 + (\bar{W}_L - 2\bar{y}_5)^2}} + \frac{\bar{W}_L + 2\bar{y}_5}{\sqrt{4(\bar{x}_5 - \bar{L})^2 + (\bar{W}_L + 2\bar{y}_5)^2}} \right] \quad (B34)$$

Comparison of equations (B34) and (B19) indicates that equation (B34) is identical in form to the expression for flux that would arrive at point 5 from the exit alone as the source having the same emission rate as the inlet.

B. Wall. There is no wall contribution to the flux at point 5 in region IV.

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(b-5) Wall half-angle, 30°

0.25	0.63830	0.999	0.998	0.994	0.990	0.985	0.978	0.961	0.940	0.906	0.867	0.821	0.769	0.650	0.511	0.213	0.008	0.002
1.50	0.52778	0.998	0.994	0.994	0.994	0.988	0.951	0.916	0.872	0.812	0.804	0.766	0.600	0.495	0.401	0.202	0.089	0.015
1.00	0.37641	0.998	0.994	0.994	0.978	0.951	0.919	0.863	0.811	0.709	0.592	0.460	0.326	0.212	0.138	0.059	0.024	0.001
2.00	0.22998	0.999	0.993	0.919	0.955	0.922	0.881	0.756	0.728	0.589	0.459	0.295	0.188	0.120	0.077	0.031	0.011	0.005
4.00	0.12700	0.988	0.987	0.987	0.987	0.986	0.889	0.811	0.756	0.725	0.368	0.222	0.146	0.092	0.058	0.022	0.010	0.001
8.00	0.05663	0.980	0.980	0.980	0.980	0.980	0.884	0.816	0.736	0.654	0.479	0.331	0.207	0.129	0.081	0.050	0.024	0.001
16.00	0.03410	0.980	0.980	0.980	0.980	0.980	0.884	0.808	0.725	0.642	0.55	0.415	0.196	0.121	0.076	0.047	0.017	0.001
32.00	0.01725	0.985	0.985	0.985	0.985	0.985	0.881	0.804	0.720	0.644	0.536	0.448	0.308	0.190	0.118	0.073	0.049	0.001
64.00	0.00867	0.985	0.985	0.985	0.985	0.985	0.880	0.802	0.718	0.632	0.443	0.304	0.188	0.116	0.065	0.045	0.017	0.001
128.00	0.00435	0.985	0.985	0.985	0.985	0.985	0.879	0.801	0.717	0.629	0.441	0.302	0.187	0.115	0.072	0.044	0.016	0.001
256.00	0.00218	0.985	0.985	0.985	0.985	0.985	0.879	0.801	0.716	0.627	0.440	0.301	0.186	0.115	0.071	0.044	0.016	0.001
512.00	0.00109	0.985	0.985	0.985	0.985	0.985	0.879	0.801	0.716	0.627	0.439	0.301	0.186	0.115	0.071	0.044	0.016	0.001

(b-6) Wall half-angle, 45°

0.25	0.60090	0.999	0.997	0.994	0.989	0.983	0.976	0.957	0.934	0.898	0.856	0.809	0.758	0.649	0.539	0.330	0.040	0.002
0.50	0.44543	0.998	0.992	0.981	0.967	0.949	0.922	0.881	0.814	0.723	0.628	0.534	0.444	0.297	0.199	0.041	0.002	0.001
1.00	0.33582	0.995	0.980	0.955	0.922	0.881	0.834	0.729	0.619	0.488	0.378	0.291	0.225	0.198	0.042	0.005	0.001	0.001
2.00	0.22112	0.991	0.965	0.923	0.810	0.807	0.740	0.604	0.479	0.353	0.260	0.167	0.104	0.045	0.01	0.003	0.001	0.000
4.00	0.12360	0.986	0.954	0.902	0.816	0.762	0.685	0.538	0.413	0.294	0.186	0.118	0.075	0.030	0.01	0.003	0.001	0.000
8.00	0.05526	0.987	0.949	0.890	0.818	0.738	0.657	0.506	0.382	0.253	0.159	0.100	0.063	0.025	0.008	0.003	0.001	0.000
16.00	0.02351	0.986	0.943	0.884	0.809	0.727	0.664	0.491	0.368	0.235	0.147	0.092	0.058	0.022	0.007	0.002	0.001	0.000
32.00	0.01698	0.986	0.944	0.882	0.805	0.721	0.637	0.493	0.361	0.227	0.141	0.088	0.055	0.021	0.006	0.002	0.001	0.000
64.00	0.00855	0.985	0.944	0.880	0.803	0.718	0.634	0.480	0.357	0.223	0.138	0.086	0.054	0.020	0.006	0.002	0.001	0.000
128.00	0.00429	0.985	0.943	0.879	0.801	0.717	0.632	0.478	0.355	0.221	0.137	0.086	0.054	0.020	0.006	0.002	0.001	0.000
256.00	0.00215	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.354	0.220	0.136	0.085	0.053	0.020	0.006	0.002	0.001	0.000
512.00	0.00107	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.354	0.219	0.136	0.085	0.053	0.020	0.006	0.002	0.001	0.000

(b-7) Wall half-angle, 60°

0.25	0.57469	0.999	0.997	0.993	0.988	0.982	0.974	0.953	0.928	0.889	0.844	0.794	0.739	0.627	0.517	0.338	0.128	0.023
0.50	0.46856	0.998	0.992	0.981	0.961	0.940	0.881	0.814	0.723	0.628	0.534	0.444	0.297	0.199	0.041	0.002	0.001	0.000
1.00	0.33584	0.995	0.980	0.955	0.922	0.882	0.837	0.735	0.629	0.503	0.394	0.260	0.238	0.147	0.095	0.022	0.001	0.000
2.00	0.21001	0.991	0.966	0.926	0.813	0.813	0.747	0.614	0.493	0.364	0.269	0.200	0.151	0.084	0.038	0.006	0.000	0.000
4.00	0.11832	0.988	0.955	0.904	0.839	0.766	0.690	0.543	0.419	0.300	0.216	0.157	0.111	0.053	0.023	0.006	0.000	0.000
8.00	0.06278	0.987	0.949	0.891	0.820	0.740	0.660	0.509	0.385	0.271	0.192	0.139	0.096	0.062	0.017	0.001	0.000	0.000
16.00	0.03233	0.986	0.946	0.885	0.810	0.728	0.645	0.592	0.462	0.340	0.257	0.181	0.130	0.086	0.035	0.014	0.001	0.000
32.00	0.01640	0.986	0.944	0.882	0.805	0.722	0.638	0.484	0.361	0.250	0.176	0.126	0.082	0.035	0.014	0.001	0.000	0.000
64.00	0.00826	0.985	0.943	0.880	0.802	0.711	0.632	0.480	0.357	0.247	0.174	0.122	0.079	0.034	0.014	0.001	0.000	0.000
128.00	0.00414	0.985	0.943	0.879	0.801	0.716	0.631	0.478	0.355	0.245	0.171	0.120	0.078	0.032	0.013	0.001	0.000	0.000
256.00	0.00208	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.355	0.245	0.170	0.119	0.077	0.031	0.012	0.001	0.000	0.000
512.00	0.00104	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.354	0.244	0.171	0.119	0.076	0.033	0.013	0.001	0.000	0.000

(b-8) Wall half-angle, 75°

0.25	0.55916	0.999	0.997	0.993	0.987	0.981	0.972	0.951	0.924	0.883	0.835	0.782	0.726	0.608	0.495	0.315	0.140	0.062
1.00	0.32105	0.995	0.979	0.954	0.920	0.879	0.832	0.729	0.623	0.499	0.394	0.309	0.243	0.152	0.099	0.047	0.015	0.000
2.00	0.20001	0.991	0.966	0.926	0.874	0.814	0.749	0.616	0.494	0.368	0.274	0.204	0.155	0.092	0.059	0.027	0.004	0.000
4.00	0.11292	0.989	0.956	0.905	0.840	0.768	0.692	0.547	0.422	0.303	0.218	0.160	0.119	0.070	0.044	0.020	0.004	0.000
8.00	0.06008	0.987	0.949	0.892	0.821	0.762	0.661	0.511	0.387	0.287	0.212	0.133	0.140	0.103	0.060	0.037	0.017	0.000
16.00	0.03099	0.986	0.946	0.885	0.811	0.729	0.646	0.493	0.370	0.258	0.182	0.131	0.096	0.055	0.034	0.014	0.000	0.000
32.00	0.01574	0.986	0.945	0.882	0.805	0.722	0.638	0.485	0.362	0.251	0.176	0.126	0.093	0.053	0.033	0.013	0.000	0.000
64.00	0.00793	0.985	0.944	0.880	0.803	0.719	0.634	0.480	0.358	0.247	0.173	0.124	0.091	0.052	0.032	0.013	0.000	0.000
128.00	0.00398	0.985	0.943	0.880	0.802	0.717	0.632	0.478	0.356	0.245	0.172	0.123	0.090	0.051	0.032	0.012	0.000	0.000
256.00	0.00199	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.355	0.245	0.171	0.122	0.090	0.051	0.032	0.012	0.000	0.000
512.00	0.00100	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.354	0.244	0.171	0.122	0.090	0.051	0.032	0.012	0.000	0.000

(d-5) Wall half-angle, 30°

0.25	0.31790	1.000	0.999	0.999	0.998	0.996	0.995	0.991	0.986	0.986	0.988	0.981	0.979	0.988	0.988	0.981
0.50	0.29646	0.999	0.998	0.998	0.996	0.996	0.995	0.992	0.988	0.988	0.986	0.980	0.976	0.982	0.982	0.980
1.00	0.24495	0.995	0.994	0.994	0.994	0.985	0.976	0.960	0.943	0.920	0.849	0.770	0.693	0.594	0.510	0.410
2.00	0.18195	0.996	0.996	0.993	0.962	0.933	0.898	0.858	0.765	0.665	0.546	0.376	0.167	0.063	0.026	0.011
4.00	0.11732	0.992	0.949	0.933	0.885	0.830	0.770	0.645	0.523	0.499	0.384	0.249	0.132	0.058	0.024	0.001
8.00	0.06860	0.989	0.959	0.911	0.850	0.782	0.710	0.559	0.309	0.113	0.058	0.036	0.012	0.007	0.003	0.001
16.00	0.03685	0.988	0.952	0.897	0.828	0.756	0.673	0.439	0.224	0.082	0.049	0.031	0.024	0.011	0.003	0.001
32.00	0.01926	0.986	0.948	0.884	0.808	0.735	0.653	0.385	0.187	0.075	0.045	0.029	0.020	0.010	0.006	0.001
64.00	0.00985	0.986	0.945	0.884	0.808	0.725	0.642	0.359	0.169	0.072	0.044	0.028	0.019	0.010	0.006	0.001
128.00	0.00498	0.986	0.944	0.881	0.804	0.720	0.630	0.347	0.160	0.070	0.043	0.028	0.019	0.010	0.006	0.001
256.00	0.00251	0.985	0.943	0.880	0.802	0.718	0.622	0.340	0.154	0.069	0.042	0.027	0.017	0.010	0.006	0.001
512.00	0.00126	0.985	0.943	0.879	0.801	0.717	0.620	0.337	0.157	0.069	0.042	0.027	0.017	0.010	0.006	0.001

(d-6) Wall half-angle, 45°

0.25	0.26696	1.000	0.999	0.999	0.998	0.996	0.995	0.991	0.985	0.977	0.967	0.956	0.943	0.913	0.879	0.800
0.50	0.24350	1.000	0.998	0.996	0.992	0.988	0.982	0.969	0.952	0.927	0.897	0.864	0.828	0.780	0.750	0.689
1.00	0.20854	0.999	0.994	0.987	0.977	0.964	0.949	0.913	0.868	0.805	0.736	0.665	0.592	0.455	0.339	0.025
2.00	0.15710	0.996	0.949	0.896	0.846	0.794	0.745	0.602	0.502	0.402	0.349	0.297	0.231	0.177	0.044	0.001
4.00	0.10466	0.993	0.973	0.941	0.895	0.847	0.792	0.673	0.558	0.432	0.332	0.219	0.159	0.072	0.015	0.001
8.00	0.06207	0.990	0.961	0.916	0.858	0.792	0.722	0.584	0.461	0.339	0.217	0.153	0.122	0.055	0.002	0.000
16.00	0.03409	0.988	0.944	0.899	0.832	0.757	0.680	0.532	0.409	0.246	0.169	0.093	0.028	0.017	0.002	0.000
32.00	0.01791	0.987	0.948	0.890	0.817	0.737	0.650	0.505	0.381	0.194	0.062	0.025	0.016	0.004	0.002	0.000
64.00	0.00919	0.986	0.946	0.884	0.809	0.727	0.664	0.491	0.368	0.170	0.049	0.022	0.015	0.007	0.001	0.000
128.00	0.00466	0.986	0.944	0.882	0.805	0.721	0.637	0.483	0.361	0.159	0.043	0.022	0.014	0.007	0.001	0.000
256.00	0.00234	0.985	0.944	0.880	0.803	0.718	0.634	0.480	0.357	0.153	0.040	0.022	0.014	0.007	0.001	0.000
512.00	0.00118	0.985	0.943	0.879	0.802	0.717	0.632	0.478	0.355	0.151	0.038	0.022	0.014	0.007	0.001	0.000

(d-7) Wall half-angle, 60°

0.25	0.23718	1.000	0.999	0.999	0.998	0.996	0.995	0.991	0.984	0.976	0.965	0.953	0.923	0.908	0.872	0.790
0.50	0.21539	0.999	0.998	0.995	0.994	0.987	0.977	0.964	0.950	0.923	0.893	0.858	0.820	0.781	0.742	0.661
1.00	0.18182	0.999	0.994	0.986	0.977	0.964	0.945	0.915	0.866	0.804	0.736	0.668	0.604	0.48	0.375	0.224
2.00	0.13834	0.997	0.991	0.986	0.976	0.965	0.946	0.918	0.866	0.810	0.728	0.646	0.546	0.436	0.320	0.200
4.00	0.09316	0.994	0.975	0.944	0.904	0.856	0.803	0.690	0.577	0.533	0.351	0.222	0.133	0.034	0.002	0.000
8.00	0.05601	0.990	0.963	0.919	0.863	0.799	0.731	0.594	0.472	0.424	0.258	0.193	0.146	0.037	0.004	0.000
16.00	0.03104	0.988	0.954	0.901	0.835	0.761	0.693	0.538	0.414	0.296	0.213	0.156	0.104	0.077	0.033	0.001
32.00	0.01639	0.987	0.949	0.891	0.819	0.739	0.659	0.508	0.384	0.270	0.192	0.139	0.069	0.033	0.001	0.000
64.00	0.00428	0.986	0.944	0.882	0.805	0.722	0.638	0.484	0.361	0.250	0.181	0.130	0.052	0.022	0.001	0.000
128.00	0.00215	0.985	0.944	0.880	0.803	0.719	0.634	0.480	0.357	0.247	0.173	0.116	0.042	0.005	0.002	0.000
256.00	0.00108	0.985	0.943	0.880	0.802	0.717	0.632	0.478	0.355	0.245	0.172	0.114	0.043	0.005	0.002	0.000

(d-8) Wall half-angle, 75°

0.25	0.22133	1.000	0.999	0.999	0.997	0.996	0.994	0.984	0.975	0.964	0.951	0.937	0.904	0.867	0.782	0.690
0.50	0.20031	0.999	0.998	0.995	0.986	0.961	0.948	0.926	0.886	0.853	0.814	0.733	0.650	0.494	0.277	0.158
1.00	0.16822	0.998	0.994	0.988	0.976	0.962	0.946	0.916	0.862	0.828	0.728	0.591	0.468	0.367	0.228	0.045
2.00	0.12724	0.996	0.986	0.969	0.945	0.916	0.883	0.807	0.74	0.619	0.522	0.436	0.362	0.251	0.176	0.042
4.00	0.08543	0.994	0.974	0.944	0.904	0.857	0.804	0.692	0.581	0.458	0.358	0.279	0.219	0.137	0.090	0.043
8.00	0.05147	0.991	0.963	0.920	0.865	0.802	0.734	0.599	0.478	0.355	0.263	0.197	0.149	0.089	0.057	0.026
16.00	0.02864	0.988	0.954	0.902	0.837	0.763	0.687	0.541	0.418	0.299	0.216	0.158	0.114	0.069	0.043	0.020
32.00	0.01517	0.987	0.949	0.891	0.820	0.741	0.660	0.510	0.386	0.271	0.193	0.140	0.103	0.060	0.015	0.000
64.00	0.00781	0.986	0.946	0.885	0.810	0.728	0.646	0.493	0.370	0.258	0.182	0.131	0.096	0.055	0.034	0.010
128.00	0.00397	0.986	0.945	0.882	0.805	0.722	0.638	0.485	0.362	0.251	0.176	0.126	0.093	0.053	0.033	0.008
256.00	0.00200	0.985	0.944	0.880	0.803	0.719	0.634	0.480	0.358	0.247	0.173	0.124	0.091	0.052	0.032	0.008
512.00	0.00100	0.985	0.943	0.880	0.802	0.717	0.632	0.478	0.356	0.246	0.172	0.123	0.090	0.052	0.032	0.006

(e-5) Wall half-angle, 30°

0.25	0.19049	1.000	1.000	1.000	0.999	0.998	0.997	0.995	0.992	0.989	0.985	0.981	0.970	0.957	0.926	0.843	0.741	
0.50	0.18067	1.000	0.999	0.999	0.998	0.998	0.997	0.996	0.995	0.989	0.982	0.973	0.961	0.947	0.896	0.854	0.495	0.008
1.00	0.16321	0.999	0.998	0.994	0.990	0.985	0.978	0.962	0.941	0.909	0.871	0.848	0.810	0.551	0.045	0.004	0.001	0.001
2.00	0.13521	0.998	0.992	0.984	0.983	0.970	0.953	0.933	0.914	0.884	0.824	0.739	0.649	0.562	0.423	0.007	0.001	0.001
4.00	0.09860	0.995	0.981	0.959	0.948	0.932	0.915	0.893	0.871	0.849	0.824	0.798	0.738	0.672	0.569	0.040	0.017	0.009
8.00	0.06305	0.992	0.969	0.932	0.912	0.884	0.854	0.829	0.799	0.769	0.644	0.428	0.112	0.058	0.035	0.023	0.011	0.001
16.00	0.03653	0.989	0.959	0.925	0.901	0.851	0.783	0.711	0.503	0.155	0.076	0.042	0.026	0.017	0.009	0.005	0.002	0.001
32.00	0.01985	0.988	0.952	0.897	0.829	0.753	0.674	0.541	0.116	0.061	0.036	0.023	0.015	0.008	0.005	0.002	0.001	0.000
64.00	0.01038	0.986	0.948	0.889	0.815	0.735	0.654	0.568	0.104	0.056	0.033	0.021	0.012	0.007	0.004	0.002	0.001	0.000
128.00	0.00531	0.986	0.945	0.884	0.808	0.726	0.642	0.234	0.098	0.053	0.032	0.020	0.014	0.007	0.004	0.002	0.000	0.000
256.00	0.00269	0.986	0.944	0.881	0.804	0.721	0.621	0.17	0.096	0.052	0.032	0.020	0.014	0.007	0.004	0.002	0.000	0.000
512.00	0.00135	0.985	0.944	0.880	0.802	0.718	0.669	0.209	0.095	0.052	0.031	0.020	0.014	0.007	0.004	0.002	0.000	0.000

(e-6) Wall half-angle, 45°

0.25	0.15227	1.000	1.000	1.000	0.999	0.998	0.997	0.995	0.993	0.993	0.989	0.986	0.981	0.971	0.959	0.929	0.850	0.757
0.50	0.14420	1.000	0.999	0.998	0.998	0.995	0.991	0.986	0.982	0.974	0.963	0.950	0.935	0.902	0.863	0.777	0.591	0.424
1.00	0.13059	0.999	0.998	0.995	0.994	0.986	0.975	0.964	0.956	0.946	0.918	0.885	0.849	0.809	0.726	0.640	0.475	0.020
2.00	0.10960	0.998	0.998	0.994	0.994	0.986	0.975	0.964	0.954	0.944	0.916	0.886	0.841	0.791	0.641	0.567	0.325	0.002
4.00	0.08234	0.996	0.985	0.966	0.966	0.941	0.910	0.875	0.792	0.703	0.590	0.487	0.399	0.326	0.230	0.101	0.003	0.001
8.00	0.05440	0.993	0.972	0.939	0.916	0.845	0.789	0.670	0.554	0.433	0.332	0.208	0.100	0.005	0.002	0.000	0.000	0.000
16.00	0.03219	0.990	0.961	0.916	0.858	0.792	0.722	0.584	0.462	0.340	0.277	0.166	0.070	0.004	0.001	0.000	0.000	0.000
32.00	0.01769	0.988	0.953	0.899	0.832	0.758	0.680	0.533	0.410	0.191	0.036	0.020	0.012	0.006	0.001	0.000	0.000	0.000
64.00	0.00939	0.987	0.948	0.890	0.817	0.738	0.657	0.506	0.382	0.18	0.032	0.018	0.011	0.005	0.003	0.001	0.000	0.000
128.00	0.00477	0.986	0.946	0.884	0.809	0.727	0.644	0.491	0.368	0.086	0.030	0.017	0.011	0.005	0.003	0.001	0.000	0.000
256.00	0.00242	0.986	0.944	0.882	0.805	0.721	0.637	0.484	0.361	0.070	0.029	0.016	0.010	0.005	0.003	0.001	0.000	0.000
512.00	0.00122	0.985	0.944	0.880	0.803	0.718	0.634	0.480	0.357	0.063	0.026	0.016	0.010	0.005	0.003	0.001	0.000	0.000

(e-7) Wall half-angle, 60°

0.25	0.13C95	1.000	1.000	1.000	0.999	0.998	0.997	0.995	0.992	0.989	0.985	0.981	0.971	0.958	0.927	0.847	0.754	
0.50	0.12398	1.000	0.999	0.998	0.997	0.996	0.995	0.994	0.989	0.983	0.973	0.962	0.949	0.934	0.900	0.861	0.774	0.591
1.00	0.11204	0.999	0.998	0.997	0.996	0.995	0.991	0.986	0.980	0.965	0.946	0.917	0.884	0.849	0.803	0.726	0.643	0.432
2.00	0.09391	0.998	0.975	0.944	0.906	0.845	0.772	0.702	0.605	0.505	0.404	0.304	0.204	0.147	0.089	0.049	0.021	0.014
4.00	0.07086	0.996	0.966	0.936	0.894	0.821	0.748	0.670	0.570	0.470	0.370	0.270	0.170	0.110	0.060	0.035	0.015	0.005
8.00	0.04739	0.993	0.974	0.943	0.902	0.834	0.760	0.680	0.580	0.480	0.380	0.280	0.180	0.120	0.070	0.040	0.020	0.005
16.00	0.02844	0.990	0.962	0.932	0.893	0.821	0.749	0.670	0.570	0.470	0.370	0.270	0.170	0.110	0.060	0.030	0.015	0.005
32.00	0.01573	0.988	0.954	0.901	0.856	0.785	0.716	0.645	0.545	0.445	0.345	0.245	0.145	0.090	0.050	0.025	0.010	0.005
64.00	0.00831	0.987	0.949	0.891	0.849	0.770	0.700	0.629	0.529	0.429	0.329	0.229	0.129	0.079	0.049	0.024	0.010	0.005
128.00	0.00427	0.986	0.946	0.885	0.810	0.728	0.645	0.542	0.442	0.342	0.242	0.142	0.071	0.041	0.024	0.011	0.005	0.000
256.00	0.00217	0.986	0.944	0.882	0.805	0.722	0.638	0.536	0.436	0.336	0.236	0.136	0.066	0.036	0.022	0.011	0.005	0.000
512.00	0.00109	0.985	0.944	0.880	0.803	0.719	0.634	0.480	0.357	0.257	0.157	0.057	0.019	0.009	0.004	0.002	0.001	0.000

(e-8) Wall half-angle, 75°

0.25	0.11992	1.000	1.000	1.000	0.999	0.998	0.997	0.995	0.992	0.989	0.985	0.980	0.970	0.957	0.925	0.844	0.748
0.50	0.11340	1.000	0.999	0.998	0.995	0.991	0.979	0.964	0.944	0.915	0.882	0.845	0.805	0.721	0.637	0.584	0.425
1.00	0.10225	0.999	0.998	0.994	0.986	0.974	0.961	0.944	0.904	0.857	0.790	0.720	0.650	0.581	0.493	0.368	0.268
2.00	0.08544	0.998	0.996	0.995	0.985	0.974	0.961	0.944	0.904	0.857	0.790	0.720	0.650	0.581	0.493	0.368	0.268
4.00	0.06428	0.996	0.996	0.995	0.985	0.974	0.961	0.944	0.904	0.857	0.790	0.720	0.650	0.581	0.493	0.368	0.268
8.00	0.04297	0.993	0.974	0.943	0.903	0.855	0.802	0.689	0.578	0.455	0.355	0.277	0.171	0.136	0.093	0.043	0.000
16.00	0.02582	0.991	0.963	0.930	0.864	0.801	0.733	0.598	0.477	0.356	0.262	0.196	0.149	0.089	0.057	0.026	0.000
32.00	0.01435	0.988	0.954	0.902	0.836	0.763	0.687	0.541	0.417	0.299	0.216	0.158	0.118	0.069	0.041	0.020	0.000
64.00	0.00760	0.987	0.949	0.891	0.820	0.741	0.660	0.510	0.386	0.271	0.193	0.140	0.103	0.060	0.037	0.013	0.000
128.00	0.00391	0.986	0.946	0.885	0.810	0.728	0.646	0.493	0.360	0.258	0.182	0.117	0.076	0.041	0.020	0.005	0.000
256.00	0.00199	0.986	0.945	0.882	0.805	0.722	0.638	0.485	0.362	0.251	0.176	0.116	0.071	0.040	0.020	0.005	0.000
512.00	0.00100	0.985	0.944	0.880	0.803	0.719	0.634	0.480	0.358	0.247	0.173	0.109	0.071	0.041	0.020	0.005	0.000

TABLE I. - Continued. CALCULATED ANGULAR DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS AXIAL DISTANCES FROM SLOT EXIT

(f) Length to inlet width ratio, 8.00

(f-1) Wall half-angle, 0°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux, $n(O) n_1$	Distance from centerplane, $\frac{y}{L}$								Flux relative to centerplane, $n(y/L, x/L)$								
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
0.25	0.24888	1.000	0.998	0.996	0.993	0.988	0.983	0.969	0.949	0.915	0.868	0.808	0.719	0.209	0.086	0.024	0.005	0.002
0.50	0.21073	1.000	0.998	0.992	0.981	0.967	0.948	0.926	0.870	0.804	0.731	0.621	0.522	0.422	0.322	0.222	0.133	0.039
1.00	0.15834	0.995	0.982	0.961	0.932	0.898	0.852	0.798	0.723	0.642	0.591	0.560	0.522	0.462	0.392	0.322	0.222	0.133
2.00	0.10939	0.994	0.976	0.882	0.554	0.411	0.321	0.208	0.139	0.087	0.057	0.039	0.027	0.015	0.009	0.004	0.001	0.000
4.00	0.07141	0.993	0.749	0.482	0.358	0.280	0.223	0.147	0.100	0.063	0.042	0.029	0.019	0.011	0.005	0.003	0.001	0.000
8.00	0.04398	0.865	0.522	0.361	0.275	0.217	0.175	0.116	0.079	0.050	0.033	0.023	0.016	0.009	0.005	0.002	0.001	0.000
16.00	0.02546	0.741	0.426	0.302	0.232	0.184	0.148	0.098	0.067	0.043	0.029	0.020	0.014	0.008	0.005	0.002	0.001	0.000
32.00	0.01396	0.670	0.379	0.271	0.209	0.166	0.134	0.090	0.061	0.039	0.026	0.017	0.013	0.007	0.004	0.002	0.001	0.000
64.00	0.00736	0.631	0.356	0.256	0.198	0.157	0.127	0.085	0.058	0.037	0.025	0.017	0.012	0.007	0.004	0.002	0.001	0.000
128.00	0.00379	0.610	0.344	0.248	0.191	0.152	0.123	0.082	0.056	0.036	0.024	0.016	0.012	0.006	0.004	0.002	0.001	0.000
256.00	0.00192	0.600	0.338	0.243	0.188	0.150	0.121	0.081	0.055	0.035	0.023	0.016	0.012	0.006	0.004	0.002	0.001	0.000
512.00	0.00097	0.594	0.335	0.241	0.187	0.149	0.120	0.080	0.055	0.035	0.023	0.016	0.011	0.006	0.004	0.002	0.001	0.000

(f-2) Wall half-angle, 5°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux, $n(O) n_1$	Distance from centerplane, $\frac{y}{L}$								Flux relative to centerplane, $n(y/L, x/L)$								
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
0.25	0.21572	1.000	1.000	0.999	0.999	0.998	0.998	0.993	0.969	0.949	0.915	0.868	0.808	0.719	0.209	0.086	0.024	0.004
0.50	0.20174	1.000	0.999	0.997	0.994	0.991	0.987	0.987	0.962	0.939	0.906	0.864	0.810	0.746	0.614	0.494	0.305	0.002
1.00	0.17381	0.998	0.994	0.986	0.974	0.960	0.942	0.896	0.839	0.695	0.291	0.166	0.103	0.046	0.024	0.009	0.002	0.001
2.00	0.13277	0.996	0.984	0.965	0.939	0.907	0.872	0.459	0.261	0.151	0.094	0.061	0.041	0.024	0.012	0.005	0.001	0.001
4.00	0.09144	0.994	0.976	0.948	0.813	0.507	0.361	0.218	0.142	0.087	0.056	0.038	0.026	0.014	0.008	0.004	0.001	0.000
8.00	0.05820	0.992	0.969	0.689	0.424	0.310	0.240	0.151	0.101	0.063	0.041	0.028	0.020	0.011	0.006	0.003	0.001	0.000
16.00	0.03447	0.990	0.594	0.456	0.320	0.243	0.191	0.123	0.083	0.052	0.034	0.023	0.016	0.009	0.005	0.002	0.001	0.000
32.00	0.01919	0.588	0.554	0.381	0.275	0.212	0.167	0.109	0.073	0.046	0.030	0.021	0.015	0.008	0.005	0.002	0.001	0.000
64.00	0.01021	0.579	0.578	0.347	0.254	0.196	0.155	0.101	0.068	0.043	0.028	0.019	0.014	0.007	0.004	0.002	0.001	0.000
128.00	0.00528	0.544	0.539	0.331	0.243	0.188	0.149	0.098	0.066	0.042	0.027	0.019	0.013	0.007	0.004	0.002	0.001	0.000
256.00	0.00269	0.516	0.519	0.323	0.238	0.184	0.146	0.096	0.064	0.041	0.027	0.018	0.013	0.007	0.004	0.002	0.001	0.000
512.00	0.00136	0.517	0.509	0.319	0.235	0.182	0.145	0.095	0.064	0.040	0.027	0.018	0.013	0.007	0.004	0.002	0.001	0.000

(f-3) Wall half-angle, 10°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux, $n(O) n_1$	Distance from centerplane, $\frac{y}{L}$								Flux relative to centerplane, $n(y/L, x/L)$									
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.	
0.25	0.17743	1.000	1.000	0.999	0.999	0.998	0.998	0.993	0.997	0.995	0.995	0.993	0.991	0.988	0.981	0.973	0.952	0.881	0.515
0.50	0.17025	1.000	0.999	0.998	0.995	0.991	0.986	0.992	0.987	0.980	0.971	0.960	0.947	0.913	0.864	0.816	0.004	0.004	0.004
1.00	0.15561	0.999	0.998	0.996	0.991	0.981	0.979	0.962	0.945	0.920	0.903	0.893	0.860	0.810	0.760	0.717	0.664	0.017	0.004
2.00	0.12946	0.998	0.991	0.981	0.966	0.947	0.924	0.868	0.803	0.746	0.693	0.653	0.613	0.562	0.512	0.467	0.417	0.364	0.004
4.00	0.09489	0.995	0.981	0.959	0.929	0.893	0.853	0.807	0.725	0.640	0.573	0.508	0.438	0.362	0.317	0.267	0.217	0.167	0.004
8.00	0.06251	0.993	0.972	0.940	0.908	0.607	0.356	0.196	0.123	0.074	0.047	0.032	0.022	0.017	0.012	0.007	0.003	0.001	0.000
16.00	0.03777	0.991	0.964	0.922	0.541	0.327	0.238	0.144	0.093	0.057	0.037	0.025	0.017	0.012	0.006	0.002	0.001	0.000	0.000
32.00	0.02127	0.989	0.956	0.695	0.375	0.262	0.197	0.122	0.080	0.049	0.032	0.022	0.015	0.008	0.005	0.002	0.001	0.000	0.000
64.00	0.01139	0.987	0.954	0.627	0.347	0.234	0.178	0.111	0.073	0.046	0.030	0.020	0.014	0.008	0.005	0.002	0.001	0.000	0.000
128.00	0.00591	0.986	0.986	0.929	0.513	0.305	0.222	0.169	0.106	0.070	0.044	0.029	0.019	0.014	0.007	0.004	0.002	0.001	0.000
256.00	0.00301	0.986	0.988	0.982	0.482	0.295	0.215	0.165	0.104	0.069	0.043	0.028	0.019	0.013	0.007	0.004	0.002	0.001	0.000
512.00	0.00152	0.985	0.982	0.466	0.290	0.212	0.163	0.103	0.068	0.042	0.028	0.019	0.013	0.007	0.004	0.002	0.001	0.000	0.000

TABLE I. - Continued. CALCULATED ANGULAR DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS AXIAL DISTANCES FROM SLOT EXIT

(g) Length to inlet width ratio, 0.25

(g-1) Wall half-angle, -5°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux relative to inlet flux, $n(0)/n_1$	Distance from centerplane, $\frac{y}{L}$								Distance from centerplane, $\frac{n(y)(x-L)}{n(0)}$								
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
0.25	0.80849	0.999	0.997	0.992	0.986	0.978	0.967	0.945	0.910	0.850	0.769	0.668	0.531	0.277	0.139	0.042	0.007	0.003
0.50	0.62935	0.996	0.985	0.967	0.941	0.907	0.868	0.770	0.643	0.474	0.334	0.231	0.161	0.082	0.045	0.016	0.004	0.002
1.00	0.40463	0.991	0.966	0.925	0.872	0.792	0.718	0.559	0.420	0.287	0.196	0.135	0.095	0.050	0.028	0.010	0.003	0.001
2.00	0.22586	0.988	0.948	0.883	0.804	0.719	0.633	0.475	0.348	0.234	0.159	0.110	0.078	0.041	0.023	0.009	0.002	0.001
4.00	0.11810	0.980	0.929	0.859	0.776	0.689	0.602	0.446	0.325	0.218	0.148	0.102	0.072	0.038	0.022	0.008	0.002	0.001
8.00	0.05985	0.976	0.924	0.853	0.768	0.680	0.593	0.438	0.317	0.212	0.144	0.099	0.070	0.037	0.021	0.008	0.002	0.001
16.00	0.02999	0.980	0.927	0.854	0.769	0.680	0.592	0.436	0.316	0.211	0.143	0.099	0.070	0.037	0.021	0.008	0.002	0.001
32.00	0.01500	0.981	0.928	0.855	0.769	0.680	0.591	0.436	0.315	0.210	0.142	0.098	0.069	0.037	0.021	0.008	0.002	0.001
64.00	0.00750	0.982	0.929	0.855	0.770	0.680	0.592	0.436	0.315	0.210	0.142	0.098	0.069	0.037	0.021	0.008	0.002	0.001
128.00	0.00375	0.982	0.929	0.856	0.770	0.680	0.592	0.436	0.315	0.210	0.142	0.098	0.069	0.037	0.021	0.008	0.002	0.001
256.00	0.00187	0.983	0.929	0.856	0.770	0.680	0.592	0.436	0.315	0.210	0.142	0.098	0.069	0.037	0.021	0.008	0.002	0.001
512.00	0.00094	0.983	0.929	0.856	0.770	0.680	0.592	0.436	0.315	0.210	0.142	0.098	0.069	0.037	0.021	0.008	0.002	0.001

(g-2) Wall half-angle, -10°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux relative to inlet flux, $n(0)/n_1$	Distance from centerplane, $\frac{y}{L}$								Distance from centerplane, $\frac{n(y)(x-L)}{n(0)}$								
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
0.25	0.80849	0.999	0.997	0.992	0.986	0.978	0.967	0.945	0.910	0.850	0.769	0.668	0.531	0.277	0.139	0.042	0.007	0.003
0.50	0.62930	0.996	0.984	0.964	0.925	0.868	0.770	0.643	0.474	0.334	0.231	0.161	0.082	0.045	0.016	0.004	0.002	0.001
1.00	0.39693	0.991	0.964	0.920	0.855	0.780	0.701	0.543	0.407	0.278	0.190	0.132	0.093	0.049	0.028	0.011	0.003	0.001
2.00	0.21981	0.982	0.937	0.872	0.794	0.709	0.624	0.469	0.332	0.232	0.158	0.110	0.078	0.042	0.024	0.009	0.003	0.001
4.00	0.11302	0.982	0.932	0.862	0.779	0.692	0.605	0.449	0.327	0.220	0.150	0.104	0.074	0.043	0.023	0.009	0.003	0.001
8.00	0.05678	0.985	0.936	0.864	0.779	0.690	0.602	0.445	0.324	0.217	0.147	0.102	0.072	0.039	0.022	0.009	0.003	0.001
16.00	0.02843	0.985	0.938	0.865	0.780	0.690	0.601	0.444	0.322	0.216	0.147	0.102	0.072	0.038	0.022	0.009	0.003	0.001
32.00	0.01422	0.985	0.939	0.867	0.781	0.690	0.601	0.444	0.322	0.216	0.146	0.101	0.072	0.038	0.022	0.009	0.003	0.001
64.00	0.00711	0.985	0.940	0.867	0.781	0.690	0.601	0.444	0.322	0.215	0.146	0.101	0.072	0.038	0.022	0.009	0.003	0.001
128.00	0.00355	0.985	0.940	0.867	0.781	0.690	0.601	0.444	0.322	0.215	0.146	0.101	0.072	0.038	0.022	0.009	0.003	0.001
256.00	0.00178	0.985	0.941	0.867	0.781	0.690	0.601	0.444	0.322	0.215	0.146	0.101	0.072	0.038	0.022	0.009	0.003	0.001
512.00	0.00089	0.985	0.941	0.867	0.781	0.690	0.601	0.444	0.322	0.215	0.146	0.101	0.072	0.038	0.022	0.009	0.003	0.001

(g-3) Wall half-angle, -20°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux relative to inlet flux, $n(0)/n_1$	Distance from centerplane, $\frac{y}{L}$								Distance from centerplane, $\frac{n(y)(x-L)}{n(0)}$								
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
0.25	0.80817	0.999	0.996	0.992	0.982	0.972	0.959	0.924	0.874	0.789	0.659	0.511	0.374	0.187	0.097	0.033	0.007	0.003
0.50	0.62929	0.995	0.981	0.958	0.925	0.881	0.825	0.694	0.555	0.398	0.277	0.192	0.135	0.071	0.040	0.015	0.004	0.002
1.00	0.37668	0.987	0.950	0.897	0.830	0.754	0.675	0.520	0.389	0.266	0.182	0.127	0.090	0.049	0.028	0.011	0.003	0.001
2.00	0.20082	0.986	0.940	0.878	0.818	0.741	0.681	0.547	0.417	0.335	0.235	0.161	0.112	0.080	0.043	0.020	0.005	0.001
4.00	0.10197	0.985	0.944	0.878	0.794	0.706	0.618	0.466	0.336	0.227	0.155	0.108	0.077	0.042	0.024	0.010	0.003	0.001
8.00	0.05118	0.985	0.943	0.879	0.795	0.705	0.616	0.457	0.334	0.225	0.153	0.107	0.076	0.041	0.024	0.010	0.003	0.001
16.00	0.02566	0.985	0.943	0.879	0.796	0.705	0.616	0.457	0.333	0.224	0.153	0.107	0.076	0.041	0.024	0.010	0.003	0.001
32.00	0.01281	0.985	0.943	0.879	0.797	0.706	0.616	0.457	0.332	0.224	0.153	0.106	0.076	0.041	0.024	0.010	0.003	0.001
64.00	0.00641	0.985	0.943	0.879	0.797	0.706	0.616	0.457	0.332	0.224	0.153	0.106	0.076	0.041	0.024	0.010	0.003	0.001
128.00	0.00320	0.985	0.943	0.879	0.797	0.706	0.616	0.457	0.332	0.224	0.153	0.106	0.076	0.041	0.024	0.010	0.003	0.001
256.00	0.00160	0.985	0.943	0.879	0.797	0.706	0.616	0.457	0.332	0.224	0.153	0.106	0.076	0.041	0.024	0.010	0.003	0.001
512.00	0.00080	C.985	0.943	0.879	0.797	0.706	0.616	0.457	0.332	0.224	0.153	0.106	0.076	0.041	0.024	0.010	0.003	0.001

(g-4) Wall half-angle, -30°

0.25	0.79314	0.998	0.994	0.986	0.975	0.960	0.942	0.892	0.814	0.684	0.536	0.394	0.280	0.141	0.076	0.028	0.007	0.003
0.50	0.57356	0.994	0.973	0.940	0.940	0.894	0.839	0.776	0.636	0.498	0.351	0.244	0.170	0.121	0.065	0.037	0.015	0.004
1.00	0.33454	0.988	0.954	0.827	0.749	0.667	0.511	0.381	0.260	0.180	0.126	0.090	0.049	0.029	0.012	0.004	0.002	
2.00	0.17477	0.985	0.946	0.885	0.890	0.723	0.639	0.478	0.352	0.239	0.165	0.116	0.083	0.046	0.027	0.011	0.003	0.001
4.00	0.08840	0.985	0.944	0.890	0.803	0.718	0.629	0.470	0.344	0.234	0.161	0.113	0.081	0.044	0.026	0.011	0.003	0.001
8.00	0.04433	0.985	0.943	0.879	0.801	0.716	0.628	0.443	0.342	0.232	0.159	0.112	0.080	0.044	0.026	0.011	0.003	0.001
16.00	0.02218	0.985	0.943	0.879	0.801	0.716	0.629	0.468	0.342	0.232	0.159	0.112	0.080	0.044	0.026	0.011	0.003	0.001
32.00	0.01109	0.985	0.943	0.879	0.800	0.716	0.629	0.468	0.342	0.232	0.159	0.111	0.080	0.044	0.026	0.011	0.003	0.001
64.00	0.00555	0.985	0.943	0.879	0.800	0.716	0.629	0.468	0.342	0.232	0.159	0.111	0.080	0.044	0.026	0.011	0.003	0.001
128.00	0.00277	0.985	0.943	0.879	0.800	0.716	0.629	0.468	0.342	0.231	0.159	0.111	0.080	0.044	0.026	0.011	0.003	0.001
256.00	0.00139	0.985	0.943	0.879	0.800	0.716	0.629	0.468	0.342	0.231	0.159	0.111	0.080	0.044	0.026	0.011	0.003	0.001
512.00	0.00069	0.985	0.943	0.879	0.800	0.716	0.630	0.468	0.342	0.231	0.159	0.111	0.080	0.044	0.026	0.011	0.003	0.001

(g-5) Wall half-angle, -45°

0.25	0.70711	0.995	0.983	0.963	0.936	0.901	0.858	0.752	0.628	0.470	0.336	0.236	0.167	0.088	0.051	0.020	0.006	0.002
0.50	0.44721	0.990	0.962	0.918	0.859	0.791	0.715	0.562	0.426	0.296	0.205	0.144	0.104	0.057	0.034	0.015	0.004	0.002
1.00	0.24254	0.987	0.949	0.891	0.818	0.737	0.654	0.499	0.370	0.254	0.176	0.124	0.090	0.055	0.030	0.013	0.004	0.002
2.00	0.12403	0.986	0.944	0.892	0.805	0.721	0.637	0.482	0.357	0.244	0.169	0.119	0.086	0.048	0.029	0.013	0.004	0.002
4.00	0.06238	0.985	0.943	0.880	0.802	0.717	0.632	0.478	0.354	0.241	0.167	0.118	0.085	0.048	0.029	0.013	0.004	0.002
8.00	0.03123	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.353	0.241	0.167	0.118	0.085	0.048	0.029	0.013	0.004	0.002
16.00	0.01562	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.353	0.241	0.166	0.118	0.085	0.047	0.028	0.013	0.004	0.002
32.00	0.00781	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.353	0.241	0.166	0.118	0.085	0.047	0.028	0.013	0.004	0.002
64.00	0.00391	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.353	0.241	0.166	0.118	0.085	0.047	0.028	0.013	0.004	0.002
128.00	0.00195	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.241	0.166	0.118	0.085	0.047	0.028	0.013	0.004	0.002
256.00	0.00098	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.241	0.166	0.118	0.085	0.047	0.028	0.013	0.004	0.002
512.00	0.00049	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.241	0.166	0.118	0.085	0.047	0.028	0.013	0.004	0.002

(g-6) Wall half-angle, -60°

0.25	0.28715	0.987	0.951	0.895	0.825	0.746	0.664	0.509	0.381	0.264	0.184	0.131	0.092	0.054	0.033	0.014	0.004	0.002
0.50	0.14834	0.986	0.945	0.883	0.807	0.723	0.639	0.485	0.361	0.261	0.174	0.124	0.090	0.051	0.031	0.014	0.004	0.002
1.00	0.07479	0.985	0.943	0.880	0.802	0.718	0.633	0.478	0.355	0.245	0.172	0.122	0.089	0.050	0.031	0.014	0.004	0.002
2.00	0.03747	0.985	0.943	0.879	0.801	0.716	0.631	0.477	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
4.00	0.01875	0.985	0.943	0.879	0.801	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
8.00	0.00932	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
16.00	0.00469	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
32.00	0.00234	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
64.00	0.00117	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
128.00	0.00059	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
256.00	0.00029	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002
512.00	0.00015	0.985	0.943	0.879	0.800	0.716	0.631	0.476	0.354	0.244	0.171	0.122	0.089	0.050	0.031	0.014	0.004	0.002

TABLE I. - Continued. CALCULATED ANGULAR DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS AXIAL DISTANCES FROM SLOT EXIT

(h) Length to inlet width ratio, 0.50

(h-1) Wall half-angle, -5°

Axial distance from slot exit, $\frac{x}{L}$	Center-plane flux relative to slot exit, $n(0)/n_1$	Distance from centerplane, $\frac{y}{\sqrt{x-L}}$																
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
(h-2) Wall half-angle, -10°																		
0.25	0.73459	0.599	0.998	0.991	0.983	0.973	0.960	0.927	0.880	0.803	0.532	0.384	0.182	0.086	0.006	0.002		
0.50	0.55941	0.596	0.996	0.995	0.995	0.997	0.987	0.974	0.930	0.863	0.693	0.532	0.384	0.182	0.086	0.006	0.002	
1.00	0.35410	0.991	0.965	0.911	0.839	0.758	0.674	0.567	0.399	0.271	0.182	0.124	0.058	0.031	0.013	0.004	0.001	
2.00	0.19888	0.974	0.920	0.848	0.765	0.677	0.589	0.375	0.248	0.164	0.109	0.073	0.037	0.022	0.008	0.003	0.001	
4.00	0.10197	0.881	0.621	0.643	0.754	0.662	0.572	0.414	0.294	0.190	0.123	0.081	0.054	0.032	0.019	0.008	0.002	0.001
8.00	0.05118	0.585	0.929	0.755	0.661	0.569	0.410	0.289	0.186	0.120	0.079	0.053	0.030	0.018	0.008	0.002	0.001	
16.00	0.02562	0.985	0.933	0.850	0.757	0.661	0.569	0.408	0.287	0.184	0.119	0.078	0.054	0.030	0.018	0.008	0.002	0.001
32.00	0.01281	0.985	0.936	0.852	0.758	0.662	0.569	0.408	0.287	0.184	0.119	0.078	0.054	0.030	0.018	0.008	0.002	0.001
64.00	0.00644	0.585	0.937	0.853	0.759	0.662	0.569	0.408	0.286	0.183	0.118	0.078	0.054	0.030	0.018	0.008	0.002	0.001
128.00	0.00320	0.985	0.938	0.854	0.759	0.662	0.569	0.407	0.286	0.183	0.118	0.077	0.054	0.030	0.018	0.008	0.002	0.001
256.00	0.00160	0.985	0.938	0.854	0.759	0.662	0.569	0.407	0.286	0.183	0.118	0.077	0.054	0.030	0.018	0.008	0.002	0.001
512.00	0.00080	0.985	0.938	0.854	0.759	0.662	0.569	0.407	0.286	0.183	0.118	0.077	0.054	0.030	0.018	0.008	0.002	0.001
(h-3) Wall half-angle, -20°																		
0.25	0.71861	0.998	0.993	0.970	0.952	0.930	0.871	0.784	0.630	0.470	0.333	0.229	0.109	0.055	0.021	0.006	0.002	
0.50	0.51119	0.994	0.976	0.944	0.890	0.827	0.756	0.606	0.463	0.318	0.214	0.145	0.099	0.050	0.029	0.012	0.004	0.002
1.00	0.30418	0.980	0.934	0.871	0.795	0.713	0.629	0.474	0.344	0.228	0.152	0.102	0.071	0.041	0.021	0.010	0.003	0.001
2.00	0.15759	0.988	0.985	0.944	0.870	0.784	0.632	0.463	0.318	0.208	0.138	0.092	0.061	0.036	0.022	0.009	0.003	0.001
4.00	0.07975	0.985	0.985	0.944	0.877	0.785	0.630	0.459	0.310	0.202	0.133	0.081	0.064	0.035	0.021	0.009	0.003	0.001
8.00	0.03997	0.985	0.986	0.944	0.879	0.788	0.691	0.597	0.433	0.307	0.200	0.131	0.088	0.063	0.035	0.021	0.009	0.003
16.00	0.02020	0.985	0.985	0.943	0.879	0.791	0.693	0.598	0.432	0.306	0.199	0.130	0.088	0.063	0.035	0.021	0.009	0.003
32.00	0.01020	0.985	0.985	0.943	0.879	0.792	0.693	0.598	0.432	0.306	0.198	0.130	0.088	0.063	0.035	0.021	0.009	0.003
64.00	0.00500	0.985	0.985	0.943	0.879	0.793	0.694	0.598	0.432	0.306	0.198	0.130	0.088	0.063	0.035	0.021	0.009	0.003
128.00	0.00250	0.985	0.985	0.943	0.879	0.793	0.694	0.598	0.432	0.306	0.198	0.130	0.088	0.063	0.035	0.021	0.009	0.003
256.00	0.00125	0.985	0.985	0.943	0.879	0.793	0.694	0.598	0.432	0.306	0.198	0.130	0.088	0.063	0.035	0.021	0.009	0.003
512.00	0.00062	0.985	0.985	0.943	0.879	0.793	0.694	0.598	0.432	0.306	0.198	0.130	0.088	0.063	0.035	0.021	0.009	0.003
(h-4) Wall half-angle, -30°																		
0.25	0.62606	0.996	0.983	0.958	0.921	0.873	0.818	0.689	0.551	0.394	0.273	0.187	0.130	0.066	0.016	0.005	0.002	
0.50	0.38723	0.989	0.955	0.944	0.890	0.827	0.754	0.517	0.383	0.259	0.175	0.120	0.084	0.046	0.025	0.012	0.004	0.002
1.00	0.20554	0.986	0.947	0.887	0.810	0.721	0.632	0.470	0.341	0.227	0.152	0.105	0.072	0.042	0.025	0.011	0.003	0.001
2.00	0.10444	0.986	0.944	0.881	0.804	0.711	0.624	0.458	0.330	0.218	0.146	0.101	0.073	0.041	0.025	0.011	0.003	0.001
4.00	0.05243	0.985	0.943	0.879	0.801	0.717	0.624	0.456	0.327	0.215	0.144	0.100	0.072	0.040	0.024	0.011	0.003	0.001
8.00	0.02624	0.985	0.943	0.879	0.801	0.716	0.626	0.456	0.326	0.214	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001
16.00	0.01312	0.985	0.943	0.879	0.800	0.716	0.627	0.456	0.326	0.214	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001
32.00	0.00656	0.985	0.943	0.879	0.800	0.716	0.627	0.456	0.326	0.214	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001
64.00	0.00328	0.985	0.943	0.879	0.800	0.716	0.628	0.456	0.326	0.213	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001
128.00	0.00164	0.985	0.943	0.879	0.800	0.716	0.628	0.457	0.326	0.213	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001
256.00	0.00084	0.985	0.943	0.879	0.800	0.716	0.628	0.457	0.326	0.213	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001
512.00	0.00041	0.985	0.943	0.879	0.800	0.716	0.628	0.457	0.326	0.213	0.143	0.100	0.072	0.040	0.024	0.011	0.003	0.001

(1) Length to inlet width ratio, 1.00
(1-1) Wall half-angle, -5°

Axial distance from slot exit, $\frac{x - \bar{x}}{L}$	Center-plane flux relative to inlet flux, $n(0)/n_1$	Distance from centerplane, $\frac{y}{x - L}$										Distance from centerplane, $\frac{n(y/x - L)}{n(0)}$									
		.1.	.2.	.3.	.4.	.5.	.6.	.8.	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.	Flux relative to centerplane, $n(y/x - L)$	$n(0)$	
0.25	0.62451	0.599	0.996	0.992	0.985	0.976	0.965	0.895	0.826	0.738	0.568	0.410	0.167	0.075	0.024	0.006	0.002	0.002	0.002	0.002	
0.50	0.48533	0.596	0.985	0.966	0.944	0.907	0.868	0.762	0.592	0.400	0.254	0.133	0.101	0.050	0.028	0.011	0.003	0.001	0.001	0.001	
1.00	0.31894	0.992	0.969	0.933	0.864	0.771	0.676	0.495	0.344	0.206	0.129	0.066	0.032	0.019	0.008	0.002	0.002	0.001	0.001	0.001	
2.00	0.18672	0.990	0.931	0.843	0.764	0.644	0.569	0.380	0.250	0.151	0.099	0.068	0.048	0.026	0.015	0.007	0.002	0.001	0.001	0.001	
4.00	0.10223	0.555	0.877	0.784	0.683	0.583	0.488	0.328	0.210	0.133	0.088	0.050	0.043	0.023	0.014	0.006	0.002	0.001	0.001	0.001	
8.00	0.05243	0.553	0.877	0.772	0.668	0.565	0.459	0.310	0.199	0.127	0.084	0.058	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	
16.00	0.02624	0.563	0.877	0.775	0.668	0.563	0.466	0.305	0.197	0.126	0.084	0.058	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	
32.00	0.01312	0.969	0.881	0.777	0.668	0.562	0.464	0.303	0.196	0.126	0.084	0.057	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	
64.00	0.00656	0.972	0.883	0.778	0.669	0.562	0.463	0.301	0.196	0.126	0.083	0.057	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	
128.00	0.00328	0.974	0.884	0.779	0.669	0.561	0.463	0.301	0.196	0.125	0.083	0.057	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	
256.00	0.00164	0.974	0.884	0.779	0.669	0.561	0.463	0.301	0.195	0.125	0.083	0.057	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	
512.00	0.00082	0.975	0.885	0.779	0.669	0.561	0.462	0.300	0.195	0.125	0.083	0.057	0.041	0.022	0.013	0.006	0.002	0.001	0.001	0.001	

(1-2) Wall half-angle, -10°

Axial distance from slot exit, $\frac{x - \bar{x}}{L}$	Center-plane flux relative to inlet flux, $n(0)/n_1$	Distance from centerplane, $\frac{y}{x - L}$										Distance from centerplane, $\frac{n(y/x - L)}{n(0)}$									
		.1.	.2.	.3.	.4.	.5.	.6.	.8.	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.	Flux relative to centerplane, $n(y/x - L)$	$n(0)$	
0.25	0.61772	0.998	0.993	0.984	0.972	0.956	0.935	0.882	0.811	0.662	0.480	0.323	0.207	0.092	0.048	0.018	0.005	0.002	0.002	0.001	
0.50	0.44936	0.995	0.978	0.861	0.760	0.611	0.451	0.320	0.180	0.120	0.057	0.031	0.018	0.008	0.002	0.001	0.001	0.001	0.001	0.001	
1.00	0.28C81	0.991	0.945	0.869	0.782	0.690	0.597	0.428	0.292	0.181	0.119	0.051	0.031	0.018	0.008	0.002	0.001	0.001	0.001	0.001	
2.00	0.15799	0.568	0.886	0.799	0.70	0.607	0.513	0.352	0.233	0.150	0.100	0.068	0.049	0.027	0.016	0.007	0.002	0.001	0.001	0.001	
4.00	0.07975	0.985	0.904	0.806	0.702	0.606	0.500	0.375	0.225	0.145	0.097	0.067	0.044	0.026	0.016	0.007	0.002	0.001	0.001	0.001	
8.00	0.03997	0.985	0.916	0.813	0.703	0.595	0.495	0.327	0.222	0.143	0.096	0.066	0.047	0.026	0.016	0.007	0.002	0.001	0.001	0.001	
16.00	0.02000	0.985	0.924	0.818	0.705	0.595	0.492	0.323	0.220	0.142	0.095	0.066	0.047	0.026	0.016	0.007	0.002	0.001	0.001	0.001	
32.00	0.01000	0.985	0.928	0.832	0.710	0.594	0.491	0.322	0.220	0.142	0.095	0.066	0.047	0.026	0.016	0.007	0.002	0.001	0.001	0.001	
64.00	0.00500	0.985	0.931	0.821	0.706	0.594	0.491	0.321	0.220	0.142	0.095	0.066	0.047	0.026	0.015	0.007	0.002	0.001	0.001	0.001	
128.00	0.00250	0.985	0.932	0.822	0.707	0.594	0.490	0.320	0.219	0.142	0.095	0.066	0.047	0.026	0.015	0.007	0.002	0.001	0.001	0.001	
256.00	0.00125	0.985	0.932	0.822	0.707	0.594	0.490	0.320	0.219	0.142	0.095	0.066	0.047	0.026	0.015	0.007	0.002	0.001	0.001	0.001	
512.00	0.00062	0.985	0.933	0.823	0.707	0.594	0.490	0.320	0.219	0.142	0.095	0.066	0.047	0.026	0.015	0.007	0.002	0.001	0.001	0.001	

(1-3) Wall half-angle, -20°

Axial distance from slot exit, $\frac{x - \bar{x}}{L}$	Center-plane flux relative to inlet flux, $n(0)/n_1$	Distance from centerplane, $\frac{y}{x - L}$										Distance from centerplane, $\frac{n(y/x - L)}{n(0)}$									
		.1.	.2.	.3.	.4.	.5.	.6.	.8.	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.	Flux relative to centerplane, $n(y/x - L)$	$n(0)$	
0.25	0.45795	0.994	0.974	0.923	0.859	0.786	0.707	0.546	0.401	0.261	0.172	0.117	0.082	0.044	0.026	0.011	0.003	0.001	0.001	0.001	
0.50	0.26963	0.983	0.924	0.850	0.764	0.674	0.586	0.420	0.294	0.178	0.120	0.083	0.059	0.033	0.021	0.009	0.003	0.001	0.001	0.001	
1.00	0.13865	0.986	0.945	0.860	0.759	0.655	0.564	0.349	0.279	0.174	0.117	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
2.00	0.06983	0.985	0.943	0.876	0.765	0.654	0.565	0.376	0.263	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
4.00	0.03498	0.985	0.943	0.879	0.770	0.655	0.572	0.388	0.272	0.178	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
8.00	0.01750	0.985	0.943	0.879	0.770	0.656	0.574	0.375	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
16.00	0.00875	0.985	0.943	0.879	0.770	0.656	0.574	0.374	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
32.00	0.00437	0.985	0.943	0.879	0.770	0.657	0.574	0.374	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
64.00	0.00219	0.985	0.943	0.879	0.770	0.657	0.574	0.374	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
128.00	0.00109	0.985	0.943	0.879	0.770	0.657	0.574	0.374	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
256.00	0.00055	0.985	0.943	0.879	0.770	0.657	0.574	0.374	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	
512.00	0.00027	0.985	0.943	0.879	0.770	0.657	0.574	0.374	0.262	0.172	0.116	0.081	0.058	0.032	0.019	0.009	0.003	0.001	0.001	0.001	

TABLE I. - Continued. CALCULATED ANGULAR DISTRIBUTION OF PARTICLE FLUX AT VARIOUS AXIAL DISTANCES FROM SLOT EXIT

(j) Length to inlet width ratio, 2.00

(j-1) Wall half-angle, -5° (j-2) Wall half-angle, -10°

Axial distance from slot exit, $x - L$	Center-plane flux, $n(O)/n_1$	Distance from centerplane, $\frac{y}{x - L}$										Distance from centerplane, $\frac{y}{x - L}$										Flux relative to centerplane, $\frac{n(y)}{n(0)}$														
		Flux relative to centerplane, $\frac{n(y)}{n(0)}$										Flux relative to centerplane, $\frac{n(y)}{n(0)}$										Flux relative to centerplane, $\frac{n(y)}{n(0)}$														
		.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.	.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.	
0.25	0.49254	0.999	0.994	0.987	0.977	0.964	0.948	0.905	0.847	0.758	0.544	0.336	0.207	0.090	0.046	0.016	0.004	0.002	0.25	0.999	0.994	0.987	0.977	0.964	0.948	0.905	0.847	0.758	0.544	0.336	0.207	0.090	0.046	0.016	0.004	0.002
0.50	0.37201	0.995	0.982	0.960	0.930	0.894	0.851	0.642	0.442	0.262	0.165	0.108	0.074	0.038	0.022	0.009	0.003	0.001	0.50	0.995	0.982	0.960	0.930	0.894	0.851	0.642	0.442	0.262	0.165	0.108	0.074	0.038	0.022	0.009	0.003	0.001
1.00	0.24471	0.992	0.970	0.909	0.797	0.680	0.565	0.364	0.244	0.153	0.100	0.068	0.047	0.025	0.015	0.006	0.002	0.001	1.00	0.992	0.970	0.909	0.797	0.680	0.565	0.364	0.244	0.153	0.100	0.068	0.047	0.025	0.015	0.006	0.002	0.001
2.00	0.14770	0.983	0.978	0.760	0.637	0.407	0.270	0.184	0.117	0.077	0.053	0.037	0.020	0.012	0.005	0.002	0.001	2.00	0.983	0.978	0.760	0.637	0.407	0.270	0.184	0.117	0.077	0.053	0.037	0.020	0.012	0.005	0.002	0.001		
4.00	0.08399	0.908	0.793	0.668	0.562	0.423	0.341	0.228	0.156	0.100	0.066	0.045	0.032	0.018	0.011	0.005	0.001	4.00	0.908	0.793	0.668	0.562	0.423	0.341	0.228	0.156	0.100	0.066	0.045	0.032	0.018	0.011	0.005	0.001		
8.00	0.04246	0.926	0.797	0.659	0.523	0.408	0.331	0.222	0.152	0.098	0.065	0.044	0.032	0.017	0.010	0.005	0.001	8.00	0.926	0.797	0.659	0.523	0.408	0.331	0.222	0.152	0.098	0.065	0.044	0.032	0.017	0.010	0.005	0.001		
16.00	0.02125	0.952	0.808	0.657	0.511	0.402	0.326	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001	16.00	0.952	0.808	0.657	0.511	0.402	0.326	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001		
32.00	0.01062	0.952	0.810	0.657	0.508	0.401	0.326	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001	32.00	0.952	0.810	0.657	0.508	0.401	0.326	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001		
64.00	0.00531	0.957	0.810	0.657	0.507	0.401	0.325	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001	64.00	0.957	0.810	0.657	0.507	0.401	0.325	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001		
128.00	0.00266	0.960	0.812	0.656	0.506	0.401	0.325	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001	128.00	0.960	0.812	0.656	0.506	0.401	0.325	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001		
256.00	0.00133	0.961	0.812	0.656	0.506	0.401	0.325	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001	256.00	0.961	0.812	0.656	0.506	0.401	0.325	0.219	0.150	0.097	0.064	0.044	0.032	0.017	0.010	0.005	0.001		
512.00	0.00066	0.962	0.812	0.656	0.506	0.400	0.325	0.219	0.150	0.096	0.064	0.044	0.032	0.017	0.010	0.005	0.001	512.00	0.962	0.812	0.656	0.506	0.400	0.325	0.219	0.150	0.096	0.064	0.044	0.032	0.017	0.010	0.005	0.001		

(j-2) Wall half-angle, -10°

TABLE I. - Concluded. CALCULATED ANGULAR DISTRIBUTION OF PARTICLE FLUX AT VARIOUS AXIAL DISTANCES FROM SLOT EXIT
 (k) Length to inlet width ratio, 4.00; wall half-angle, -5°

Axial distance from slot exit, $x - L$	Center-plane flux relative to slot exit, $n(0)/n_1$								Distance from centerplane, $\frac{y}{n(0)} / \frac{x - L}{n(0)}$								
	.1	.2	.3	.4	.5	.6	.8	1.	1.25	1.5	1.75	2.	2.5	3.	4.	6.	8.
0.25	0.31449	0.996	0.785	0.966	0.941	0.909	0.872	0.645	0.415	0.252	0.159	0.104	0.071	0.036	0.021	0.008	0.002
0.50	0.21760	0.994	0.975	0.924	0.776	0.523	0.218	0.138	0.061	0.043	0.023	0.013	0.006	0.002	0.001	0.001	0.001
1.00	0.14070	0.992	0.936	0.670	0.517	0.412	0.334	0.223	0.152	0.097	0.064	0.044	0.031	0.017	0.010	0.004	0.001
2.00	0.08694	0.850	0.670	0.501	0.394	0.317	0.258	0.173	0.119	0.076	0.051	0.035	0.025	0.014	0.008	0.004	0.001
4.00	0.04649	0.858	0.534	0.471	0.372	0.300	0.244	0.165	0.113	0.073	0.049	0.033	0.024	0.013	0.008	0.003	0.001
8.00	0.02249	0.884	0.611	0.465	0.368	0.297	0.242	0.164	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001
16.00	0.01125	0.901	0.617	0.462	0.366	0.296	0.241	0.163	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001
32.00	0.00562	0.912	0.616	0.461	0.365	0.295	0.241	0.163	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001
64.00	0.00281	0.917	0.615	0.461	0.365	0.295	0.240	0.162	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001
128.00	0.00141	0.920	0.615	0.460	0.364	0.294	0.240	0.162	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001
256.00	0.00070	0.922	0.614	0.460	0.364	0.294	0.240	0.162	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001
512.00	0.00035	0.922	0.614	0.460	0.364	0.294	0.240	0.162	0.112	0.072	0.048	0.033	0.024	0.013	0.008	0.003	0.001

(a-5) Wall half-angle, 30°

0.64	0.53668	1.005	1.000	1.003	0.996	0.975	0.960	0.942	0.921	0.897	0.870	0.840	0.806	0.768	0.727	0.680	
1.00	0.40333	1.002	1.000	0.995	0.985	0.970	0.952	0.929	0.903	0.877	0.846	0.816	0.787	0.759	0.729	0.692	
2.00	0.23693	0.999	0.982	0.978	0.959	0.934	0.905	0.870	0.832	0.790	0.721	0.635	0.541	0.439	0.329	0.212	0.090
4.00	0.12627	0.997	0.971	0.970	0.947	0.917	0.882	0.843	0.790	0.715	0.634	0.547	0.454	0.357	0.256	0.152	0.023
6.00	0.06433	0.996	0.955	0.966	0.941	0.910	0.873	0.828	0.758	0.681	0.600	0.513	0.422	0.327	0.229	0.129	0.047
16.00	0.01288	0.996	0.946	0.944	0.939	0.907	0.869	0.814	0.743	0.666	0.585	0.498	0.408	0.314	0.217	0.119	0.046
32.00	0.00154	0.998	0.984	0.964	0.958	0.938	0.906	0.868	0.807	0.736	0.659	0.578	0.491	0.408	0.318	0.215	0.046
64.00	0.00082	0.996	0.984	0.964	0.954	0.938	0.905	0.867	0.804	0.733	0.656	0.574	0.488	0.398	0.305	0.209	0.112
128.00	0.00045	0.996	0.984	0.964	0.954	0.937	0.905	0.866	0.803	0.731	0.655	0.573	0.486	0.396	0.303	0.208	0.111
256.00	0.000208	0.996	0.984	0.964	0.954	0.937	0.905	0.866	0.802	0.731	0.655	0.572	0.486	0.396	0.303	0.207	0.111
512.00	0.000104	0.996	0.984	0.964	0.954	0.937	0.905	0.866	0.802	0.730	0.653	0.571	0.485	0.395	0.302	0.207	0.110

(a-6) Wall half-angle, 45°

0.75	0.47854	1.003	1.001	0.995	0.988	0.977	0.963	0.946	0.926	0.902	0.875	0.844	0.808	0.768	0.721	0.667	0.604
1.00	0.39880	1.002	1.000	0.995	0.986	0.973	0.956	0.935	0.910	0.881	0.846	0.807	0.764	0.715	0.663	0.609	0.571
2.00	0.23594	0.999	0.992	0.977	0.957	0.937	0.908	0.873	0.833	0.789	0.740	0.688	0.631	0.520	0.394	0.258	0.172
4.00	0.12490	0.999	0.987	0.971	0.950	0.927	0.891	0.841	0.795	0.744	0.690	0.613	0.510	0.401	0.288	0.170	0.049
8.00	0.06442	0.996	0.985	0.967	0.941	0.917	0.882	0.830	0.778	0.724	0.659	0.563	0.463	0.358	0.249	0.138	0.013
16.00	0.03268	0.996	0.984	0.965	0.943	0.916	0.885	0.830	0.770	0.715	0.637	0.542	0.442	0.339	0.233	0.125	0.029
32.00	0.01645	0.996	0.984	0.964	0.943	0.917	0.893	0.833	0.767	0.711	0.627	0.532	0.433	0.330	0.225	0.118	0.029
64.00	0.00825	0.996	0.984	0.964	0.943	0.916	0.892	0.832	0.765	0.709	0.622	0.527	0.428	0.326	0.222	0.115	0.029
128.00	0.00413	0.996	0.984	0.963	0.943	0.916	0.892	0.832	0.764	0.708	0.620	0.526	0.426	0.324	0.220	0.114	0.029
256.00	0.00207	0.996	0.984	0.963	0.943	0.916	0.892	0.832	0.764	0.708	0.618	0.524	0.425	0.323	0.219	0.113	0.029
512.00	0.00103	0.996	0.984	0.963	0.943	0.916	0.892	0.832	0.764	0.708	0.618	0.523	0.425	0.323	0.218	0.112	0.029

(a-7) Wall half-angle, 60°

0.92	0.40736	1.001	0.999	0.994	0.986	0.976	0.962	0.944	0.923	0.899	0.870	0.836	0.797	0.753	0.702	0.662	0.571
1.00	0.38675	1.001	0.998	0.993	0.984	0.972	0.957	0.938	0.914	0.887	0.855	0.818	0.776	0.731	0.681	0.635	0.549
2.00	0.22889	0.999	0.990	0.980	0.960	0.940	0.912	0.878	0.839	0.794	0.744	0.689	0.639	0.564	0.495	0.383	0.198
4.00	0.12215	0.997	0.988	0.972	0.959	0.932	0.884	0.843	0.796	0.744	0.687	0.626	0.560	0.490	0.370	0.229	0.083
8.00	0.06316	0.997	0.986	0.967	0.942	0.910	0.871	0.827	0.777	0.721	0.661	0.597	0.529	0.435	0.309	0.178	0.064
16.00	0.03208	0.996	0.985	0.965	0.945	0.916	0.866	0.820	0.768	0.711	0.649	0.574	0.514	0.406	0.293	0.158	0.007
32.00	0.01616	0.996	0.984	0.965	0.943	0.916	0.863	0.816	0.764	0.706	0.644	0.577	0.507	0.392	0.271	0.148	0.023
64.00	0.00811	0.996	0.984	0.964	0.943	0.916	0.862	0.814	0.762	0.704	0.641	0.574	0.503	0.386	0.266	0.143	0.020
128.00	0.00406	0.996	0.984	0.964	0.943	0.917	0.861	0.814	0.761	0.702	0.640	0.573	0.500	0.383	0.263	0.141	0.018
256.00	0.00203	0.996	0.984	0.964	0.943	0.916	0.861	0.813	0.760	0.702	0.639	0.572	0.508	0.381	0.262	0.140	0.016
512.00	0.00102	0.996	0.984	0.964	0.943	0.916	0.860	0.813	0.760	0.702	0.639	0.571	0.497	0.381	0.261	0.139	0.017

(a-8) Wall half-angle, 75°

1.42	0.29008	0.999	0.994	0.985	0.972	0.955	0.933	0.908	0.877	0.841	0.800	0.753	0.700	0.640	0.573	0.498	0.415
2.00	0.22032	0.998	0.991	0.980	0.967	0.951	0.923	0.888	0.848	0.802	0.750	0.692	0.648	0.570	0.497	0.418	0.335
4.00	0.11883	0.997	0.988	0.972	0.951	0.936	0.904	0.864	0.823	0.781	0.725	0.664	0.610	0.543	0.332	0.248	0.14
8.00	0.06153	0.997	0.986	0.969	0.944	0.913	0.875	0.831	0.791	0.744	0.684	0.638	0.580	0.453	0.375	0.294	0.156
16.00	0.03128	0.996	0.985	0.967	0.941	0.908	0.869	0.823	0.771	0.714	0.651	0.594	0.544	0.412	0.358	0.276	0.120
32.00	0.01576	0.996	0.985	0.966	0.940	0.916	0.866	0.820	0.767	0.708	0.645	0.577	0.504	0.428	0.349	0.267	0.105
64.00	0.00791	0.996	0.985	0.965	0.940	0.919	0.864	0.817	0.764	0.706	0.642	0.573	0.500	0.424	0.345	0.263	0.097
128.00	0.00396	0.996	0.984	0.965	0.940	0.918	0.864	0.816	0.763	0.704	0.640	0.571	0.500	0.422	0.343	0.261	0.094
256.00	0.00198	0.996	0.984	0.965	0.940	0.918	0.863	0.816	0.763	0.704	0.639	0.571	0.508	0.421	0.342	0.259	0.092
512.00	0.00099	0.996	0.984	0.965	0.940	0.918	0.863	0.816	0.762	0.703	0.639	0.570	0.507	0.421	0.341	0.258	0.091

(b-5) Wall half-angle, 30°

0.79	0.43026	1.007	1.01	1.011	1.008	1.002	0.992	0.979	0.962	0.962	0.962	0.919	0.893	0.864	0.833	0.799	0.763	0.725	0.686
1.00	0.7641	1.005	1.007	1.004	1.006	0.987	0.977	0.954	0.931	0.905	0.876	0.876	0.855	0.811	0.777	0.746	0.716	0.672	0.436
2.00	0.22998	1.001	1.005	0.995	0.984	0.967	0.945	0.919	0.889	0.857	0.822	0.787	0.665	0.671	0.444	0.305	0.154	0.055	0.028
4.00	0.12700	0.998	0.988	0.972	0.950	0.923	0.891	0.856	0.819	0.727	0.628	0.532	0.410	0.291	0.169	0.080	0.048	0.022	
8.00	0.06663	0.957	0.958	0.967	0.942	0.913	0.878	0.841	0.754	0.660	0.561	0.456	0.347	0.234	0.119	0.072	0.044	0.020	
16.00	0.03410	0.916	0.984	0.965	0.939	0.908	0.872	0.812	0.723	0.639	0.530	0.427	0.319	0.209	0.100	0.069	0.042	0.019	
32.00	0.01725	0.916	0.983	0.963	0.937	0.905	0.863	0.798	0.709	0.615	0.516	0.413	0.306	0.197	0.097	0.067	0.041	0.019	
64.00	0.00867	0.996	0.983	0.961	0.936	0.904	0.861	0.791	0.702	0.608	0.509	0.406	0.300	0.192	0.096	0.067	0.041	0.019	
128.00	0.00435	0.936	0.983	0.963	0.936	0.904	0.867	0.787	0.699	0.604	0.506	0.403	0.297	0.189	0.096	0.066	0.041	0.019	
256.00	0.00218	0.936	0.983	0.962	0.936	0.903	0.866	0.786	0.697	0.603	0.504	0.401	0.296	0.188	0.096	0.066	0.041	0.019	
512.00	0.00190	0.936	0.983	0.962	0.936	0.903	0.866	0.785	0.696	0.602	0.503	0.400	0.295	0.187	0.095	0.066	0.041	0.019	

(b-6) Wall half-angle, 45°

1.00	0.35582	1.004	1.005	1.003	0.999	0.989	0.978	0.962	0.944	0.922	0.896	0.867	0.835	0.799	0.759	0.716	0.669	0.620
2.00	0.22112	1.001	1.006	0.996	0.986	0.971	0.951	0.927	0.897	0.863	0.822	0.785	0.761	0.669	0.649	0.597	0.529	0.401
4.00	0.12360	0.998	0.989	0.974	0.952	0.925	0.892	0.855	0.813	0.768	0.720	0.669	0.537	0.395	0.244	0.144	0.088	0.033
8.00	0.06526	0.997	0.986	0.968	0.943	0.911	0.875	0.833	0.787	0.738	0.685	0.544	0.394	0.261	0.163	0.094	0.059	0.020
16.00	0.03351	0.996	0.984	0.965	0.938	0.905	0.866	0.822	0.774	0.723	0.637	0.516	0.390	0.261	0.128	0.066	0.037	0.012
32.00	0.01698	0.996	0.983	0.963	0.936	0.902	0.862	0.817	0.768	0.715	0.614	0.494	0.370	0.242	0.113	0.045	0.026	0.011
64.00	0.00855	0.996	0.983	0.962	0.934	0.900	0.860	0.814	0.765	0.711	0.603	0.484	0.360	0.234	0.108	0.044	0.026	0.011
128.00	0.00429	0.996	0.983	0.962	0.934	0.904	0.869	0.839	0.813	0.763	0.709	0.598	0.478	0.355	0.229	0.102	0.044	0.026
256.00	0.00215	0.996	0.983	0.962	0.934	0.903	0.869	0.838	0.812	0.762	0.708	0.595	0.476	0.353	0.227	0.100	0.044	0.026
512.00	0.00167	0.996	0.983	0.962	0.933	0.903	0.869	0.838	0.812	0.762	0.708	0.594	0.475	0.352	0.226	0.099	0.044	0.026

(b-7) Wall half-angle, 60°

1.35	0.277838	1.001	0.999	0.994	0.986	0.974	0.959	0.940	0.917	0.890	0.859	0.825	0.785	0.741	0.692	0.638	0.578	0.513
2.00	0.21001	1.000	0.999	0.997	0.987	0.974	0.950	0.925	0.907	0.875	0.838	0.797	0.751	0.701	0.664	0.614	0.558	0.528
4.00	0.1832	0.998	0.990	0.976	0.956	0.929	0.898	0.860	0.818	0.771	0.719	0.664	0.604	0.541	0.484	0.444	0.424	0.377
8.00	0.06278	0.997	0.987	0.969	0.945	0.914	0.867	0.835	0.787	0.735	0.678	0.617	0.547	0.473	0.458	0.424	0.386	0.348
16.00	0.03233	0.996	0.985	0.966	0.940	0.907	0.867	0.822	0.772	0.717	0.657	0.594	0.527	0.473	0.401	0.333	0.293	0.253
32.00	0.01640	0.996	0.984	0.964	0.941	0.903	0.862	0.816	0.764	0.708	0.647	0.582	0.514	0.368	0.206	0.144	0.104	0.066
64.00	0.00826	0.996	0.983	0.963	0.943	0.900	0.860	0.813	0.760	0.703	0.641	0.576	0.507	0.353	0.193	0.131	0.091	0.055
128.00	0.00414	0.996	0.983	0.963	0.943	0.903	0.860	0.811	0.758	0.701	0.639	0.573	0.501	0.345	0.186	0.126	0.084	0.055
256.00	0.00208	0.996	0.983	0.963	0.943	0.900	0.858	0.810	0.757	0.700	0.637	0.571	0.501	0.341	0.183	0.125	0.084	0.055
512.00	0.00104	0.996	0.983	0.963	0.943	0.903	0.858	0.810	0.757	0.700	0.637	0.571	0.501	0.340	0.182	0.125	0.084	0.055

(b-8) Wall half-angle, 75°

2.35	0.17638	0.999	0.993	0.993	0.969	0.951	0.928	0.901	0.869	0.832	0.790	0.742	0.689	0.631	0.567	0.496	0.420	0.337
4.00	0.11292	0.998	0.990	0.977	0.952	0.919	0.886	0.843	0.795	0.743	0.685	0.622	0.554	0.483	0.417	0.347	0.207	0.106
8.00	0.06008	0.997	0.987	0.971	0.948	0.919	0.884	0.843	0.796	0.744	0.685	0.622	0.554	0.483	0.417	0.347	0.207	0.106
16.00	0.03099	0.997	0.986	0.968	0.943	0.911	0.883	0.842	0.798	0.745	0.686	0.623	0.555	0.484	0.418	0.348	0.208	0.107
32.00	0.01574	0.996	0.985	0.966	0.940	0.907	0.868	0.822	0.769	0.712	0.649	0.582	0.510	0.435	0.357	0.276	0.166	0.082
64.00	0.00793	0.996	0.985	0.965	0.939	0.905	0.865	0.818	0.765	0.707	0.643	0.575	0.503	0.427	0.349	0.267	0.166	0.082
128.00	0.00398	0.996	0.984	0.965	0.938	0.904	0.863	0.816	0.763	0.704	0.640	0.571	0.502	0.428	0.344	0.263	0.166	0.082
256.00	0.00199	0.996	0.984	0.965	0.938	0.903	0.862	0.815	0.761	0.702	0.638	0.569	0.497	0.420	0.341	0.261	0.166	0.082
512.00	0.00100	0.996	0.984	0.965	0.938	0.903	0.862	0.815	0.761	0.702	0.638	0.569	0.497	0.420	0.341	0.261	0.166	0.082

TABLE III. - Continued. CALCULATED DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS RADIAL DISTANCES FROM SLOT EXIT
 (c) Length to inlet width ratio, 1.00
 (c-1) Wall half-angle, 0°

Radial distance from slot exit, R/W_1	Center-plane flux relative to inlet flux, $n(0)/n_1$	Angle from centerplane, ϕ , deg																
		5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	
Flux relative to centerplane, $n(\phi)/n(0)$																		
0.50	0.49514	1.015	1.025	1.029	1.027	1.021	1.010	0.994	0.974	0.951	0.924	0.895	0.863	0.829	0.793	0.755	0.715	
1.00	0.33747	1.005	1.003	1.003	1.003	1.003	1.003	0.994	0.981	0.965	0.945	0.920	0.890	0.857	0.828	0.799	0.755	0.714
2.00	0.20158	0.599	0.592	0.592	0.592	0.592	0.592	0.591	0.584	0.574	0.567	0.558	0.548	0.538	0.524	0.514	0.503	0.499
4.00	0.11143	0.597	0.595	0.596	0.596	0.596	0.596	0.594	0.584	0.572	0.562	0.552	0.548	0.540	0.530	0.520	0.510	0.500
8.00	0.05887	0.5985	0.5933	0.5933	0.5933	0.5933	0.5933	0.5915	0.5810	0.5799	0.5662	0.5508	0.5494	0.5403	0.528	0.5227	0.5181	0.5139
16.00	0.03031	0.5969	0.5916	0.5916	0.5916	0.5916	0.5916	0.5856	0.5856	0.5856	0.5669	0.5560	0.5469	0.5378	0.5314	0.5264	0.5218	0.5174
32.00	0.01535	0.5961	0.5907	0.5907	0.5907	0.5907	0.5907	0.5846	0.5846	0.5846	0.5628	0.5544	0.5457	0.5366	0.5308	0.5259	0.5214	0.5171
64.00	0.00775	0.5957	0.5902	0.5902	0.5902	0.5902	0.5902	0.5841	0.5841	0.5841	0.5622	0.5538	0.5451	0.5360	0.5256	0.5211	0.5170	0.5130
128.00	0.00389	0.5955	0.5900	0.5900	0.5900	0.5900	0.5900	0.5839	0.5839	0.5839	0.5619	0.5538	0.5448	0.5357	0.5303	0.5255	0.5210	0.5169
256.00	0.00195	0.5954	0.5907	0.5907	0.5907	0.5907	0.5907	0.5838	0.5838	0.5838	0.5617	0.5533	0.5446	0.5354	0.5302	0.5254	0.5210	0.5168
512.00	0.00098	0.5953	0.5909	0.5909	0.5909	0.5909	0.5909	0.5837	0.5837	0.5837	0.5617	0.5533	0.5445	0.5354	0.5302	0.5254	0.5210	0.5168
(c-2) Wall half-angle, 50°																		
0.58	0.46472	1.014	1.024	1.027	1.026	1.020	1.009	0.994	0.975	0.952	0.926	0.897	0.866	0.833	0.798	0.762	0.724	0.684
1.00	0.34743	1.007	1.006	1.000	0.989	0.973	0.954	0.938	0.911	0.884	0.846	0.811	0.781	0.750	0.717	0.680	0.643	0.606
2.00	0.21164	1.000	0.993	0.981	0.966	0.941	0.917	0.893	0.864	0.839	0.801	0.761	0.727	0.693	0.659	0.622	0.580	0.537
4.00	0.11811	0.998	0.998	0.995	0.997	0.989	0.976	0.968	0.950	0.936	0.916	0.893	0.876	0.850	0.826	0.794	0.762	0.731
8.00	0.06269	0.997	0.976	0.956	0.947	0.937	0.915	0.895	0.874	0.853	0.832	0.812	0.792	0.771	0.749	0.726	0.695	0.666
16.00	0.03235	0.996	0.956	0.938	0.923	0.903	0.883	0.862	0.842	0.822	0.802	0.782	0.762	0.742	0.722	0.699	0.675	0.648
32.00	0.01644	0.996	0.945	0.881	0.811	0.755	0.652	0.565	0.474	0.378	0.299	0.250	0.205	0.163	0.125	0.089	0.057	0.027
64.00	0.00829	0.996	0.940	0.876	0.817	0.755	0.646	0.558	0.466	0.371	0.296	0.247	0.203	0.162	0.124	0.089	0.056	0.027
128.00	0.00416	0.995	0.937	0.873	0.813	0.750	0.642	0.555	0.463	0.368	0.294	0.246	0.202	0.161	0.123	0.088	0.056	0.027
256.00	0.00208	0.993	0.936	0.872	0.810	0.748	0.641	0.553	0.461	0.365	0.293	0.245	0.201	0.160	0.123	0.088	0.056	0.027
512.00	0.00104	0.993	0.935	0.871	0.800	0.722	0.640	0.552	0.460	0.365	0.293	0.245	0.201	0.160	0.123	0.088	0.056	0.027
(c-3) Wall half-angle, 100°																		
0.68	0.42800	1.013	1.022	1.025	1.023	1.017	1.006	0.992	0.973	0.951	0.926	0.898	0.867	0.835	0.801	0.766	0.730	0.692
1.00	0.35084	1.008	1.010	1.007	1.000	0.998	0.984	0.967	0.946	0.923	0.899	0.876	0.842	0.812	0.781	0.740	0.709	0.680
2.00	0.18707	1.001	0.998	0.984	0.968	0.948	0.928	0.851	0.787	0.724	0.674	0.621	0.571	0.520	0.470	0.427	0.386	0.346
4.00	0.06347	1.000	0.998	0.995	0.975	0.957	0.937	0.883	0.802	0.715	0.621	0.551	0.474	0.404	0.336	0.275	0.217	0.179
8.00	0.06591	0.997	0.977	0.957	0.927	0.901	0.872	0.812	0.737	0.667	0.551	0.449	0.344	0.259	0.210	0.165	0.126	0.098
16.00	0.03410	0.996	0.986	0.956	0.926	0.892	0.821	0.750	0.689	0.613	0.516	0.415	0.310	0.245	0.199	0.157	0.119	0.084
32.00	0.01735	0.996	0.985	0.952	0.887	0.776	0.689	0.620	0.568	0.500	0.439	0.398	0.323	0.238	0.194	0.153	0.116	0.083
64.00	0.00876	0.996	0.985	0.952	0.885	0.775	0.680	0.610	0.550	0.490	0.435	0.385	0.325	0.259	0.202	0.161	0.121	0.082
128.00	0.00444	0.996	0.985	0.952	0.886	0.776	0.687	0.616	0.567	0.503	0.446	0.386	0.323	0.262	0.203	0.160	0.124	0.081
256.00	0.00220	0.996	0.985	0.952	0.884	0.773	0.682	0.612	0.567	0.501	0.447	0.387	0.323	0.261	0.201	0.160	0.124	0.081
512.00	0.00110	0.996	0.985	0.952	0.883	0.771	0.680	0.611	0.566	0.500	0.446	0.386	0.323	0.260	0.200	0.160	0.124	0.081
(c-4) Wall half-angle, 200°																		
0.86	0.36840	1.011	1.018	1.020	1.017	1.011	1.000	0.985	0.967	0.945	0.921	0.893	0.864	0.832	0.799	0.765	0.731	0.697
1.00	0.34186	1.009	1.014	1.014	1.014	1.009	1.000	0.986	0.968	0.947	0.923	0.896	0.868	0.838	0.810	0.784	0.753	0.716
2.00	0.22071	1.003	0.999	0.997	0.995	0.954	0.932	0.909	0.885	0.842	0.733	0.612	0.476	0.324	0.191	0.129	0.077	0.034
4.00	0.127C1	0.599	0.990	0.975	0.955	0.930	0.910	0.850	0.732	0.620	0.502	0.376	0.217	0.143	0.074	0.034	0.025	0.012
8.00	0.06845	0.597	0.986	0.984	0.986	0.944	0.889	0.856	0.817	0.771	0.668	0.547	0.445	0.330	0.217	0.143	0.072	0.045
16.00	0.03558	0.596	0.984	0.986	0.986	0.942	0.887	0.853	0.819	0.775	0.666	0.548	0.445	0.335	0.218	0.140	0.071	0.044
32.00	0.01815	0.595	0.985	0.986	0.986	0.941	0.887	0.853	0.819	0.775	0.666	0.548	0.445	0.335	0.218	0.140	0.071	0.044
64.00	0.00917	0.595	0.983	0.984	0.984	0.940	0.887	0.853	0.819	0.775	0.666	0.548	0.445	0.335	0.218	0.140	0.071	0.044
128.00	0.00464	0.595	0.983	0.984	0.984	0.940	0.887	0.853	0.819	0.775	0.666	0.548	0.445	0.335	0.218	0.140	0.071	0.044
256.00	0.00231	0.595	0.983	0.984	0.984	0.940	0.887	0.853	0.819	0.775	0.666	0.548	0.445	0.335	0.218	0.140	0.071	0.044
512.00	0.00116	0.595	0.982	0.983	0.983	0.940	0.887	0.853	0.819	0.775	0.666	0.548	0.445	0.335	0.218	0.140	0.071	0.044

(c-5) Wall half-angle, 30°

1.08	0.30965	1.008	1.013	1.010	1.002	0.991	0.976	0.957	0.935	0.911	0.883	0.854	0.822	0.789	0.755	0.721	0.688	
2.00	0.21386	1.003	1.001	0.993	0.980	0.963	0.941	0.916	0.889	0.860	0.831	0.805	0.728	0.556	0.356	0.143	0.080	
4.00	0.12540	0.999	0.981	0.977	0.957	0.933	0.905	0.876	0.845	0.788	0.653	0.508	0.353	0.188	0.117	0.078	0.046	
8.00	0.06828	0.997	0.986	0.984	0.965	0.946	0.918	0.887	0.854	0.764	0.636	0.501	0.359	0.212	0.131	0.094	0.064	
16.00	0.03567	0.996	0.997	0.986	0.966	0.947	0.910	0.877	0.847	0.770	0.727	0.660	0.594	0.524	0.450	0.373	0.293	0.205
32.00	0.01824	0.996	0.995	0.984	0.963	0.942	0.936	0.906	0.872	0.840	0.794	0.756	0.719	0.686	0.659	0.606	0.536	0.417
64.00	0.00922	0.995	0.995	0.982	0.961	0.941	0.903	0.869	0.835	0.767	0.644	0.516	0.384	0.249	0.147	0.111	0.081	0.056
128.00	0.00464	0.995	0.995	0.982	0.961	0.941	0.902	0.867	0.835	0.759	0.636	0.508	0.376	0.245	0.145	0.110	0.081	0.055
256.00	0.00233	0.995	0.995	0.982	0.961	0.941	0.902	0.867	0.835	0.759	0.632	0.504	0.372	0.248	0.145	0.110	0.081	0.055
512.00	0.00116	0.995	0.995	0.982	0.960	0.940	0.901	0.866	0.835	0.759	0.630	0.502	0.370	0.246	0.144	0.109	0.080	0.055

(c-6) Wall half-angle, 45°

1.00	0.23473	1.005	1.006	1.003	0.998	0.988	0.975	0.958	0.939	0.915	0.889	0.860	0.828	0.794	0.756	0.721	0.682
2.00	0.19683	1.003	1.002	0.996	0.987	0.973	0.955	0.933	0.907	0.878	0.846	0.811	0.775	0.738	0.702	0.670	0.640
4.00	0.11811	1.001	0.993	0.981	0.962	0.947	0.911	0.879	0.843	0.812	0.781	0.744	0.704	0.663	0.627	0.597	0.567
8.00	0.06510	0.997	0.988	0.971	0.947	0.918	0.884	0.847	0.805	0.765	0.724	0.683	0.644	0.607	0.577	0.547	0.517
16.00	0.03423	0.996	0.996	0.985	0.965	0.949	0.910	0.870	0.838	0.794	0.756	0.715	0.675	0.635	0.597	0.566	0.536
32.00	0.01756	0.996	0.998	0.983	0.962	0.945	0.901	0.862	0.830	0.797	0.759	0.722	0.682	0.642	0.602	0.573	0.543
64.00	0.00889	0.996	0.998	0.982	0.961	0.941	0.903	0.868	0.838	0.795	0.756	0.726	0.686	0.646	0.606	0.576	0.546
128.00	0.00448	0.995	0.998	0.982	0.960	0.940	0.901	0.868	0.838	0.794	0.755	0.727	0.687	0.647	0.607	0.577	0.547
256.00	0.00224	0.995	0.995	0.982	0.960	0.940	0.901	0.868	0.838	0.794	0.755	0.728	0.689	0.648	0.608	0.578	0.548
512.00	0.00112	0.995	0.995	0.982	0.960	0.940	0.901	0.868	0.838	0.794	0.755	0.728	0.689	0.648	0.608	0.578	0.548

(c-7) Wall half-angle, 60°

2.20	0.16930	1.001	0.999	0.994	0.985	0.972	0.956	0.936	0.913	0.886	0.855	0.821	0.784	0.743	0.698	0.650	0.599	0.544
4.00	0.10928	0.999	0.996	0.983	0.967	0.947	0.921	0.891	0.857	0.818	0.775	0.728	0.679	0.626	0.571	0.513	0.460	0.410
8.00	0.06035	0.998	0.973	0.952	0.924	0.891	0.853	0.810	0.761	0.724	0.671	0.624	0.574	0.524	0.474	0.424	0.374	0.324
16.00	0.03216	0.997	0.966	0.968	0.943	0.911	0.874	0.831	0.783	0.730	0.674	0.621	0.571	0.521	0.471	0.421	0.371	0.321
32.00	0.01654	0.996	0.984	0.965	0.938	0.904	0.864	0.819	0.768	0.713	0.654	0.602	0.552	0.506	0.456	0.406	0.356	0.306
64.00	0.00839	0.996	0.984	0.963	0.935	0.900	0.859	0.813	0.761	0.704	0.644	0.591	0.541	0.494	0.444	0.394	0.344	0.294
128.00	0.00422	0.996	0.993	0.962	0.934	0.909	0.859	0.827	0.777	0.709	0.639	0.574	0.527	0.477	0.427	0.377	0.327	0.277
256.00	0.00212	0.996	0.993	0.962	0.933	0.903	0.858	0.826	0.775	0.709	0.637	0.572	0.522	0.472	0.422	0.372	0.322	0.272
512.00	0.00106	0.996	0.996	0.983	0.962	0.933	0.897	0.855	0.827	0.774	0.709	0.637	0.572	0.521	0.471	0.421	0.371	0.321

(c-8) Wall half-angle, 75°

4.20	0.09826	0.999	0.983	0.969	0.950	0.927	0.899	0.867	0.830	0.788	0.742	0.690	0.634	0.572	0.505	0.432	0.354
8.00	0.05662	0.998	0.989	0.976	0.956	0.931	0.901	0.864	0.833	0.790	0.745	0.682	0.629	0.568	0.505	0.432	0.354
16.00	0.03023	0.997	0.987	0.970	0.947	0.918	0.882	0.841	0.809	0.773	0.729	0.662	0.619	0.552	0.481	0.418	0.354
32.00	0.01557	0.996	0.986	0.967	0.942	0.910	0.872	0.837	0.807	0.777	0.727	0.660	0.610	0.549	0.479	0.417	0.354
64.00	0.00791	0.996	0.985	0.966	0.940	0.909	0.870	0.839	0.807	0.778	0.726	0.668	0.618	0.550	0.481	0.419	0.354
128.00	0.00398	0.996	0.984	0.965	0.938	0.905	0.864	0.831	0.800	0.774	0.724	0.664	0.614	0.554	0.484	0.420	0.357
256.00	0.00200	0.996	0.984	0.965	0.937	0.903	0.862	0.830	0.800	0.774	0.724	0.664	0.614	0.554	0.484	0.420	0.357
512.00	0.00100	0.996	0.984	0.965	0.937	0.903	0.862	0.830	0.800	0.774	0.724	0.664	0.614	0.554	0.484	0.420	0.357

(d-5) Wall half-angle, 30°

1.00	0.19996	1.008	1.012	1.011	1.006	0.997	0.983	0.966	0.946	0.923	0.897	0.869	0.839	0.808	0.776	0.744	0.712	0.683
2.00	0.18195	1.007	1.009	1.006	1.006	0.998	0.986	0.968	0.949	0.920	0.892	0.867	0.837	0.807	0.772	0.738	0.708	0.698
4.00	0.1732	1.001	0.996	0.986	0.979	0.973	0.952	0.928	0.901	0.874	0.847	0.819	0.789	0.753	0.723	0.698	0.671	0.621
8.00	0.06800	0.988	0.989	0.988	0.986	0.980	0.952	0.928	0.901	0.874	0.847	0.819	0.789	0.753	0.723	0.698	0.671	0.621
16.00	0.03689	0.997	0.985	0.966	0.942	0.915	0.886	0.856	0.875	0.847	0.819	0.789	0.753	0.723	0.698	0.671	0.621	0.573
32.00	0.01926	0.936	0.936	0.962	0.937	0.908	0.877	0.774	0.844	0.816	0.788	0.750	0.722	0.694	0.666	0.636	0.597	0.534
64.00	0.00985	0.935	0.936	0.981	0.960	0.934	0.904	0.812	0.730	0.549	0.346	0.199	0.153	0.117	0.088	0.064	0.043	0.027
128.00	0.00498	0.995	0.995	0.959	0.959	0.932	0.901	0.869	0.708	0.518	0.325	0.194	0.149	0.114	0.086	0.062	0.043	0.026
256.00	0.00251	0.995	0.995	0.959	0.959	0.931	0.900	0.867	0.697	0.505	0.315	0.192	0.148	0.113	0.085	0.062	0.042	0.026
512.00	0.00126	0.935	0.980	0.958	0.958	0.931	0.900	0.867	0.691	0.502	0.310	0.190	0.147	0.113	0.085	0.062	0.042	0.026

(d-6) Wall half-angle, 45°

2.50	0.13987	1.004	1.005	1.001	0.994	0.983	0.969	0.951	0.931	0.907	0.881	0.853	0.823	0.791	0.759	0.727	0.695	0.664
4.00	0.10466	1.002	0.999	0.999	0.991	0.978	0.961	0.940	0.915	0.888	0.858	0.826	0.793	0.761	0.730	0.702	0.671	0.620
8.00	0.06207	0.999	0.999	0.991	0.977	0.956	0.932	0.903	0.871	0.836	0.802	0.762	0.724	0.696	0.666	0.637	0.602	0.560
16.00	0.03409	0.997	0.986	0.986	0.964	0.944	0.916	0.880	0.842	0.802	0.760	0.711	0.684	0.655	0.625	0.595	0.566	0.520
32.00	0.01791	0.996	0.984	0.983	0.964	0.936	0.904	0.886	0.825	0.781	0.736	0.607	0.531	0.496	0.457	0.420	0.384	0.348
64.00	0.00919	0.996	0.996	0.962	0.932	0.898	0.859	0.816	0.770	0.720	0.526	0.257	0.098	0.067	0.045	0.028	0.016	0.007
128.00	0.00464	0.995	0.995	0.981	0.959	0.930	0.895	0.855	0.811	0.764	0.715	0.487	0.222	0.094	0.064	0.043	0.028	0.016
256.00	0.00234	0.995	0.995	0.981	0.959	0.929	0.893	0.852	0.808	0.761	0.711	0.468	0.205	0.092	0.063	0.043	0.027	0.016
512.00	0.00118	0.995	0.981	0.958	0.958	0.931	0.892	0.851	0.807	0.759	0.709	0.459	0.196	0.091	0.063	0.042	0.027	0.016

(d-7) Wall half-angle, 60°

3.50	0.09472	1.001	0.998	0.992	0.983	0.969	0.953	0.933	0.909	0.883	0.853	0.821	0.786	0.748	0.707	0.665	0.620	0.573
4.00	0.09316	1.001	0.998	0.992	0.981	0.964	0.942	0.915	0.884	0.849	0.810	0.767	0.722	0.673	0.632	0.591	0.551	0.513
8.00	0.05601	0.999	0.992	0.981	0.962	0.937	0.901	0.872	0.848	0.816	0.780	0.744	0.708	0.654	0.613	0.568	0.513	0.466
16.00	0.03104	0.997	0.996	0.992	0.981	0.955	0.921	0.888	0.849	0.806	0.759	0.722	0.673	0.622	0.569	0.523	0.473	0.423
32.00	0.01639	0.996	0.996	0.995	0.995	0.967	0.941	0.909	0.871	0.834	0.782	0.742	0.692	0.643	0.597	0.547	0.501	0.454
64.00	0.00843	0.996	0.996	0.996	0.996	0.964	0.936	0.902	0.862	0.816	0.766	0.711	0.653	0.591	0.537	0.486	0.439	0.390
128.00	0.00428	0.996	0.996	0.996	0.996	0.963	0.934	0.898	0.854	0.810	0.758	0.702	0.642	0.579	0.514	0.468	0.419	0.371
256.00	0.00215	0.996	0.996	0.993	0.996	0.961	0.932	0.897	0.854	0.807	0.754	0.697	0.637	0.573	0.506	0.456	0.408	0.359
512.00	0.00108	0.996	0.982	0.961	0.961	0.932	0.896	0.853	0.805	0.752	0.695	0.634	0.570	0.489	0.416	0.358	0.310	0.263

(d-8) Wall half-angle, 75°

7.00	0.05199	0.998	0.993	0.982	0.968	0.949	0.926	0.899	0.867	0.830	0.790	0.744	0.694	0.639	0.579	0.514	0.444	0.368
8.00	0.05147	0.998	0.992	0.982	0.968	0.949	0.926	0.898	0.866	0.829	0.788	0.742	0.692	0.637	0.576	0.511	0.444	0.364
16.00	0.02864	0.997	0.989	0.975	0.955	0.930	0.899	0.863	0.821	0.772	0.722	0.665	0.603	0.531	0.467	0.392	0.312	0.202
32.00	0.01517	0.997	0.987	0.970	0.947	0.917	0.881	0.840	0.792	0.739	0.681	0.619	0.551	0.480	0.405	0.326	0.207	0.091
64.00	0.00781	0.996	0.987	0.967	0.942	0.910	0.871	0.827	0.776	0.720	0.659	0.593	0.523	0.450	0.373	0.293	0.204	0.091
128.00	0.00397	0.996	0.996	0.996	0.996	0.965	0.939	0.906	0.866	0.820	0.768	0.710	0.647	0.580	0.509	0.434	0.326	0.193
256.00	0.00200	0.996	0.986	0.995	0.995	0.963	0.934	0.894	0.853	0.805	0.757	0.705	0.641	0.573	0.501	0.426	0.327	0.193
512.00	0.00100	0.996	0.984	0.965	0.965	0.933	0.904	0.863	0.821	0.774	0.721	0.667	0.608	0.536	0.467	0.376	0.276	0.193

(e-5) Wall half-angle, 30°

2.82	0.11766	1.007	1.009	1.007	1.000	0.989	0.971	0.955	0.931	0.909	0.882	0.854	0.824	0.794	0.763	0.732	0.702	0.673
4.00	0.09860	1.004	1.003	0.997	0.986	0.971	0.953	0.931	0.908	0.884	0.859	0.836	0.815	0.780	0.752	0.722	0.697	0.637
8.00	0.06305	1.000	0.981	0.980	0.971	0.964	0.921	0.925	0.900	0.876	0.856	0.836	0.816	0.788	0.750	0.719	0.682	0.614
16.00	0.03653	0.988	0.988	0.987	0.971	0.950	0.925	0.900	0.876	0.856	0.836	0.816	0.792	0.754	0.717	0.685	0.641	0.594
32.00	0.01985	0.936	0.984	0.964	0.940	0.914	0.886	0.829	0.505	0.242	0.174	0.130	0.098	0.072	0.052	0.035	0.021	0.010
64.00	0.01038	0.995	0.981	0.961	0.940	0.914	0.886	0.829	0.505	0.242	0.174	0.130	0.098	0.072	0.052	0.035	0.021	0.010
128.00	0.00531	0.995	0.980	0.958	0.932	0.902	0.877	0.626	0.307	0.198	0.148	0.113	0.086	0.065	0.047	0.032	0.019	0.009
256.00	0.00269	0.995	0.980	0.957	0.930	0.900	0.869	0.593	0.275	0.192	0.145	0.110	0.084	0.063	0.046	0.031	0.019	0.009
512.00	0.00135	0.994	0.979	0.951	0.929	0.899	0.867	0.577	0.263	0.190	0.143	0.109	0.084	0.063	0.046	0.031	0.019	0.009

(e-6) Wall half-angle, 45°

4.50	0.07744	1.003	1.002	0.998	0.989	0.977	0.962	0.944	0.922	0.899	0.874	0.847	0.818	0.790	0.761	0.732	0.705	0.680
8.00	0.05440	1.001	0.996	0.986	0.972	0.954	0.932	0.901	0.876	0.851	0.821	0.791	0.763	0.736	0.706	0.669	0.635	0.612
16.00	0.03219	0.998	0.989	0.979	0.954	0.975	0.950	0.929	0.900	0.868	0.834	0.799	0.764	0.728	0.696	0.654	0.631	0.617
32.00	0.01769	0.997	0.985	0.967	0.942	0.942	0.912	0.878	0.840	0.801	0.761	0.719	0.684	0.637	0.607	0.570	0.535	0.507
64.00	0.00930	0.996	0.983	0.962	0.942	0.934	0.901	0.864	0.823	0.780	0.746	0.509	0.127	0.079	0.051	0.034	0.021	0.005
128.00	0.00477	0.995	0.981	0.959	0.930	0.895	0.856	0.813	0.769	0.722	0.382	0.112	0.072	0.048	0.032	0.011	0.005	0.005
256.00	0.00242	0.995	0.981	0.958	0.928	0.892	0.852	0.808	0.762	0.715	0.322	0.106	0.069	0.046	0.031	0.011	0.005	0.005
512.00	0.00122	0.995	0.980	0.957	0.927	0.890	0.850	0.850	0.759	0.711	0.292	0.103	0.067	0.045	0.030	0.019	0.011	0.005

(e-7) Wall half-angle, 60°

7.30	0.05032	1.000	0.397	0.990	0.980	0.966	0.943	0.929	0.906	0.881	0.852	0.821	0.788	0.753	0.716	0.677	0.636	0.594
8.00	0.04739	1.000	0.996	0.989	0.978	0.963	0.945	0.924	0.900	0.872	0.842	0.812	0.774	0.737	0.698	0.657	0.615	0.573
16.00	0.02840	0.998	0.991	0.979	0.961	0.940	0.912	0.881	0.846	0.807	0.765	0.720	0.673	0.623	0.571	0.522	0.484	0.444
32.00	0.01573	0.997	0.987	0.971	0.948	0.966	0.940	0.920	0.885	0.847	0.804	0.755	0.707	0.654	0.598	0.546	0.507	0.462
64.00	0.00831	0.996	0.985	0.965	0.940	0.971	0.940	0.907	0.869	0.826	0.778	0.727	0.671	0.613	0.552	0.484	0.426	0.366
128.00	0.00427	0.996	0.983	0.963	0.935	0.901	0.880	0.841	0.764	0.709	0.651	0.590	0.527	0.488	0.422	0.361	0.305	0.262
256.00	0.00217	0.996	0.981	0.961	0.923	0.897	0.855	0.809	0.756	0.700	0.641	0.579	0.514	0.462	0.402	0.341	0.285	0.242
512.00	0.00109	0.996	0.982	0.961	0.931	0.895	0.851	0.805	0.752	0.696	0.636	0.573	0.501	0.440	0.389	0.330	0.270	0.227

(e-8) Wall half-angle, 75°

15.36	0.02676	0.998	0.992	0.982	0.968	0.949	0.926	0.899	0.867	0.831	0.791	0.766	0.697	0.643	0.584	0.520	0.451	0.377
16.00	0.02582	0.998	0.992	0.982	0.967	0.948	0.924	0.896	0.864	0.827	0.786	0.750	0.690	0.645	0.575	0.510	0.460	0.365
32.00	0.01435	0.997	0.989	0.975	0.955	0.929	0.898	0.862	0.820	0.773	0.721	0.665	0.603	0.537	0.467	0.392	0.313	0.261
64.00	0.00760	0.997	0.987	0.970	0.947	0.917	0.881	0.839	0.792	0.739	0.681	0.638	0.581	0.480	0.405	0.326	0.264	0.201
128.00	0.00391	0.998	0.985	0.967	0.942	0.910	0.871	0.826	0.775	0.720	0.659	0.593	0.523	0.449	0.373	0.293	0.202	0.160
256.00	0.00199	0.996	0.985	0.966	0.939	0.906	0.866	0.819	0.767	0.709	0.647	0.580	0.509	0.434	0.356	0.276	0.200	0.160
512.00	0.00100	0.996	0.984	0.965	0.938	0.904	0.863	0.816	0.763	0.704	0.641	0.573	0.501	0.426	0.348	0.267	0.202	0.160

TABLE II. - Continued. CALCULATED DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS RADIAL DISTANCES FROM SLOT EXIT^a

(f) Length to inlet width ratio, 8.00

(f-1) Wall half-angle, 0°

Radial distance from slot exit, R/W_1	Center-plane flux relative to inlet, $n(0)/n_1$	Angle from centerplane, φ , deg											
		5	10	15	20	25	30	35	40	45	50	55	60
Flux relative to centerplane, $n(\varphi)/n(0)$													
0.50	0.21073	1.016	1.024	1.025	1.019	1.006	0.998	0.964	0.936	0.903	0.867	0.827	0.738
1.00	0.15834	1.008	1.003	0.993	0.977	0.957	0.936	0.745	0.583	0.487	0.413	0.350	0.292
2.00	0.10939	1.000	0.994	0.960	0.927	0.546	0.450	0.382	0.327	0.281	0.240	0.202	0.167
4.00	0.07141	0.998	0.846	0.582	0.367	0.246	0.269	0.232	0.200	0.171	0.144	0.119	0.096
8.00	0.06398	0.915	0.614	0.427	0.341	0.285	0.244	0.211	0.183	0.158	0.135	0.114	0.094
16.00	0.02546	0.794	0.489	0.356	0.287	0.242	0.208	0.180	0.156	0.135	0.115	0.097	0.081
32.00	0.01396	0.724	0.333	0.320	0.259	0.218	0.188	0.163	0.141	0.122	0.105	0.088	0.073
64.00	0.00736	0.686	0.406	0.301	0.244	0.206	0.177	0.154	0.134	0.116	0.099	0.084	0.069
128.00	0.00379	0.666	0.392	0.291	0.237	0.200	0.172	0.149	0.130	0.112	0.096	0.081	0.067
256.00	0.00192	0.626	0.285	0.287	0.273	0.197	0.169	0.147	0.128	0.110	0.095	0.080	0.064
512.00	0.00097	0.651	0.382	0.284	0.231	0.195	0.168	0.146	0.127	0.109	0.094	0.080	0.069

Radial distance from slot exit, R/W_1	Center-plane flux relative to inlet, $n(0)/n_1$	Angle from centerplane, φ , deg											
		5	10	15	20	25	30	35	40	45	50	55	60
Flux relative to centerplane, $n(\varphi)/n(0)$													
1.14	0.16675	1.014	1.020	1.020	1.013	1.001	0.983	0.960	0.933	0.901	0.866	0.828	0.786
2.00	0.13277	1.007	1.005	0.997	0.983	0.965	0.944	0.922	0.867	0.829	0.780	0.740	0.695
4.00	0.09144	1.001	0.973	0.984	0.977	0.955	0.935	0.912	0.867	0.829	0.780	0.740	0.695
8.00	0.05820	0.998	0.992	0.853	0.855	0.416	0.328	0.284	0.241	0.205	0.173	0.144	0.118
16.00	0.03447	0.957	0.907	0.582	0.405	0.323	0.233	0.268	0.227	0.194	0.160	0.141	0.118
32.00	0.01919	0.997	0.697	0.688	0.466	0.346	0.280	0.235	0.200	0.171	0.146	0.124	0.104
64.00	0.01021	0.997	0.692	0.422	0.319	0.259	0.218	0.186	0.159	0.136	0.116	0.097	0.080
128.00	0.00528	0.997	0.653	0.401	0.305	0.249	0.210	0.179	0.154	0.131	0.112	0.094	0.077
256.00	0.00269	0.985	0.533	0.391	0.298	0.244	0.205	0.175	0.151	0.126	0.104	0.082	0.062
512.00	0.00136	0.976	0.623	0.386	0.295	0.241	0.203	0.174	0.149	0.128	0.109	0.091	0.075

(f-2) Wall half-angle, 50°

Radial distance from slot exit, R/W_1	Center-plane flux relative to inlet, $n(0)/n_1$	Angle from centerplane, φ , deg											
		5	10	15	20	25	30	35	40	45	50	55	60
Flux relative to centerplane, $n(\varphi)/n(0)$													
1.14	0.16675	1.014	1.020	1.020	1.013	1.001	0.983	0.960	0.933	0.901	0.866	0.828	0.786
2.00	0.13277	1.007	1.005	0.997	0.983	0.965	0.944	0.922	0.867	0.829	0.780	0.740	0.695
4.00	0.09144	1.001	0.973	0.984	0.977	0.955	0.935	0.912	0.867	0.829	0.780	0.740	0.695
8.00	0.05820	0.998	0.992	0.853	0.855	0.416	0.328	0.284	0.241	0.205	0.173	0.144	0.118
16.00	0.03447	0.957	0.907	0.582	0.405	0.323	0.233	0.268	0.227	0.194	0.160	0.141	0.118
32.00	0.01919	0.997	0.697	0.688	0.466	0.346	0.280	0.235	0.200	0.171	0.146	0.124	0.104
64.00	0.01021	0.997	0.692	0.422	0.319	0.259	0.218	0.186	0.159	0.136	0.116	0.097	0.080
128.00	0.00528	0.997	0.653	0.401	0.305	0.249	0.210	0.179	0.154	0.131	0.112	0.094	0.077
256.00	0.00269	0.985	0.533	0.391	0.298	0.244	0.205	0.175	0.151	0.126	0.104	0.082	0.062
512.00	0.00136	0.976	0.623	0.386	0.295	0.241	0.203	0.174	0.149	0.128	0.109	0.091	0.075

(f-3) Wall half-angle, 10°

Radial distance from slot exit, R/W_1	Center-plane flux relative to inlet, $n(0)/n_1$	Angle from centerplane, φ , deg											
		5	10	15	20	25	30	35	40	45	50	55	60
Flux relative to centerplane, $n(\varphi)/n(0)$													
1.94	0.13074	1.012	1.017	1.015	1.008	0.996	0.978	0.956	0.930	0.900	0.867	0.831	0.793
2.00	0.12934	1.011	1.016	1.014	1.006	0.994	0.976	0.953	0.927	0.897	0.864	0.829	0.791
4.00	0.09489	1.004	1.001	0.991	0.970	0.943	0.926	0.886	0.836	0.782	0.742	0.709	0.670
8.00	0.06251	1.000	0.993	0.982	0.970	0.897	0.855	0.834	0.804	0.754	0.720	0.682	0.642
16.00	0.03177	0.998	0.989	0.980	0.979	0.879	0.847	0.817	0.787	0.737	0.700	0.662	0.622
32.00	0.01217	0.996	0.986	0.977	0.968	0.881	0.854	0.826	0.796	0.746	0.709	0.672	0.634
64.00	0.001139	0.996	0.986	0.974	0.960	0.874	0.843	0.816	0.786	0.736	0.699	0.662	0.622
128.00	0.000591	0.995	0.985	0.973	0.955	0.868	0.839	0.809	0.780	0.730	0.693	0.656	0.617
256.00	0.000161	0.995	0.985	0.973	0.955	0.868	0.839	0.809	0.780	0.730	0.693	0.656	0.617
512.00	0.000152	0.995	0.985	0.973	0.955	0.868	0.839	0.809	0.780	0.730	0.693	0.656	0.617

(f-4) Wall half-angle, 20°

3.38	0.09128	1.008	1.011	1.009	1.000	0.988	0.971	0.950	0.926	0.899	0.869	0.837	0.804	0.768	0.731	0.693	0.653	0.611
4.00	0.08522	1.007	1.008	1.003	0.994	0.979	0.961	0.940	0.916	0.890	0.862	0.834	0.806	0.779	0.755	0.724	0.690	0.650
8.00	0.05927	1.002	0.986	0.977	0.955	0.937	0.920	0.907	0.877	0.840	0.811	0.782	0.751	0.722	0.691	0.660	0.631	0.601
16.00	0.03690	0.998	0.990	0.976	0.960	0.945	0.932	0.920	0.900	0.876	0.851	0.824	0.795	0.766	0.737	0.707	0.677	0.647
32.00	0.02113	0.997	0.955	0.970	0.953	0.938	0.922	0.906	0.886	0.860	0.834	0.806	0.777	0.748	0.719	0.689	0.659	0.629
64.00	0.01142	0.995	0.983	0.966	0.948	0.930	0.912	0.893	0.874	0.850	0.824	0.795	0.766	0.737	0.707	0.677	0.647	0.617
128.00	0.00595	0.995	0.981	0.963	0.944	0.931	0.915	0.896	0.877	0.852	0.826	0.797	0.768	0.739	0.709	0.679	0.649	0.619
256.00	0.00304	0.994	0.980	0.961	0.942	0.932	0.914	0.895	0.876	0.851	0.825	0.796	0.767	0.738	0.708	0.678	0.648	0.618
512.00	0.00154	0.994	0.980	0.961	0.941	0.931	0.912	0.893	0.874	0.850	0.824	0.795	0.766	0.737	0.707	0.677	0.647	0.617

(f-5) Wall half-angle, 30°

5.14	0.06474	1.005	1.006	1.002	0.993	0.980	0.964	0.944	0.922	0.897	0.870	0.842	0.813	0.783	0.753	0.723	0.693	0.663
8.00	0.05197	1.003	1.004	1.000	0.992	0.979	0.961	0.941	0.920	0.890	0.864	0.837	0.809	0.779	0.750	0.720	0.690	0.660
16.00	0.03329	0.999	0.992	0.979	0.957	0.939	0.920	0.899	0.879	0.850	0.824	0.795	0.766	0.737	0.707	0.677	0.647	0.617
32.00	0.01937	0.997	0.986	0.969	0.948	0.925	0.901	0.879	0.849	0.820	0.791	0.762	0.733	0.703	0.673	0.643	0.613	0.583
64.00	0.01055	0.996	0.983	0.963	0.941	0.913	0.887	0.863	0.834	0.805	0.776	0.747	0.718	0.688	0.658	0.628	0.598	0.568
128.00	0.00553	0.995	0.980	0.959	0.938	0.905	0.881	0.853	0.824	0.795	0.766	0.737	0.708	0.678	0.648	0.618	0.588	0.558
256.00	0.00283	0.995	0.979	0.957	0.930	0.901	0.872	0.842	0.813	0.784	0.755	0.726	0.697	0.667	0.637	0.607	0.577	0.547
512.00	0.00143	0.994	0.979	0.956	0.928	0.898	0.869	0.831	0.802	0.773	0.744	0.715	0.686	0.656	0.626	0.596	0.566	0.536

(f-6) Wall half-angle, 45°

8.50	0.04092	1.002	1.000	0.994	0.985	0.957	0.927	0.906	0.877	0.847	0.818	0.789	0.760	0.731	0.701	0.671	0.641	0.611
16.00	0.02785	1.000	0.994	0.984	0.964	0.939	0.905	0.876	0.846	0.816	0.787	0.758	0.728	0.698	0.668	0.638	0.608	0.578
32.00	0.01650	0.998	0.988	0.973	0.952	0.927	0.898	0.867	0.834	0.804	0.775	0.746	0.716	0.686	0.656	0.626	0.596	0.566
64.00	0.00908	0.996	0.984	0.965	0.940	0.910	0.876	0.840	0.801	0.771	0.742	0.712	0.682	0.652	0.622	0.592	0.562	0.532
128.00	0.00478	0.995	0.982	0.961	0.938	0.903	0.870	0.836	0.803	0.774	0.745	0.715	0.685	0.655	0.625	0.595	0.565	0.535
256.00	0.00246	0.995	0.981	0.958	0.929	0.893	0.854	0.812	0.780	0.741	0.711	0.681	0.651	0.621	0.591	0.561	0.531	0.501
512.00	0.00125	0.995	0.980	0.957	0.926	0.890	0.850	0.806	0.771	0.732	0.702	0.672	0.642	0.612	0.582	0.552	0.522	0.492

TABLE III. - Continued. CALCULATED DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS RADIAL DISTANCES FROM SLOT EXIT

(g) Length to inlet width ratio, 0.25

(g-1) Wall half-angle, -5°

Radial distance from slot exit, R/W ₁	Center-plane flux relative to inlet, n(O)/n ₁	Angle from centerplane, φ, deg																
		5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85
Flux relative to centerplane, n(φ)/n(O)																		
0.48	0.64201	1.007	1.011	1.008	1.002	0.993	0.980	0.965	0.947	0.926	0.893	0.850	0.821	0.790	0.758	0.725		
0.50	0.62935	1.007	1.010	1.006	0.999	0.983	0.976	0.960	0.941	0.919	0.896	0.870	0.842	0.813	0.779	0.737	0.651	
1.00	0.40463	1.000	0.996	0.986	0.972	0.953	0.922	0.886	0.844	0.794	0.737	0.611	0.594	0.506	0.407	0.295	0.173	0.070
2.00	0.22586	0.997	0.963	0.933	0.897	0.854	0.804	0.749	0.687	0.618	0.544	0.464	0.379	0.289	0.193	0.105	0.050	
4.00	0.11810	0.991	0.977	0.944	0.910	0.870	0.823	0.770	0.711	0.646	0.576	0.501	0.422	0.349	0.254	0.165	0.095	0.046
8.00	0.05989	0.989	0.968	0.939	0.904	0.862	0.814	0.759	0.699	0.633	0.563	0.488	0.405	0.326	0.242	0.155	0.092	0.044
16.00	0.02999	0.992	0.977	0.942	0.906	0.863	0.814	0.759	0.698	0.631	0.560	0.484	0.405	0.323	0.238	0.151	0.092	0.044
32.00	0.01500	0.994	0.977	0.943	0.907	0.864	0.814	0.759	0.697	0.631	0.559	0.483	0.404	0.321	0.236	0.149	0.092	0.044
64.00	0.00750	0.994	0.973	0.944	0.908	0.864	0.815	0.759	0.697	0.630	0.559	0.483	0.403	0.320	0.234	0.148	0.091	0.044
128.00	0.00375	0.995	0.973	0.944	0.908	0.865	0.815	0.759	0.697	0.630	0.558	0.482	0.402	0.320	0.234	0.147	0.091	0.044
256.00	0.00187	0.995	0.973	0.944	0.908	0.865	0.815	0.759	0.697	0.630	0.558	0.482	0.402	0.320	0.234	0.147	0.091	0.044
512.00	0.00094	0.995	0.973	0.944	0.908	0.865	0.815	0.759	0.697	0.630	0.558	0.482	0.402	0.320	0.234	0.147	0.091	0.044
(g-2) Wall half-angle, -10°																		
0.45	0.65524	1.007	1.010	1.007	1.000	0.990	0.977	0.960	0.941	0.920	0.896	0.870	0.841	0.812	0.782	0.751	0.719	
0.50	0.62530	1.006	1.006	1.007	1.002	0.993	0.982	0.967	0.949	0.928	0.906	0.882	0.853	0.822	0.785	0.737	0.659	0.474
1.00	0.36963	1.000	0.994	0.983	0.964	0.938	0.907	0.870	0.827	0.776	0.718	0.651	0.575	0.489	0.392	0.284	0.168	0.072
2.00	0.21987	0.993	0.97	0.952	0.922	0.886	0.844	0.795	0.740	0.679	0.612	0.538	0.460	0.376	0.289	0.197	0.112	0.054
4.00	0.11302	0.994	0.975	0.948	0.914	0.875	0.834	0.781	0.728	0.658	0.582	0.508	0.429	0.349	0.261	0.173	0.104	0.050
8.00	0.05678	0.996	0.979	0.952	0.917	0.875	0.837	0.772	0.712	0.646	0.575	0.500	0.420	0.338	0.252	0.165	0.102	0.049
16.00	0.02843	0.996	0.979	0.954	0.919	0.876	0.837	0.772	0.711	0.644	0.573	0.497	0.417	0.334	0.249	0.161	0.101	0.049
32.00	0.01422	0.996	0.978	0.954	0.916	0.877	0.838	0.772	0.711	0.644	0.572	0.496	0.416	0.333	0.247	0.160	0.101	0.049
64.00	0.00711	0.996	0.978	0.956	0.920	0.877	0.838	0.772	0.711	0.644	0.572	0.496	0.416	0.332	0.247	0.159	0.101	0.049
128.00	0.00355	0.996	0.978	0.956	0.920	0.878	0.838	0.772	0.711	0.644	0.572	0.495	0.415	0.332	0.246	0.158	0.101	0.049
256.00	0.00178	0.996	0.978	0.956	0.921	0.878	0.838	0.772	0.711	0.644	0.572	0.495	0.415	0.332	0.246	0.158	0.101	0.049
512.00	0.00089	0.996	0.978	0.956	0.921	0.878	0.838	0.772	0.711	0.644	0.572	0.495	0.415	0.332	0.246	0.158	0.101	0.049
(g-3) Wall half-angle, -20°																		
0.41	0.67487	1.006	1.008	1.007	1.002	0.993	0.981	0.966	0.948	0.926	0.902	0.880	0.856	0.830	0.803	0.775	0.745	0.713
0.50	0.60929	1.004	1.003	0.999	0.930	0.978	0.963	0.946	0.925	0.903	0.876	0.846	0.810	0.766	0.708	0.626	0.494	0.271
1.00	0.37688	0.995	0.983	0.966	0.944	0.917	0.884	0.846	0.801	0.750	0.690	0.623	0.548	0.464	0.384	0.297	0.207	0.126
2.00	0.20082	0.997	0.985	0.961	0.931	0.895	0.852	0.803	0.747	0.686	0.619	0.546	0.467	0.389	0.307	0.227	0.149	0.058
4.00	0.10197	0.996	0.985	0.966	0.933	0.893	0.850	0.803	0.746	0.686	0.619	0.546	0.466	0.389	0.307	0.227	0.149	0.058
8.00	0.05118	0.996	0.985	0.966	0.935	0.894	0.851	0.805	0.746	0.686	0.619	0.546	0.466	0.389	0.307	0.227	0.149	0.058
16.00	0.02562	0.996	0.985	0.966	0.931	0.895	0.857	0.807	0.747	0.687	0.620	0.547	0.467	0.389	0.307	0.227	0.149	0.058
32.00	0.01281	0.996	0.985	0.966	0.930	0.896	0.858	0.806	0.748	0.688	0.621	0.548	0.468	0.390	0.307	0.227	0.149	0.058
64.00	0.00641	0.996	0.985	0.966	0.930	0.897	0.859	0.807	0.749	0.689	0.622	0.549	0.469	0.391	0.307	0.227	0.149	0.058
128.00	0.00320	0.996	0.985	0.966	0.930	0.897	0.859	0.807	0.749	0.689	0.623	0.550	0.470	0.392	0.307	0.227	0.149	0.058
256.00	0.00160	0.996	0.985	0.966	0.930	0.897	0.859	0.807	0.749	0.689	0.624	0.551	0.471	0.393	0.307	0.227	0.149	0.058
512.00	0.00080	0.996	0.985	0.966	0.930	0.897	0.859	0.807	0.749	0.689	0.625	0.552	0.472	0.394	0.307	0.227	0.149	0.058

(g-4) Wall half-angle, -30°

0.35	0.69157	1.004	1.000	0.992	0.980	0.964	0.949	0.933	0.915	0.895	0.874	0.850	0.825	0.799	0.771	0.742	0.711
0.50	0.57356	0.999	0.994	0.985	0.973	0.958	0.941	0.920	0.896	0.867	0.833	0.793	0.743	0.681	0.601	0.494	0.351
1.00	0.33434	0.977	0.969	0.953	0.930	0.913	0.895	0.871	0.842	0.812	0.781	0.742	0.692	0.631	0.561	0.494	0.351
2.00	0.17477	0.997	0.986	0.969	0.945	0.910	0.866	0.816	0.760	0.698	0.630	0.557	0.479	0.376	0.309	0.219	0.140
4.00	0.08840	0.96	0.985	0.96	0.941	0.908	0.863	0.810	0.752	0.687	0.617	0.542	0.463	0.380	0.295	0.206	0.134
8.00	0.04433	0.996	0.985	0.966	0.940	0.864	0.810	0.750	0.685	0.614	0.539	0.459	0.376	0.290	0.203	0.133	0.065
16.00	0.02218	0.996	0.985	0.966	0.940	0.864	0.810	0.750	0.684	0.613	0.537	0.457	0.374	0.288	0.203	0.132	0.065
32.00	0.01109	0.996	0.985	0.966	0.940	0.864	0.811	0.751	0.685	0.613	0.537	0.457	0.373	0.287	0.202	0.132	0.065
64.00	0.00555	0.996	0.985	0.966	0.940	0.864	0.811	0.751	0.685	0.612	0.537	0.457	0.373	0.287	0.202	0.132	0.065
128.00	0.00277	0.996	0.985	0.966	0.940	0.864	0.812	0.751	0.685	0.613	0.537	0.457	0.373	0.286	0.202	0.132	0.065
256.00	0.00139	0.996	0.985	0.966	0.940	0.864	0.812	0.751	0.685	0.613	0.537	0.457	0.373	0.286	0.202	0.132	0.065
512.00	0.00069	0.996	0.985	0.966	0.940	0.864	0.812	0.751	0.685	0.613	0.537	0.457	0.373	0.286	0.202	0.132	0.065

(g-5) Wall half-angle, -45°

0.25	0.70711	0.998	0.994	0.988	0.979	0.970	0.958	0.944	0.929	0.911	0.892	0.872	0.849	0.825	0.800	0.773	0.744
0.50	0.44721	0.998	0.992	0.982	0.968	0.948	0.922	0.891	0.853	0.809	0.757	0.697	0.626	0.545	0.451	0.346	0.228
1.00	0.24254	0.997	0.987	0.971	0.949	0.920	0.885	0.843	0.790	0.732	0.667	0.595	0.518	0.435	0.356	0.248	0.112
2.00	0.12463	0.996	0.985	0.967	0.941	0.908	0.863	0.810	0.752	0.687	0.617	0.542	0.462	0.380	0.295	0.206	0.082
4.00	0.06238	0.996	0.985	0.966	0.940	0.907	0.867	0.821	0.768	0.706	0.637	0.563	0.484	0.401	0.316	0.232	0.155
8.00	0.03123	0.996	0.985	0.966	0.940	0.907	0.866	0.820	0.767	0.706	0.636	0.561	0.482	0.399	0.313	0.230	0.152
16.00	0.01662	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.706	0.636	0.561	0.482	0.399	0.313	0.230	0.152
32.00	0.008181	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.636	0.561	0.482	0.398	0.312	0.230	0.151
64.00	0.00391	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.636	0.561	0.482	0.398	0.312	0.230	0.151
128.00	0.00195	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.637	0.561	0.482	0.398	0.312	0.230	0.151
256.00	0.00098	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.637	0.561	0.482	0.398	0.312	0.230	0.151
512.00	0.00049	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.637	0.561	0.482	0.398	0.312	0.230	0.151

(g-5) Wall half-angle, -60°

0.08	0.70711	0.599	0.996	0.991	0.985	0.976	0.966	0.953	0.938	0.921	0.903	0.883	0.861	0.848	0.813	0.786	0.758
0.25	0.28135	0.997	0.988	0.972	0.948	0.922	0.891	0.853	0.809	0.757	0.697	0.626	0.545	0.451	0.346	0.285	0.190
0.50	0.14634	0.996	0.986	0.968	0.943	0.912	0.873	0.828	0.777	0.719	0.655	0.587	0.510	0.429	0.344	0.258	0.171
1.00	0.07479	0.996	0.985	0.967	0.941	0.908	0.868	0.821	0.761	0.700	0.646	0.577	0.501	0.420	0.336	0.251	0.166
2.00	0.03747	0.996	0.985	0.966	0.940	0.907	0.866	0.820	0.762	0.701	0.644	0.574	0.501	0.418	0.334	0.249	0.165
4.00	0.01875	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
8.00	0.00937	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
16.00	0.00469	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
32.00	0.00234	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
64.00	0.00117	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
128.00	0.00059	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
256.00	0.00029	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165
512.00	0.00015	0.996	0.985	0.966	0.940	0.906	0.866	0.819	0.766	0.707	0.643	0.574	0.499	0.417	0.333	0.249	0.165

TABLE II. - Continued. CALCULATED DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS RADIAL DISTANCES FROM SLOT EXIT

(h) Length to inlet width ratio, 0.50

(h-1) Wall half-angle, -5° Angle from centerplane, ϕ , deg

Radial distance from slot exit, R/W_1	$n(0)/n_1$	Flux relative to centerplane, $n(\phi)/n(0)$																
		5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85
(h-2) Wall half-angle, -10°																		
0.46	0.59356	1.012	1.019	1.021	1.020	1.014	1.004	0.990	0.972	0.952	0.928	0.902	0.873	0.842	0.810	0.775	0.739	0.703
0.50	0.57057	1.010	1.016	1.017	1.014	1.006	0.994	0.978	0.959	0.931	0.912	0.886	0.856	0.823	0.783	0.732	0.655	0.467
1.00	0.37105	1.002	0.987	0.973	0.949	0.911	0.888	0.817	0.760	0.694	0.619	0.534	0.438	0.331	0.214	0.136	0.064	
2.00	0.21137	0.998	0.985	0.953	0.915	0.870	0.820	0.763	0.700	0.630	0.555	0.474	0.397	0.310	0.210	0.151	0.096	
4.00	0.11232	0.985	0.956	0.920	0.878	0.829	0.774	0.713	0.647	0.575	0.498	0.417	0.333	0.245	0.186	0.134	0.086	
8.00	0.05741	0.981	0.951	0.913	0.866	0.817	0.760	0.697	0.629	0.556	0.479	0.397	0.312	0.232	0.179	0.129	0.083	
16.00	0.02874	0.988	0.956	0.916	0.871	0.819	0.760	0.696	0.627	0.552	0.473	0.391	0.306	0.230	0.178	0.128	0.082	
32.00	0.01437	0.991	0.959	0.919	0.874	0.821	0.761	0.696	0.625	0.550	0.471	0.388	0.302	0.229	0.177	0.128	0.082	
64.00	0.00719	0.993	0.960	0.921	0.874	0.821	0.761	0.696	0.625	0.549	0.469	0.386	0.300	0.228	0.177	0.128	0.082	
128.00	0.00359	0.994	0.961	0.921	0.874	0.821	0.761	0.696	0.625	0.549	0.469	0.386	0.300	0.228	0.177	0.128	0.082	
256.00	0.00180	0.994	0.961	0.921	0.875	0.821	0.761	0.696	0.625	0.549	0.469	0.386	0.300	0.228	0.177	0.128	0.082	
512.00	0.00090	0.994	0.962	0.922	0.875	0.821	0.761	0.696	0.625	0.549	0.469	0.386	0.300	0.228	0.177	0.128	0.082	
(h-3) Wall half-angle, -20°																		
0.41	0.61659	1.012	1.019	1.021	1.018	1.011	1.000	0.985	0.967	0.945	0.920	0.892	0.830	0.796	0.763	0.729	0.694	
0.50	0.55911	1.008	1.012	1.010	1.003	0.992	0.977	0.958	0.936	0.910	0.879	0.844	0.803	0.753	0.588	0.596	0.451	
1.00	0.25430	1.000	0.994	0.979	0.950	0.917	0.877	0.832	0.780	0.722	0.655	0.597	0.497	0.362	0.209	0.134	0.063	
2.00	0.19898	0.986	0.956	0.929	0.891	0.848	0.794	0.742	0.681	0.633	0.560	0.461	0.378	0.290	0.217	0.157	0.101	
4.00	0.10197	0.954	0.965	0.930	0.888	0.839	0.784	0.723	0.657	0.585	0.509	0.428	0.363	0.261	0.203	0.147	0.095	
8.00	0.05118	0.956	0.975	0.937	0.892	0.841	0.784	0.720	0.651	0.577	0.509	0.431	0.356	0.256	0.198	0.144	0.093	
16.00	0.02562	0.956	0.976	0.931	0.887	0.834	0.784	0.720	0.650	0.574	0.507	0.433	0.356	0.254	0.197	0.143	0.092	
32.00	0.01281	0.956	0.983	0.944	0.897	0.844	0.785	0.720	0.649	0.573	0.507	0.430	0.352	0.252	0.197	0.143	0.092	
64.00	0.00641	0.996	0.984	0.945	0.898	0.849	0.785	0.720	0.649	0.573	0.507	0.432	0.353	0.253	0.197	0.143	0.092	
128.00	0.00320	0.956	0.989	0.945	0.899	0.845	0.786	0.720	0.649	0.572	0.507	0.432	0.353	0.253	0.197	0.143	0.092	
256.00	0.00160	0.966	0.985	0.946	0.899	0.846	0.786	0.720	0.649	0.572	0.507	0.432	0.353	0.253	0.197	0.143	0.092	
512.00	0.00080	0.956	0.985	0.946	0.899	0.846	0.786	0.720	0.648	0.572	0.507	0.431	0.353	0.253	0.197	0.143	0.092	
(h-4) Wall half-angle, -30°																		
0.32	0.65156	1.011	1.016	1.017	1.012	1.002	0.988	0.970	0.948	0.923	0.894	0.869	0.842	0.814	0.784	0.753	0.720	0.686
0.50	0.51191	1.003	0.999	0.999	0.974	0.953	0.929	0.900	0.867	0.829	0.784	0.731	0.667	0.589	0.493	0.375	0.242	0.117
1.00	0.20478	0.941	0.971	0.946	0.915	0.879	0.837	0.789	0.735	0.674	0.606	0.532	0.451	0.363	0.277	0.203	0.131	0.063
2.00	0.15799	0.942	0.956	0.946	0.918	0.873	0.822	0.764	0.701	0.631	0.557	0.477	0.393	0.311	0.243	0.178	0.115	0.056
4.00	0.07795	0.956	0.985	0.941	0.897	0.844	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.235	0.172	0.111	0.054
8.00	0.03997	0.956	0.985	0.944	0.897	0.844	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.235	0.170	0.110	0.053
16.00	0.02020	0.956	0.985	0.946	0.898	0.845	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.231	0.169	0.110	0.053
32.00	0.01000	0.956	0.985	0.946	0.898	0.845	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.231	0.169	0.110	0.053
64.00	0.00550	0.956	0.985	0.946	0.898	0.845	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.231	0.169	0.110	0.053
128.00	0.00250	0.956	0.985	0.946	0.898	0.845	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.231	0.169	0.110	0.053
256.00	0.00125	0.956	0.985	0.946	0.898	0.845	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.231	0.169	0.110	0.053
512.00	0.00062	0.956	0.985	0.946	0.898	0.845	0.785	0.720	0.649	0.573	0.509	0.432	0.356	0.275	0.231	0.169	0.110	0.053

(1) Length to inlet width ratio, 1.00
 (1-1) Wall half-angle, -5°

Radial distance from slot exit, R/W ₁	Center-plane flux relative to slot exit, n(0)/n ₁	Angle from centerplane, φ, deg																			
		5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85			
Flux relative to centerplane, n(φ)/n(0)																					
0.42	0.52572	1.016	1.026	1.030	1.028	1.021	1.009	0.993	0.972	0.948	0.921	0.890	0.857	0.822	0.784	0.745	0.704	0.661			
0.50	0.45533	1.013	1.019	1.019	1.013	1.002	0.988	0.966	0.943	0.916	0.888	0.850	0.812	0.773	0.73	0.672	0.616	0.573	0.512	0.412	0.212
1.00	0.31892	1.003	1.019	1.019	1.019	1.002	0.987	0.972	0.947	0.916	0.875	0.834	0.795	0.750	0.717	0.676	0.630	0.594	0.554	0.511	0.454
2.00	0.18672	0.998	0.973	0.925	0.871	0.811	0.745	0.673	0.595	0.511	0.421	0.329	0.289	0.232	0.178	0.128	0.092	0.059	0.039	0.019	0.009
4.00	0.023	0.910	0.92	0.870	0.880	0.744	0.673	0.59	0.515	0.429	0.357	0.302	0.250	0.201	0.155	0.112	0.072	0.034	0.012	0.006	0.002
8.00	0.0243	0.969	0.918	0.860	0.796	0.727	0.651	0.571	0.486	0.398	0.342	0.289	0.239	0.192	0.149	0.107	0.068	0.033	0.012	0.006	0.002
16.00	0.02624	0.980	0.926	0.866	0.799	0.726	0.648	0.575	0.477	0.394	0.338	0.286	0.237	0.191	0.147	0.107	0.068	0.033	0.012	0.006	0.002
32.00	0.01312	0.986	0.931	0.869	0.801	0.726	0.667	0.562	0.472	0.392	0.337	0.285	0.236	0.190	0.147	0.106	0.068	0.033	0.012	0.006	0.002
64.00	0.00656	0.989	0.934	0.871	0.802	0.722	0.664	0.560	0.470	0.392	0.336	0.284	0.236	0.190	0.147	0.106	0.068	0.033	0.012	0.006	0.002
128.00	0.00328	0.991	0.935	0.872	0.803	0.727	0.665	0.559	0.469	0.391	0.336	0.284	0.235	0.190	0.147	0.106	0.068	0.033	0.012	0.006	0.002
256.00	0.00164	0.992	0.935	0.872	0.803	0.727	0.665	0.559	0.468	0.391	0.336	0.284	0.235	0.190	0.147	0.106	0.068	0.033	0.012	0.006	0.002
512.00	0.00082	0.992	0.936	0.873	0.803	0.727	0.665	0.559	0.468	0.391	0.336	0.284	0.235	0.190	0.147	0.106	0.068	0.033	0.012	0.006	0.002
(1-2) Wall half-angle, -10°																					
0.32	0.56301	1.017	1.026	1.030	1.028	1.020	1.007	0.989	0.967	0.941	0.912	0.879	0.844	0.807	0.768	0.731	0.692	0.652	0.612	0.573	0.512
1.00	0.44936	1.008	1.008	1.008	1.008	1.002	0.971	0.946	0.908	0.864	0.815	0.759	0.716	0.656	0.523	0.415	0.312	0.205	0.104	0.050	0.008
2.00	0.28081	0.999	0.98	0.943	0.899	0.850	0.794	0.732	0.664	0.589	0.507	0.424	0.355	0.289	0.224	0.162	0.104	0.050	0.019	0.009	0.002
4.00	0.15799	0.912	0.950	0.882	0.828	0.768	0.703	0.632	0.555	0.474	0.405	0.344	0.287	0.232	0.180	0.131	0.084	0.040	0.019	0.009	0.002
8.00	0.0795	0.936	0.968	0.898	0.826	0.767	0.687	0.603	0.514	0.444	0.389	0.327	0.276	0.223	0.173	0.126	0.081	0.039	0.019	0.009	0.002
16.00	0.03997	0.986	0.968	0.907	0.840	0.764	0.689	0.612	0.528	0.450	0.383	0.326	0.272	0.220	0.171	0.124	0.080	0.039	0.019	0.009	0.002
32.00	0.02000	0.996	0.977	0.914	0.844	0.767	0.685	0.608	0.529	0.441	0.381	0.324	0.270	0.219	0.170	0.124	0.080	0.039	0.019	0.009	0.002
64.00	0.00500	0.996	0.984	0.917	0.846	0.768	0.688	0.608	0.529	0.441	0.380	0.323	0.270	0.219	0.170	0.124	0.080	0.039	0.019	0.009	0.002
128.00	0.00250	0.996	0.985	0.920	0.848	0.769	0.684	0.604	0.529	0.441	0.380	0.323	0.269	0.218	0.170	0.123	0.080	0.038	0.019	0.009	0.002
256.00	0.00125	0.996	0.985	0.921	0.848	0.769	0.684	0.604	0.529	0.441	0.380	0.323	0.269	0.218	0.170	0.123	0.080	0.038	0.019	0.009	0.002
512.00	0.00062	0.996	0.985	0.921	0.848	0.769	0.684	0.604	0.529	0.441	0.380	0.323	0.269	0.218	0.170	0.123	0.080	0.038	0.019	0.009	0.002
(1-3) Wall half-angle, -20°																					
0.14	0.62303	1.017	1.025	1.027	1.022	1.011	0.994	0.972	0.945	0.915	0.881	0.852	0.822	0.790	0.758	0.724	0.689	0.653	0.612	0.573	0.512
0.25	0.55795	1.003	0.996	0.977	0.951	0.921	0.887	0.848	0.803	0.752	0.694	0.637	0.549	0.466	0.379	0.318	0.284	0.246	0.186	0.136	0.090
0.50	0.26963	0.995	0.964	0.928	0.886	0.816	0.784	0.725	0.659	0.587	0.516	0.447	0.379	0.311	0.244	0.179	0.116	0.056	0.019	0.009	0.002
1.00	0.13865	0.956	0.986	0.951	0.895	0.834	0.766	0.693	0.615	0.544	0.476	0.410	0.345	0.282	0.221	0.161	0.105	0.051	0.019	0.009	0.002
2.00	0.06983	0.996	0.985	0.960	0.910	0.838	0.761	0.677	0.601	0.531	0.464	0.399	0.336	0.274	0.215	0.157	0.102	0.049	0.019	0.009	0.002
4.00	0.0458	0.996	0.986	0.966	0.912	0.843	0.758	0.670	0.597	0.522	0.460	0.395	0.333	0.272	0.213	0.156	0.101	0.049	0.019	0.009	0.002
8.00	0.01750	0.926	0.985	0.966	0.933	0.848	0.757	0.668	0.594	0.524	0.458	0.393	0.331	0.271	0.212	0.155	0.101	0.049	0.019	0.009	0.002
16.00	0.00875	0.926	0.985	0.966	0.935	0.849	0.757	0.668	0.594	0.524	0.457	0.393	0.331	0.270	0.212	0.155	0.101	0.049	0.019	0.009	0.002
32.00	0.00437	0.926	0.985	0.966	0.936	0.850	0.757	0.668	0.593	0.524	0.457	0.393	0.330	0.270	0.212	0.155	0.101	0.049	0.019	0.009	0.002
64.00	0.00219	0.926	0.985	0.966	0.937	0.850	0.757	0.668	0.593	0.524	0.457	0.393	0.330	0.270	0.212	0.155	0.101	0.049	0.019	0.009	0.002
128.00	0.00109	0.926	0.985	0.966	0.937	0.850	0.757	0.668	0.593	0.524	0.457	0.393	0.330	0.270	0.212	0.155	0.101	0.049	0.019	0.009	0.002
256.00	0.00055	0.926	0.985	0.966	0.937	0.850	0.757	0.668	0.593	0.524	0.457	0.393	0.330	0.270	0.212	0.155	0.101	0.049	0.019	0.009	0.002
512.00	0.00027	0.926	0.985	0.966	0.937	0.850	0.757	0.668	0.593	0.524	0.457	0.393	0.330	0.270	0.212	0.155	0.101	0.049	0.019	0.009	0.002

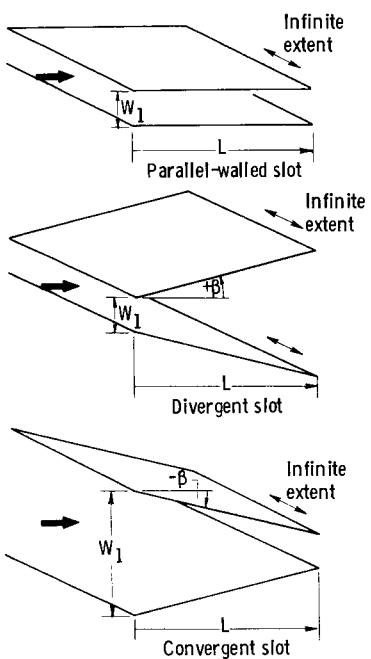
TABLE II. - Continued. CALCULATED DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS RADIAL DISTANCES FROM SLOT EXIT

(j) Length to inlet width ratio, 2.00
(j-1) Wall half-angle, -5°

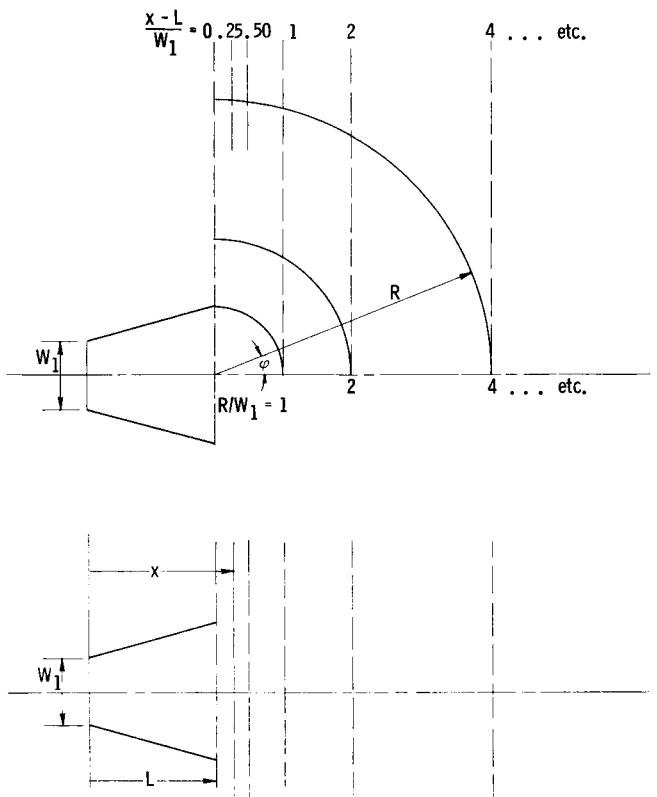
Radial distance from slot inlet, R/W_1	Center-plane flux relative to inlet flux, $n(0)/n_1$	Angle from centerplane, φ , deg																	
		5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	
Flux relative to centerplane, $n(\varphi)/n(0)$																			
0.34	0.44358	1.018	1.029	1.033	1.031	1.022	1.008	0.989	0.965	0.937	0.905	0.871	0.833	0.793	0.751	0.707	0.660	0.613	
0.50	0.31201	1.011	1.014	1.009	0.998	0.981	0.959	0.935	0.895	0.840	0.758	0.676	0.581	0.485	0.394	0.297	0.195	0.093	
1.00	0.24471	1.002	0.995	0.983	0.917	0.842	0.760	0.672	0.576	0.495	0.425	0.361	0.301	0.243	0.188	0.135	0.086	0.041	
2.00	0.14770	0.998	0.998	0.998	0.998	0.987	0.948	0.848	0.762	0.671	0.574	0.491	0.426	0.369	0.317	0.268	0.223	0.179	0.138
4.00	0.08399	0.927	0.845	0.756	0.662	0.562	0.476	0.414	0.361	0.313	0.268	0.227	0.189	0.152	0.117	0.085	0.054	0.026	
8.00	0.04246	0.948	0.853	0.753	0.666	0.535	0.462	0.402	0.351	0.304	0.261	0.222	0.184	0.148	0.115	0.083	0.053	0.026	
16.00	0.02125	0.966	0.864	0.755	0.640	0.529	0.458	0.399	0.348	0.301	0.260	0.220	0.183	0.148	0.115	0.083	0.053	0.026	
32.00	0.01062	0.976	0.869	0.756	0.637	0.527	0.456	0.397	0.347	0.301	0.259	0.219	0.182	0.147	0.114	0.083	0.053	0.026	
64.00	0.00531	0.982	0.872	0.756	0.635	0.525	0.455	0.397	0.346	0.300	0.258	0.219	0.182	0.147	0.114	0.083	0.053	0.026	
128.00	0.00266	0.985	0.874	0.757	0.634	0.525	0.454	0.396	0.346	0.300	0.258	0.219	0.182	0.147	0.114	0.082	0.053	0.026	
256.00	0.00133	0.986	0.875	0.757	0.633	0.524	0.454	0.396	0.346	0.300	0.258	0.219	0.182	0.147	0.114	0.082	0.053	0.026	
512.00	0.00066	0.987	0.875	0.757	0.633	0.524	0.454	0.396	0.346	0.300	0.258	0.219	0.182	0.147	0.114	0.082	0.053	0.026	
(j-2) Wall half-angle, -10°																			
0.14	0.50271	1.020	1.032	1.036	1.033	1.024	1.008	0.988	0.962	0.932	0.899	0.862	0.823	0.781	0.738	0.696	0.654	0.611	
0.25	0.37897	1.008	1.006	0.996	0.979	0.948	0.895	0.838	0.774	0.704	0.626	0.549	0.474	0.397	0.317	0.235	0.152	0.072	
0.50	0.24323	0.958	0.951	0.891	0.825	0.754	0.677	0.598	0.529	0.465	0.405	0.347	0.291	0.236	0.184	0.133	0.086	0.041	
1.00	0.13865	0.962	0.950	0.811	0.727	0.638	0.561	0.496	0.437	0.383	0.332	0.283	0.237	0.192	0.149	0.108	0.070	0.034	
2.00	0.06583	0.956	0.922	0.821	0.714	0.619	0.545	0.482	0.425	0.372	0.322	0.274	0.229	0.186	0.144	0.105	0.068	0.033	
4.00	0.03498	0.956	0.949	0.828	0.704	0.612	0.539	0.476	0.420	0.367	0.318	0.271	0.227	0.184	0.143	0.104	0.067	0.032	
8.00	0.01750	0.996	0.967	0.833	0.701	0.610	0.537	0.474	0.418	0.366	0.317	0.270	0.226	0.183	0.143	0.104	0.067	0.032	
16.00	0.00875	0.996	0.978	0.835	0.700	0.608	0.535	0.473	0.417	0.365	0.316	0.270	0.225	0.183	0.142	0.104	0.067	0.032	
32.00	0.00437	0.996	0.984	0.837	0.659	0.608	0.535	0.472	0.416	0.364	0.316	0.269	0.225	0.183	0.142	0.104	0.067	0.032	
64.00	0.00219	0.796	0.985	0.837	0.659	0.608	0.535	0.472	0.416	0.364	0.315	0.269	0.225	0.183	0.142	0.104	0.067	0.032	
128.00	0.00055	0.996	0.985	0.838	0.659	0.607	0.534	0.472	0.416	0.364	0.315	0.269	0.225	0.183	0.142	0.104	0.067	0.032	
256.00	0.00027	0.996	0.985	0.838	0.659	0.607	0.534	0.472	0.416	0.364	0.315	0.269	0.225	0.183	0.142	0.104	0.067	0.032	
512.00	0.00012	0.996	0.985	0.838	0.659	0.607	0.534	0.472	0.416	0.364	0.315	0.269	0.225	0.183	0.142	0.104	0.067	0.032	

TABLE II. - Concluded. CALCULATED DISTRIBUTIONS OF PARTICLE FLUX AT VARIOUS RADIAL DISTANCES FROM SLOT EXIT
 (k) Length to inlet width ratio, 4.00; wall half-angle, -5°

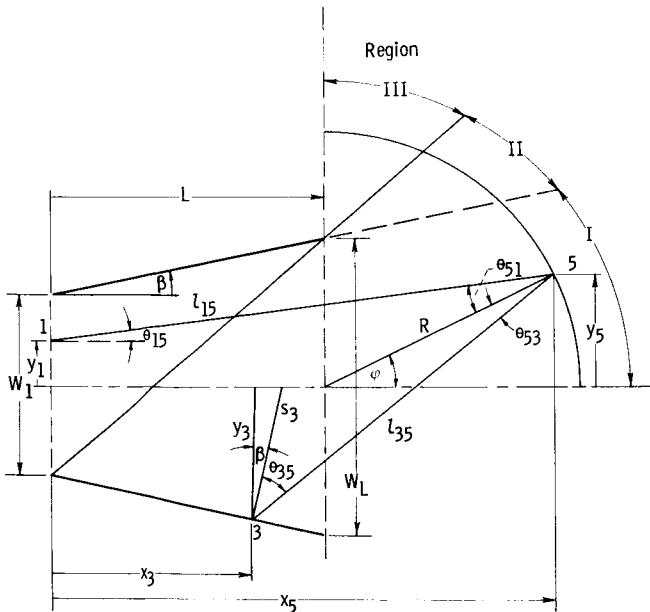
Radial distance from slot exit, R/W_1	Center-plane flux relative to slot inlet flux, $n(0)/n_1$	Angle from centerplane, φ , deg																
		5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85
Flux relative to centerplane, $n(\varphi)/n(0)$																		
0.18	0.35983	1.019	1.030	1.033	1.029	1.019	1.003	0.981	0.954	0.923	0.888	0.850	0.809	0.765	0.719	0.671	0.621	0.570
0.25	0.31449	1.013	1.017	1.012	1.017	1.001	0.983	0.959	0.932	0.902	0.833	0.744	0.648	0.560	0.478	0.395	0.305	0.204
0.50	0.21760	1.003	0.997	0.984	0.966	0.977	0.682	0.584	0.507	0.441	0.382	0.325	0.272	0.220	0.171	0.123	0.079	0.037
1.00	0.1470	0.998	0.895	0.768	0.655	0.536	0.463	0.404	0.353	0.307	0.264	0.224	0.186	0.150	0.116	0.084	0.054	0.026
2.00	0.08694	0.877	0.733	0.585	0.433	0.413	0.359	0.314	0.274	0.238	0.205	0.174	0.145	0.117	0.090	0.065	0.042	0.020
4.00	0.04495	0.892	0.708	0.549	0.456	0.392	0.341	0.298	0.261	0.227	0.195	0.166	0.138	0.111	0.086	0.062	0.040	0.019
8.00	0.02249	0.924	0.70	0.562	0.451	0.388	0.338	0.298	0.259	0.225	0.194	0.165	0.137	0.111	0.088	0.062	0.040	0.019
16.00	0.01125	0.945	0.676	0.539	0.449	0.386	0.336	0.295	0.258	0.224	0.193	0.164	0.136	0.110	0.085	0.062	0.040	0.019
32.00	0.00562	0.958	0.692	0.537	0.448	0.385	0.336	0.294	0.257	0.224	0.193	0.164	0.136	0.110	0.085	0.062	0.040	0.019
64.00	0.00281	0.965	0.691	0.537	0.447	0.385	0.335	0.294	0.257	0.224	0.193	0.164	0.136	0.110	0.085	0.062	0.040	0.019
128.00	0.00141	0.969	0.691	0.537	0.447	0.385	0.335	0.294	0.257	0.224	0.193	0.164	0.136	0.110	0.085	0.062	0.040	0.019
256.00	0.00070	0.971	0.691	0.536	0.447	0.384	0.335	0.294	0.257	0.224	0.193	0.164	0.136	0.110	0.085	0.062	0.040	0.019
512.00	0.00035	0.972	0.691	0.536	0.447	0.384	0.335	0.294	0.257	0.224	0.193	0.164	0.136	0.110	0.085	0.062	0.040	0.019



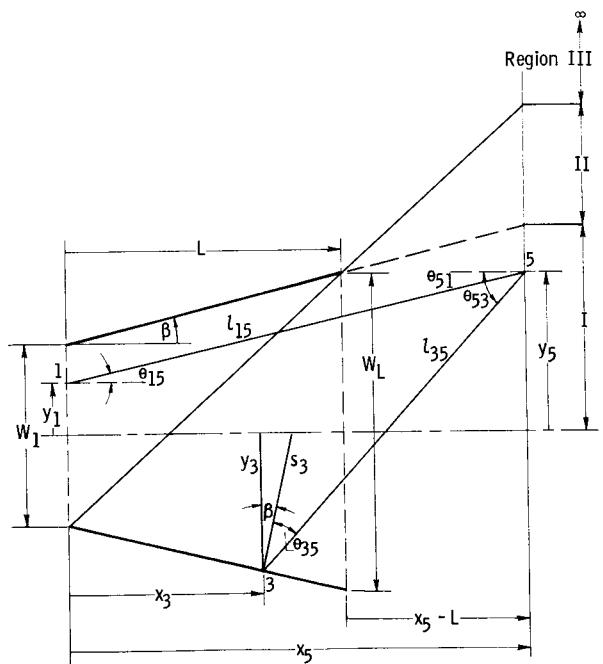
(a) Illustration of configurations investigated.



(b) Illustration of location of planes and cylindrical surfaces at which flux patterns are calculated.



(c) Parameters in radial flux relations.



(d) Parameters in planar flux relations.

Figure 1. - Schematic diagrams.

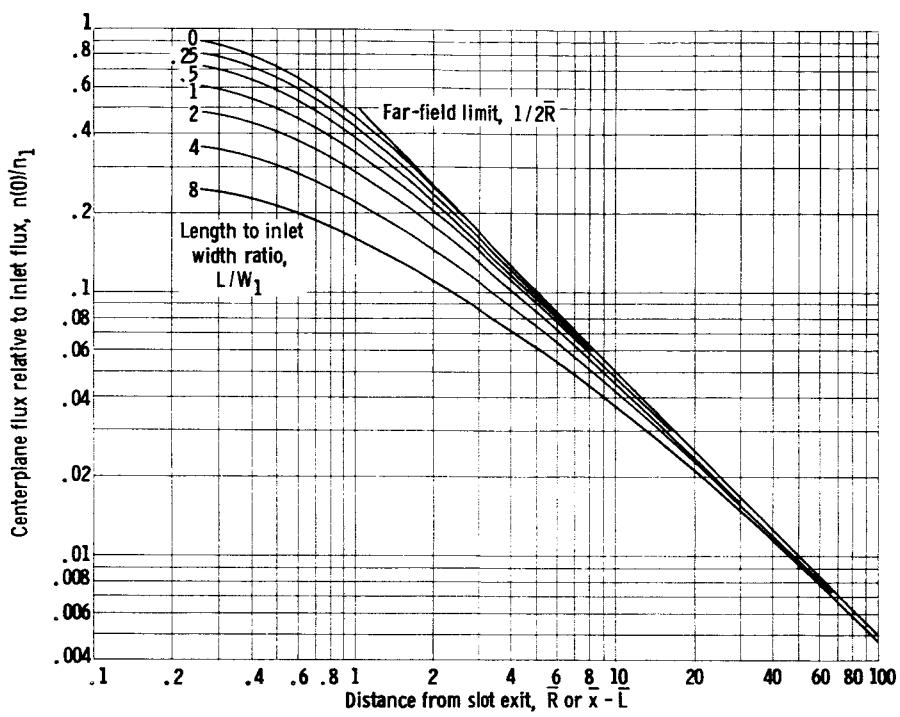


Figure 2. - Variation of centerplane flux with distance from exit aperture for parallel-walled slot.

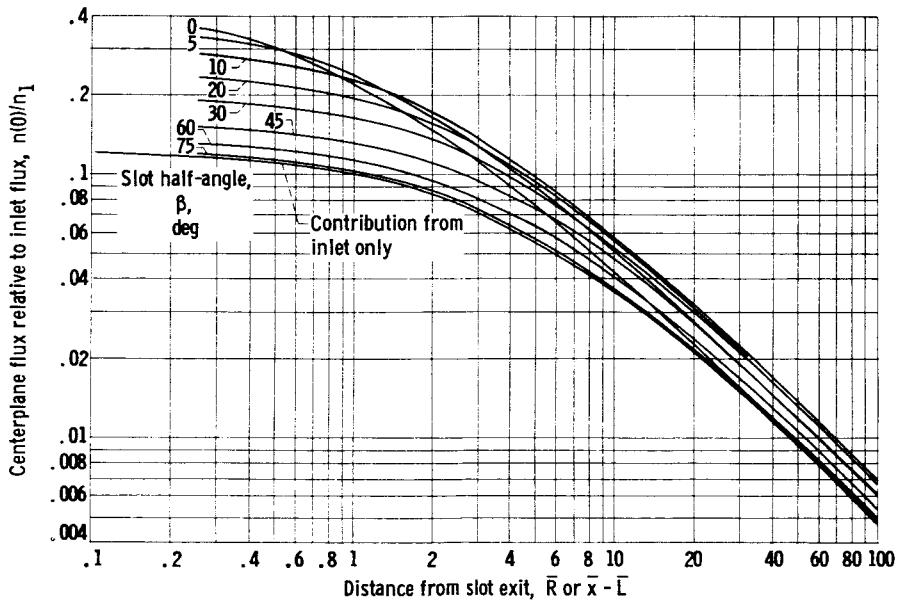


Figure 3. - Variation of centerplane flux with distance from exit aperture. Length to inlet width ratio, 4.

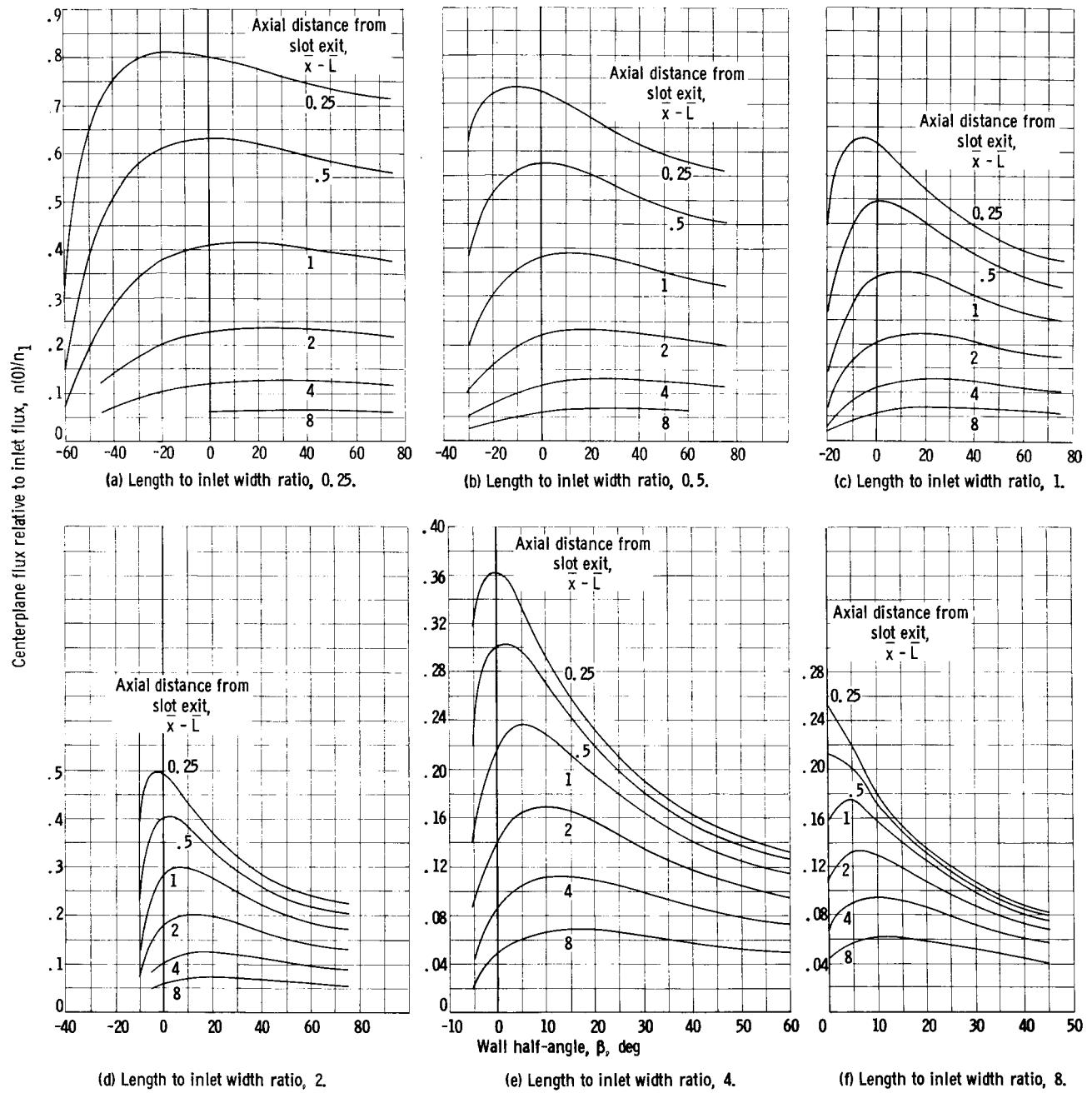


Figure 4. - Variation of centerplane flux with wall half-angle at various distances from exit aperture.

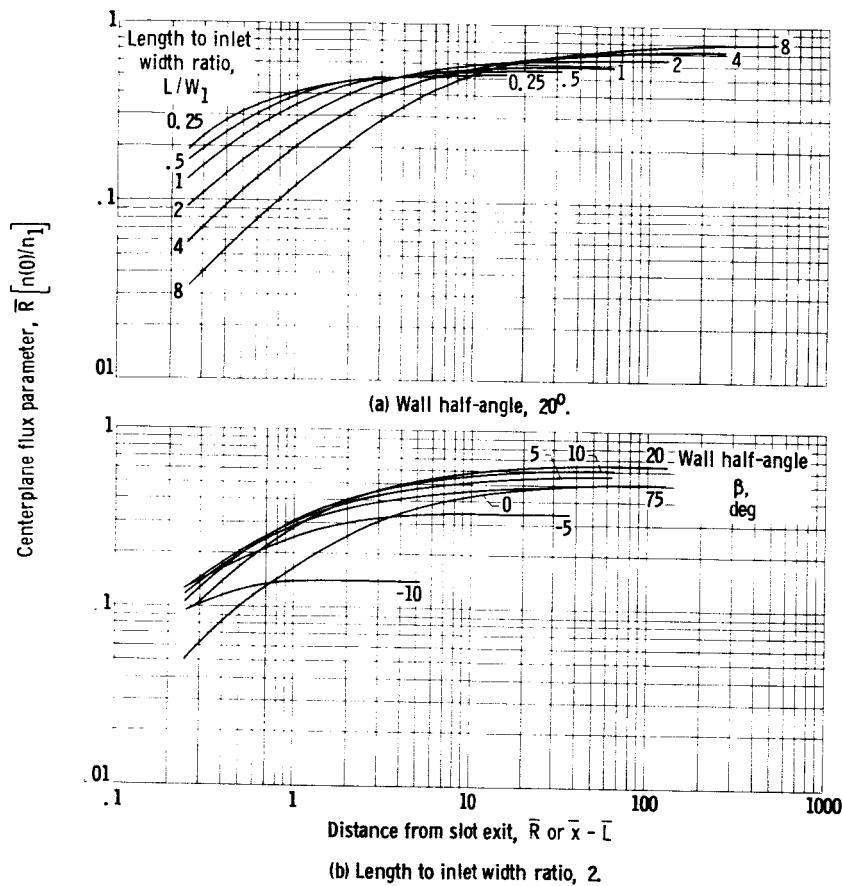


Figure 5. - Variation of centerplane flux parameter with distance from slot exit.

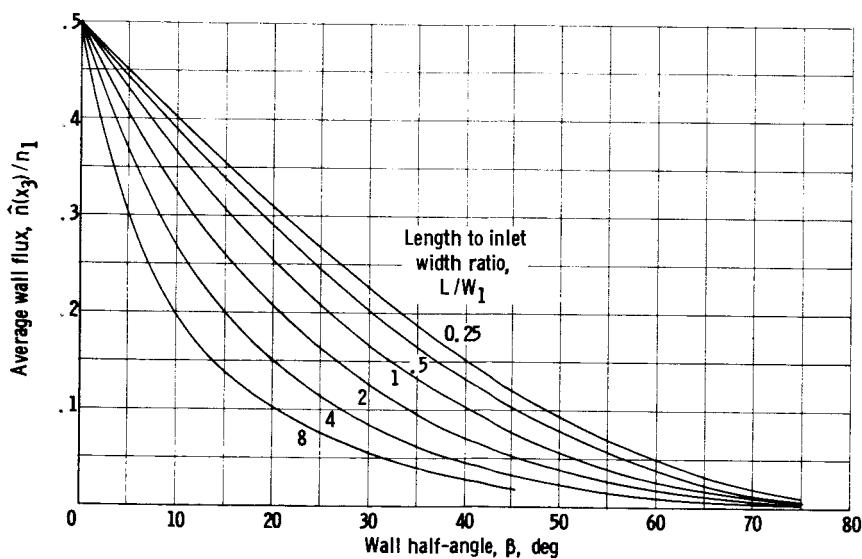


Figure 6. - Average wall flux values for slots of varying length to initial width ratios and wall half-angle.

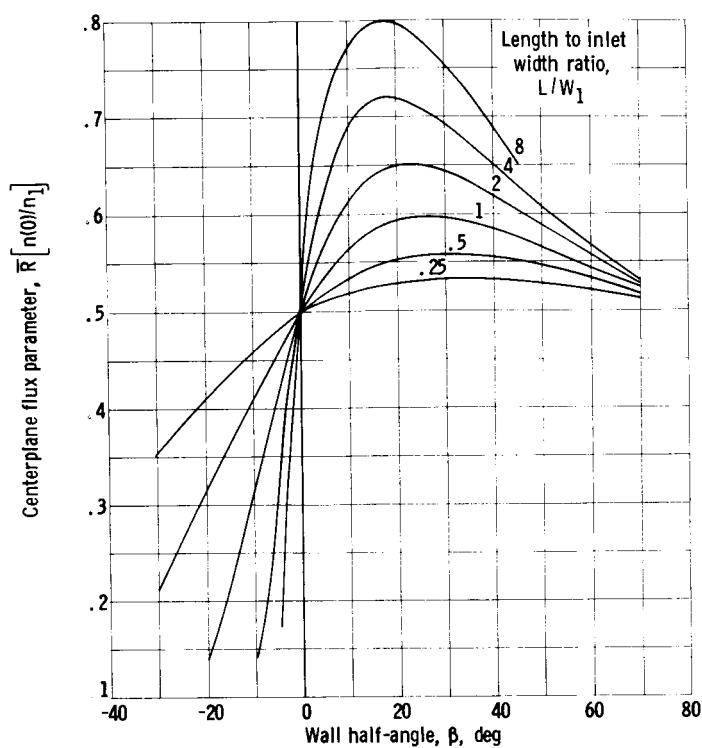


Figure 7. - Variation of limiting value of centerplane flux parameter with wall half-angle and slot length to inlet width ratio.

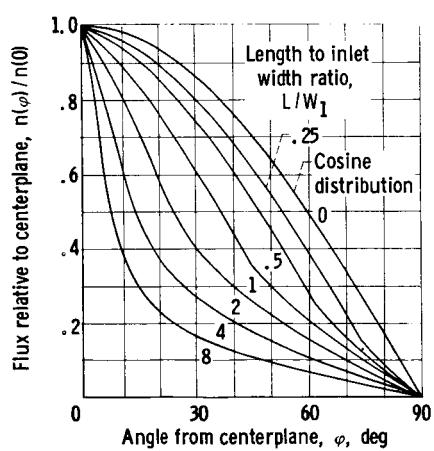
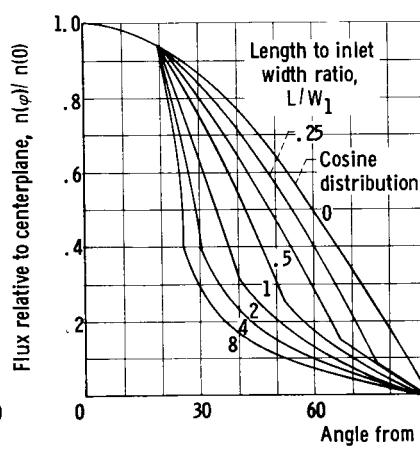


Figure 8. - Far-field flux patterns for parallel-walled slots (wall half-angle = 0) and various length to inlet width ratios.



(a) Divergent slots; wall half-angle, 20° . (b) Convergent slots; wall half-angle, -20° .

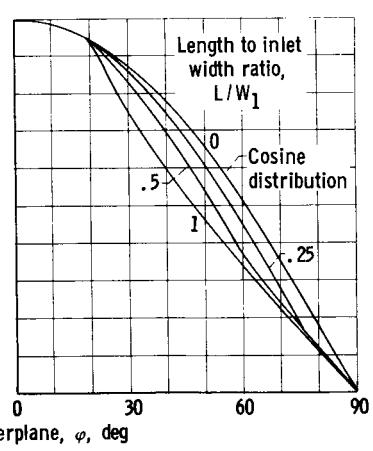


Figure 9. - Far-field flux patterns for slots with 20° wall-half angle and various length to inlet width ratios.

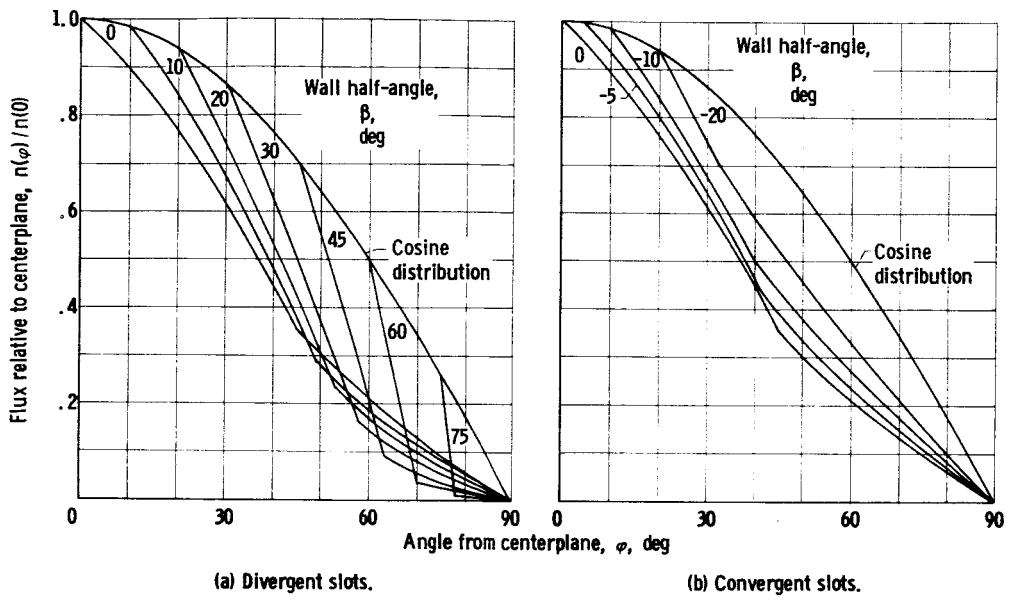


Figure 10. - Far-field flux patterns for slots with length to inlet width ratio of 1 and varying wall half-angles.

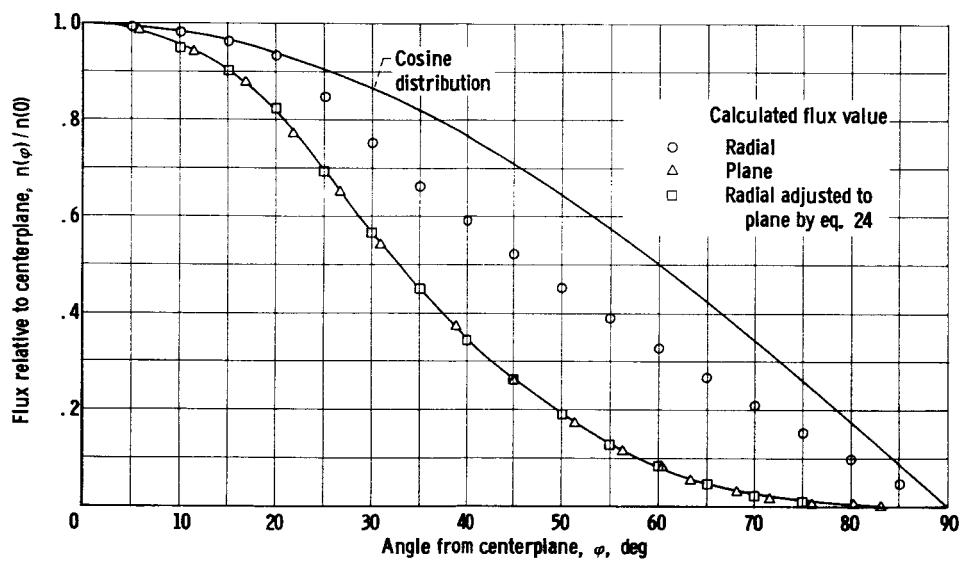
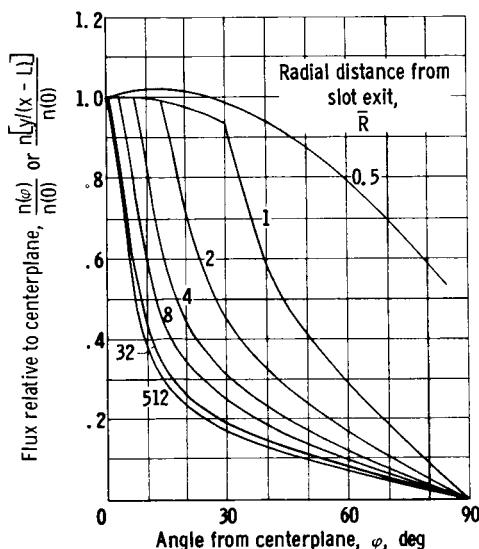
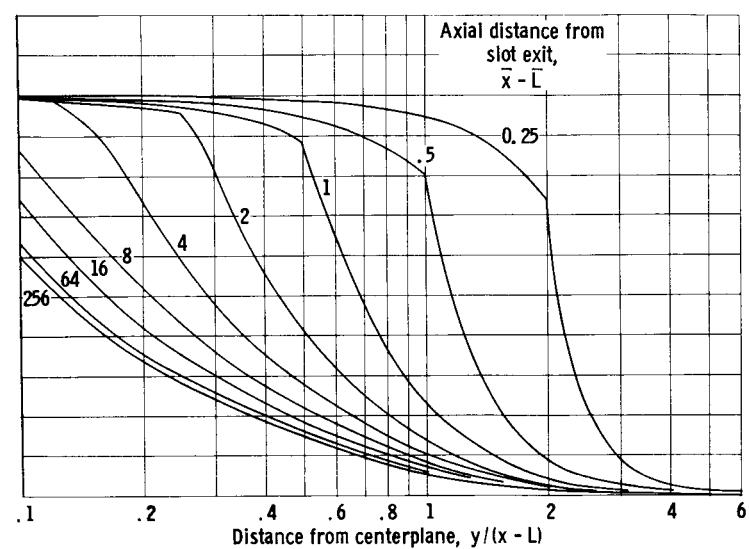


Figure 11. - Comparison of radial and planar flux patterns in far field. Length to inlet width ratio, 1; wall half-angle, -20° .

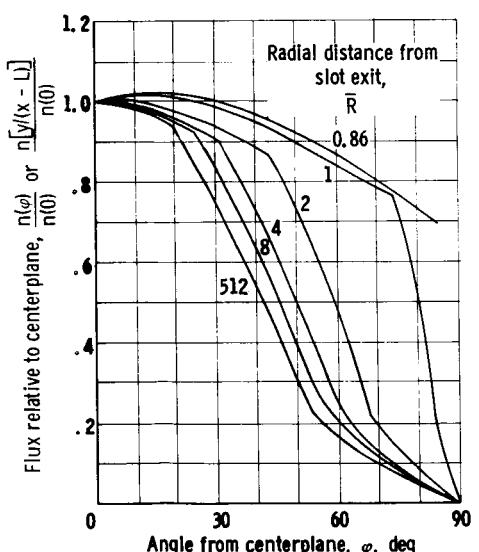


(a) Radial patterns.

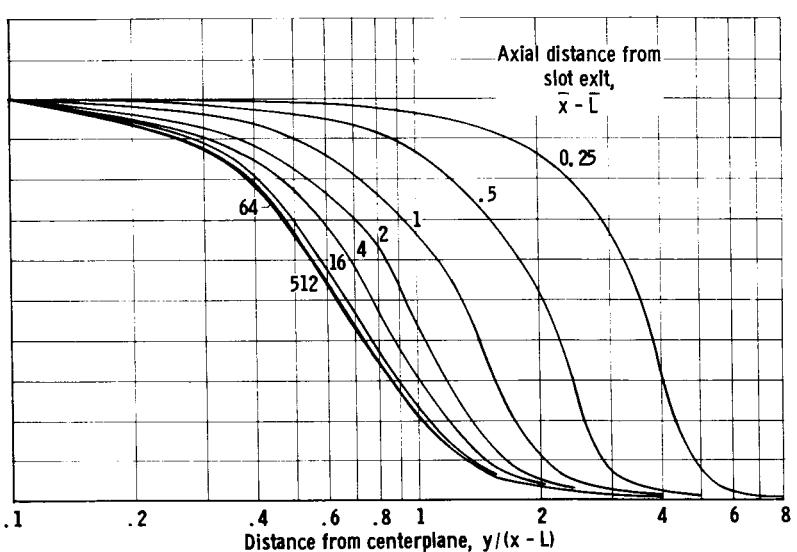


(b) Plane patterns.

Figure 12. - Variation of flux patterns with distance from slot exit. Length to inlet width ratio, 8; wall half-angle, 0.

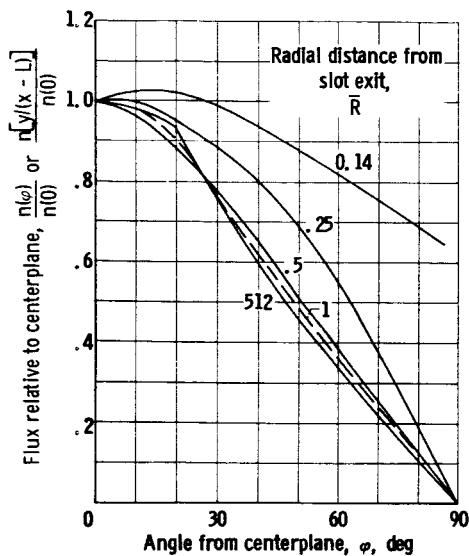


(a) Radial patterns.

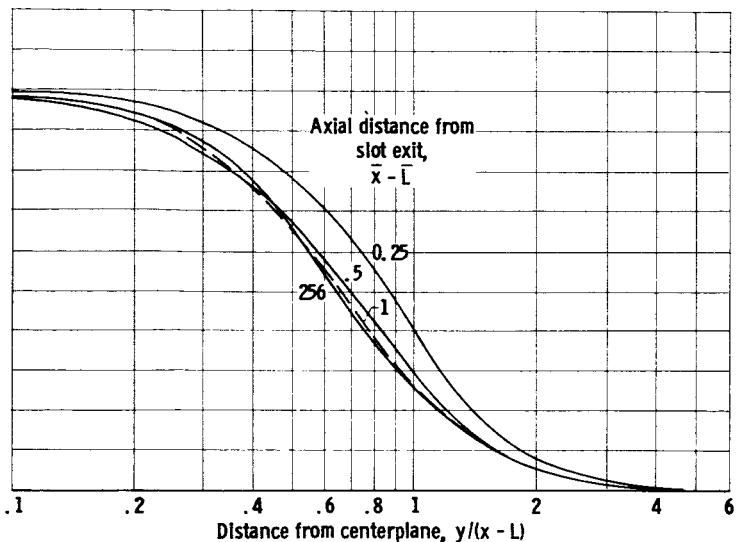


(b) Plane patterns.

Figure 13. - Variation of flux patterns for 20° divergent slot. Length to inlet width ratio, 1.



(a) Radial patterns.



(b) Plane patterns.

Figure 14. - Variation of flux patterns for 20° convergent slot. Length to inlet width ratio, 1.

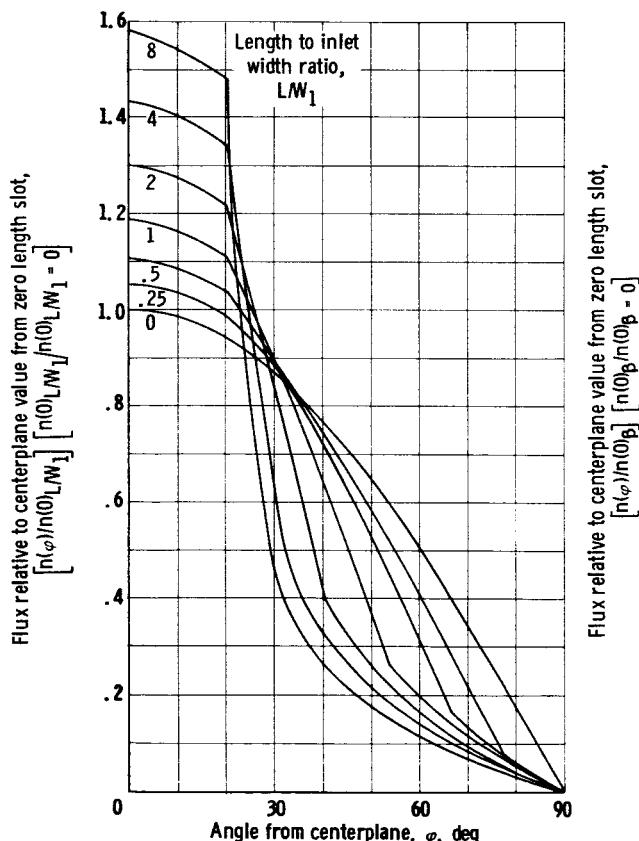


Figure 15. - Comparison of far-field relative flux from slots of different length to inlet width ratios.

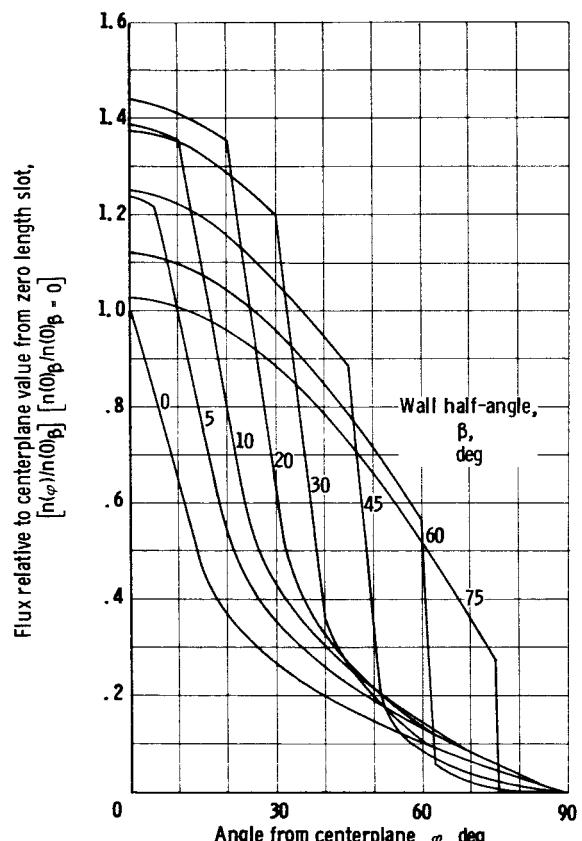


Figure 16. - Comparison of relative flux from slots of different wall half-angles. Length to inlet width ratio, 4.